

Supply Chain Resilience: Should Policy Promote International Diversification or Reshoring?*

Gene M. Grossman
Princeton University

Elhanan Helpman
Harvard University

Hugo Lhuillier
Princeton University

January 2, 2023

Abstract

Little is known about optimal policy in the face of global supply chain disruptions. Should governments promote resilience by subsidizing backup sources of input supply in multiple countries? Should they encourage firms to source from safer, domestic suppliers? We address these questions in a model of production with a critical input and exogenous risks of supply disturbances. With CES preferences, a subsidy for diversification achieves the constrained social optimum. When the demand elasticity rises with price, private investments in resilience may be socially excessive and the social planner may wish to discourage diversification while favoring sourcing from abroad.

Keywords: global supply chains, global value chains, input sourcing, resilience,

JEL Classification: F13, H21, F12

*We are grateful to David Baqaee and Kiminori Matsuyama for very helpful discussions and to Maxim Alekseev and Alejandro Sabal for excellent research assistance.

1 Introduction

The United States needs resilient, diverse, and secure supply chains to ensure our economic prosperity and national security. Pandemics and other biological threats, cyber-attacks, climate shocks and extreme weather events, terrorist attacks, geopolitical and economic competition, and other conditions can reduce critical manufacturing capacity and the availability and integrity of critical goods, products, and services. Resilient American supply chains will revitalize and rebuild domestic manufacturing capacity, maintain America’s competitive edge in research and development, and create well-paying jobs.

Joseph R. Biden, Jr., Executive Order on America’s Supply Chains, February 24, 2021

Supply chain disruptions have become the new normal. The Great East Japan Earthquake of 2011 and the massive tsunami that it triggered brought such events to the attention of economists. Since then, hardly a month passes without news of a fresh disturbance. The pace of disruptions has quickened with the advent of the COVID-19 pandemic, and now we hear regularly of supply chain breakdowns in industries as disparate as automobiles, dishwashers, plastics, copper wire, lumber, pork, and toilet paper.

Disruptions have a myriad of causes. They result from natural disasters, geopolitical disputes, transportation failures, cyber-attacks, fires, power outages, labor shortages, human error and pandemic lockdowns. McKinsey Global Institute (2020), which recently conducted a series of interviews with supply chain experts, reports that disruptions lasting one to two weeks happen to a given company on average every second year, while those lasting one to two months occur every 3.7 years. The disruptions impose significant costs, presenting firms with expected losses per decade that averaged 42% of their annual pre-tax earnings (see Exhibit E5 on p.12).

Many commentators associate the increasing frequency and severity of supply chain disruptions with the perils of globalization.¹ *Global* supply chains leave firms exposed to risks in multiple countries, some quite distant from where consumption takes place. This perceived connection between supply shortages and international trade, in turn, has sparked soul searching amongst policy makers and a call to action in the broader public. If costly shocks reflect concentration of input supplies, wouldn’t it be sensible for governments to encourage firms to diversify their international sourcing? And if distance from suppliers intensifies the risk of disruption, wouldn’t it be better to bring some parts of the supply chains closer to home? The preamble to President Biden’s Executive Order suggests that “*diverse* and secure supply chains” are a prerequisite for economic prosperity and that “resilient American supply chains” will rest on “rebuil[t] *domestic* manufacturing capacity [emphasis added].”

Little is known about the efficacy of policies aimed at global supply chain management in an environment with recurring disturbances. Disruptions generate input shortages that can give rise to price spikes or even outright unavailability of downstream products. Consumers suffer from

¹See, for example, Shih (2020a, 2020b), Iakovou and White III (2020), and Baldwin and Freeman (2022).

their hampered ability to purchase the products they covet. To the extent that households forfeit consumer surplus in the face of supply chain disruptions, governments may have reason to enact policies that curtail their occurrence. But production impediments impact not only consumers' surplus, but also firms' bottom lines. The question for governments is not whether shortages adversely affect households, but whether firms' private incentives to avoid such shortages fall short of (or exceed) what is socially desirable.

In this paper, we propose a bare-bones framework to evaluate policies that can alter the organization of global supply chains. We abstract from all complexity in the production process by assuming that home firms manufacture unique varieties of nontraded differentiated products using a single, critical input. Firms face a choice of whether to procure their inputs at home or abroad. Sourcing from a foreign supplier is tempting, because production costs are assumed to be cheaper there. But foreign sourcing may be riskier than local sourcing, for geopolitical, logistical or other reasons. Thus, firms may face a tradeoff between the lower costs of offshoring and the greater safety of onshoring. They might also invest in resilience by establishing multiple supply relationships. Redundancy is costly, but it allows a firm to be active in more states of the world.

Focusing on welfare in the country where the final goods are consumed, we identify three potential distortions in private sourcing decisions. First, firms typically do not capture all of the surplus generated by the availability of their product. This *consumer-surplus externality* suggests that too many firms may be ready to accept the extra risk of foreign sourcing in exchange for lower expected costs and that too few firms may bear the extra costs of diversification. Meanwhile, when firms manage to avoid disruptions, some of their profits come at the expense of competitors that are also viable in the same state of the world. This *business-stealing externality* tends to lead firms to *overweight* the resilience of their networks. Finally, a *consumption distortion* arises when prices of differentiated products exceed marginal costs while other goods are priced competitively. In a setting with potential supply disruptions and positive markups, government policy might be directed to encourage product availability in states of the world when markups would otherwise be especially high.

Inasmuch as the social cost of supply chain disruptions stems from loss of consumer surplus, the form of consumer preferences plays a crucial role in our policy analysis. It has become commonplace to use CES preferences in trade models with endogenous entry, but the very special properties of these preferences have been recognized since the seminal work by Dixit and Stiglitz (1977). In many contexts with CES preferences, the consumer-surplus externality from extra product variety happens to exactly offset the business-stealing externality from extra competition. These considerations apply as much to investments in “resilience” as they do to investments in entry, so it is important for understanding the efficient organization of global supply chains to allow for more flexible forms of demand. To this end, we follow Matsuyama and Ushchev (2017, 2020a) in adopting a broader class of preferences that are *Homothetic with a Single Aggregator* (HSA). With HSA preferences, the demand for any variety depends on its price relative to a (common) aggregator of all prices. The CES utility function is a member of this class, but, more generally, HSA preferences

allow the demand elasticity to increase with price. This property of demand, which characterizes many consumer goods, has been termed “Marshall’s Second Law of Demand” (or MSLD). When it applies, the consumer-surplus and business-stealing externalities do not cancel.

We find that, with CES preferences for the differentiated products and optimal subsidies to address consumption distortions arising from markup pricing, the planner need not influence incentives for diversification, nor those for sourcing at home versus abroad. But with more general forms of HSA preferences that obey MSLD, the planner requires not only consumption subsidies, but also a policy to discourage diversification and another to alter the incentives to form chains at home versus abroad. The optimal diversification tax corrects for the business-stealing externality, which generally exceeds the consumer-surplus externality under MSLD. The optimal policy to influence offshoring versus onshoring reflects that, with a non-constant elasticity of substitution, the benefits from greater competition differ across states of the world.

Turning to the second-best policy problem that arises when consumption subsidies are infeasible, we find that CES preferences dictate a subsidy for diversification as the only necessary supply chain policy. These subsidies are a second-best response to the distortion from markup pricing. However, with more general HSA preferences, the second-best policy must also take into account the dominance of the business-stealing externality relative to the consumer-surplus externality, as well as the different distortions from markup pricing that emerge in different states of the world. For example, if production costs abroad are nearly the same as those at home but the risk of a supply disruption is higher, there will be reduced product availability and less competition in states of the world when procurement from foreign suppliers is disrupted than in states where disturbances happen locally. Price-cost markups will be larger in the former states absent government policy, and second-best policy will tilt supply chain formation in favor of offshoring. On the other hand, if the two countries are relatively similar in their risks but differ greatly in costs, a tax on offshoring or a subsidy for onshoring may be indicated.

Our paper fits into an earlier literature on trade disruptions in a neoclassical setting. Much of this previous work addressed optimal policy responses to potential trade embargoes. Mayer (1977) showed that production subsidies are an optimal response to threats of trade interruption in the presence of costly adjustment. Bhagwati and Srinivasan (1976) made the likelihood of a disruption a function of the volume of trade and elucidated an efficiency role for tariffs to give agents an incentive to internalize the externality arising from their effect on the probability of a trade restriction. Arad and Hillman (1979) extended these earlier papers to allow for learning-by-doing in the production of a good that might later be subject to an embargo. Bergström et al. (1985) developed an infinite-horizon model to study the potential role of inventories to mitigate the threat of embargo. Perhaps the most sophisticated of these early studies was that by Cheng (1989), who considered recurrent embargo threats as a stationary Markov process that plays out with constraints on the speed of intersectoral reallocation.

The main difference between our work and this earlier literature stems from our treatment of the endogenous availability of differentiated products. With perfect competition and homogeneous

goods, aggregate *quantities* matter for welfare but the availability of a particular firm’s offering does not. If a disruption causes some import good to be unavailable, there is no harm to consumers beyond the higher price of the domestic (perfect) substitutes. Of course, higher sticker prices play a role in a world with differentiated products, but there is also a direct harm to consumers from a particular variety not being available for purchase. For this reason, we believe that endogenous determination of the set of available products should feature prominently when evaluating policy toward supply-chain security.

Our paper also relates to a literature on distortions in the entry process, which began with the seminal paper by Dixit and Stiglitz (1977) and includes more recent contributions by Bilbiie et al. (2012), Matsuyama and Ushchev (2020a), Baqaee and Farhi (2020), among others. This literature focuses on entry of new firms into an industry in settings with imperfect competition. Bilbiie et al. (2012) study pricing and entry over the business cycle, focusing on intertemporal variation in markups and their relation to intertemporal marginal rates of substitutions. Baqaee and Farhi (2020) decompose the welfare losses from inefficient pricing and entry by calculating second-order approximations around an efficient equilibrium, while mostly treating markups as given. Matsuyama and Ushchev (2020a) analyze the inefficiencies that arise in a one-sector model with endogenous entry and endogenous markups. They introduce HSA preferences to allow for non-constant markups and Marshall’s Second Law of Demand, an original approach that proves very useful in our context as well. Our paper differs from this literature inasmuch as we do not consider new entry into an industry, but rather the organization of supply chains that determines product availability in different states of the world. Unlike Baqaee and Farhi (2020), we derive exact wedges that describe the gaps between social valuations and private valuation and use these wedges to characterize first-best and second-best policies. Our model is designed to address inefficiencies in *global* value chains in the face of supply disruptions and so we emphasize the asymmetries in cost and risk that often characterize international trade in intermediate goods.²

The remainder of this paper is organized as follows. In Section 2, we develop our model of risky supply chains and describe the *laissez-faire* equilibrium. Then, in Section 3, we pose and solve the social planner’s problem that arises when she has access to state-and-product specific consumption subsidies to offset the inefficiencies caused by monopoly pricing. We characterize the “wedges” between social and private incentives for forming supply relationships in each country relative to an alternative of diversified sourcing. Armed with this understanding of the sources of inefficiency in supply-chain formation, we turn in Section 4 to the more realistic policy problem that arises when consumption subsidies are infeasible. We characterize the supply chain policies that achieve a constrained optimum for arbitrary cost and risk parameters when preferences take the CES form. For more general, HSA preferences, we derive analytical results that apply when cost and risk parameters are not very different in the two countries. We then turn to numerical simulations in Section 5 to extend our insights to asymmetric cost and risk parameters. Section 6 concludes. An

²A tangentially related paper is Elliot et al. (2022), who study networks with idiosyncratic probabilities of breakup that depend on investment choices. They do not entertain aggregate shocks as here. Rather, they are interested in the propagation of idiosyncratic shocks up and down the supply chain.

online appendix contains further details, proofs, and additional numerical simulations.

2 A Simple Model of Risky Supply Chains

2.1 Supply Relationships

The home economy can produce a homogeneous, numeraire good and potentially a unit measure of nontraded differentiated consumer products. Revenues from sales of the numeraire good amount to \bar{Y} , all of which is paid to workers as labor income. Production of differentiated products requires no labor. Rather, firm ω in this industry converts a single, customized critical input into the final good ω using the linear production technology,

$$x(\omega) = m(\omega),$$

where $x(\omega)$ is output of good ω and $m(\omega)$ is the quantity of the customized input.³ If the firm has established a supplier relationship in country i and if that supply chain is operative, then the firm can procure the customized inputs at a cost of q_i per unit, $i \in \{H, F\}$, where the subscripts denote “home” and “foreign,” respectively, and we assume that $q_F < q_H$ to capture the motive for the internationalization of the value chain.⁴

To form any supply relationship, a firm must bear a sunk investment cost, k , in units of the numeraire good. This cost represents the up-front outlays associated with searching for a partner, negotiating a contract, and designing a suitable input. It captures the costliness of resilience, inasmuch as firms that form multiple supply relationships bear extra expenses compared to those whose supply chain is more streamlined.

Once a supply relationship has been established, it is subject to two possible “disruption shocks.” With probability $1 - \rho \geq 0$, any particular supply chain breaks down for exogenous and idiosyncratic reasons, which might be a failure of the prototype input, a strike in the supplier factory, a localized weather event in the location where the input would be produced, or anything else that happens independently of all other supply relationships. In any of these circumstances, the downstream firm loses the ability to purchase its input from the particular supplier for the length of the period captured by our model.⁵ In the complementary event, with probability $0 < \rho \leq 1$, no idiosyncratic supply disruption occurs and the firm can buy as much as it wants from the particular supplier provided that the latter is located in a country that is “open for business.”⁶ However,

³Note that the “producer” of the final good might actually be a retailer and the “input” might be a consumer product.

⁴The constant cost of procurement fits best with a market structure in which the downstream firm is vertically integrated with its upstream subsidiaries. Alternatively, we can imagine a situation in which the downstream firm has all the bargaining power in its relationship with arms-length suppliers and the marginal cost of the input is constant.

⁵We treat all disruptions as catastrophic; when they occur, they eliminate all input supply from the affected source. Alternatively, we could allow for less severe shocks that limit supply to some positive quantity or that raise the cost of purchases above q_i .

⁶Our analysis could be conducted without the idiosyncratic shocks, i.e., with $\rho = 1$. However, $\rho < 1$ provides an additional incentive for diversification, and it implies that not all firms will be able to operate even when neither

with probability $1 - \gamma_i$ a country-wide shock disrupts all chains with suppliers in country i . These shocks, which we assume to be independent across countries (to simplify the expressions, but with no substantive importance), represent events such as epidemics, political conflicts between national governments, or failures of the national transportation system. The relative safety of the home country is captured by the assumption that $\gamma_H > \gamma_F$.

The realizations of the two country-wide shocks generate four possible aggregate states of the world that we denote by $J \in \{H, F, B, N\}$. In state H , which occurs with probability $\delta^H = \gamma_H(1 - \gamma_F)$, foreign sources of supply are unavailable, but a firm that has a supplier in the home country can still operate, conditional on its relationship there surviving any idiosyncratic shock. In state F , which happens with probability $\delta^F = \gamma_F(1 - \gamma_H)$, a common shock hits home input suppliers and only those downstream firms with supply relationships abroad might operate. In state B , no broad-based disruptions occur and every downstream firm that avoids idiosyncratic shocks to some of its supply relationships will produce positive output. This state arises with probability $\delta^B = \gamma_H\gamma_F$. Finally, with the residual probability $\delta^N = (1 - \gamma_H)(1 - \gamma_F)$, both countries suffer adverse shocks and no production or consumption of differentiated products takes place.

2.2 Preferences and Demand

There is a unit mass of identical consumers in the home country. The representative consumer is risk neutral and holds quasi-linear preferences over consumption of the homogeneous good, Y , and consumption of an aggregate index of differentiated products, X . We represent her (cardinal) utility as

$$V(X, Y) = Y + U(X), \tag{1}$$

where $U(\cdot)$ has a constant elasticity $\varepsilon > 1$;⁷ i.e.,

$$U(X) = \frac{\varepsilon}{\varepsilon - 1} \left(X^{\frac{\varepsilon - 1}{\varepsilon}} - 1 \right) \quad \text{for } \varepsilon > 1.$$

Each consumer maximizes utility in any state of the world subject to a standard budget constraint, $Y + \int_{\omega \in \Omega} p(\omega) x(\omega) d\omega = I$, where $p(\omega)$ is the price and $x(\omega)$ the quantity purchased of variety ω , Ω is the set of varieties available in the relevant state, and I is income. When consumers have sufficient income, the constant elasticity of $U(X)$ gives rise to a constant-elasticity demand

country suffers a broad-based disruption. Moreover, the number of active firms in the state of the world when neither source country is fully disrupted will depend on the sourcing strategies adopted by the firms, which then becomes a consideration in the choice of policy.

⁷A unitary elasticity can be treated as a limiting case as $\varepsilon \rightarrow 1$. We cannot allow $\varepsilon = 1$, because then $V \rightarrow -\infty$ in the state of the world when all firms face supply disruptions in both countries. We could introduce a backup technology such that firms can produce their own critical inputs at some high cost $\bar{q} > q_H$ and then we could entertain $\varepsilon = 1$ and even $\varepsilon < 1$. But introducing the additional parameter \bar{q} complicates the expressions without providing additional insights. Accordingly, we choose to restrict the range of the demand elasticity, in keeping with the empirical evidence provided by Fajgelbaum et al. (2020).

for differentiated products,

$$X = P^{-\varepsilon}, \quad (2)$$

where P is the real price index dual to U . The consumer spends $PX = P^{1-\varepsilon}$ on differentiated products and devotes residual spending of $I - P^{1-\varepsilon}$ to the homogeneous good.

Following Matsuyama and Ushchev (2017, 2020a), we assume that preferences for the bundle of differentiated products belong to a class they aptly term *Homothetic with a Single Aggregator*. Homotheticity implies that the consumption index X is a linearly homogenous function of consumption of the individual varieties $\{x(\omega)\}_{\omega \in \Omega}$. A single aggregator, A , which is a linearly homogenous function of the set of prices $\{p(\omega)\}_{\omega \in \Omega}$, guides the substitution between a particular variety ω and all other varieties. More formally, HSA preferences require the existence of a price aggregator A and market-share function $s[p(\omega)/A]$ that is non-negative for all relative prices such that

$$\frac{d \log P}{d \log p(\omega)} = s[z(\omega)] \quad (3)$$

and

$$\int_{\omega \in \Omega} s[z(\omega)] d\omega = 1, \quad (4)$$

where $z(\omega) := p(\omega)/A$ is the price of variety ω relative to the price aggregator. Equation (3) expresses the demand for any variety ω in implicit form; the substantive assumption is that this demand depends only on the price of that variety relative to a *common* aggregator. Equation (4) stipulates that the market shares sum to one.

We place some mild restrictions on the market-share function, $s(z)$. First, we impose

Assumption 1 *The market-share function $s(z)$ is strictly decreasing when positive, with $\lim_{z \rightarrow \bar{z}} s(z) = 0$, for $\bar{z} \equiv \inf \{z > 0 \mid s(z) = 0\}$.*

The assumption that $s(z)$ is strictly decreasing ensures that all varieties in X are gross substitutes. It admits both the case when $\bar{z} < \infty$, so that demand “chokes” at some finite relative price, and the case $\bar{z} = \infty$, when positive quantities are demanded at any finite price. We also assume that the aggregator A is well defined for any measure of firms.⁸

Equation (3) implies that the elasticity of substitution between any two goods with equal prices is a function of the common relative price, and is given by

$$\sigma(z) = 1 - \frac{zs'(z)}{s(z)} > 1.$$

We further adopt

⁸Matsuyama and Ushchev (2020b, 2022) discuss various ways to ensure the existence of a well-defined aggregator, such as, for example, limiting the size of the market relative to the fixed cost of entry or assuming that $s(z)$ is large enough for the lowest feasible value of z .

Assumption 2 (i) Either $\sigma(z) = \sigma$ or $\sigma'(z) > 0$ for all $z \in (0, \bar{z})$ and (ii) $\sigma(z) > \varepsilon$ in the neighborhood of the equilibrium and the social optimum.

The first part of Assumption 2 allows for the case of *Symmetric CES* preferences, where $s(z) = \alpha z^{1-\sigma}$, $\alpha > 0$. For all other HSA preferences, we impose *Marshall's Second Law of Demand (MSLD)*, namely that the demand for a good becomes more elastic as its price rises.⁹ For example, the *Symmetric Translog* preferences, developed by Feenstra (2003), drawing on Diewert (1974), satisfy MSLD. These preferences can be represented by a market-share function $s(z) = -\theta \log z$, $z \in (0, 1)$, $\theta > 0$. Then $\sigma(z) = 1 - 1/\log z$.

The second part of Assumption 2 ensures that the demand for any variety ω increases when the aggregate price of competing brands rises. For some market-share functions, this assumption might be satisfied at all values of $z \in (0, \bar{z})$. For others, we would need to verify that it is satisfied *ex post*, i.e., after solving for the equilibrium.

Finally, we note for future reference the relationship between the price index P and the demand aggregator A that applies for any HSA preferences. Matsuyama and Ushchev (2020a) prove that

$$\log P = C + \log A - \int_{\omega \in \Omega} \int_{p(\omega)/A}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta d\omega, \quad (5)$$

where C is a constant.

2.3 Profit Maximization in State J

Once the state of the world has been realized, the surviving producers purchase inputs and set prices to maximize profits taking into account the aggregate demand for differentiated profits (summarized by P^J) and the competition they face (summarized by A^J). The firm producing variety ω maximizes its profits in state J by procuring its inputs from its least-cost, viable supplier and by marking up its price relative to that cost. Specifically, a firm that pays q_K for its inputs in state J solves

$$p^{J,K}(\omega) = \arg \max_{\mathbf{p}} (P^J)^{1-\varepsilon} s\left(\frac{\mathbf{p}}{A^J}\right) \mathbf{p}^{-1} [\mathbf{p} - q_K] \text{ for } J \in \{H, F, B\}, K \in \{H, F\},$$

taking the state-contingent price index P^J and the state-contingent aggregator A^J as given. Profit maximization requires

$$p^{J,K}(\omega) = \frac{\sigma[z^{J,K}(\omega)]}{\sigma[z^{J,K}(\omega)] - 1} q_K \quad (6)$$

⁹Zhelobodko et al. (2012) and Mrázová and Neary (2017) introduce MSLD by assuming what they refer to as “increasing relative love of variety” and “sub-convex” demand, respectively. In each case, their preferences are directly explicitly additive (DEA), which rules out homotheticity; see Matsuyama and Ushchev (2017). One advantage of the HSA class of utility functions, relative to DEA and many others used in the literature, is that it allows for a non-constant elasticity of substitution without violating homotheticity. See Matsuyama (2019) for further discussion.

and yields operating profits

$$\pi^{J,K}(\omega) = \frac{s[z^{J,K}(\omega)]}{\sigma[z^{J,K}(\omega)]} (P^J)^{1-\varepsilon}, \quad (7)$$

where $z^{J,K}(\omega) := p^{J,K}(\omega)/A^J$.¹⁰ Notice that the price of any variety might vary across states of the world and with the source of its inputs. The markup reflects the elasticity of demand, as usual, but the latter is not constant; rather, it reflects the cost and availability of inputs. Markups will be higher in states of nature with dampened competition due to supply disruptions than in states with more ample competition. Similarly, markups will be higher for goods produced with high cost (domestic) inputs than goods produced with cheaper (foreign) inputs.

2.4 Supply Chain Management

The identical households collectively own the unit measure of downstream (potential) producers. Since the quasi-linear utility represented by (1) implies that these households are risk neutral with respect to income shocks, the firms make their ex-ante investment to maximize expected profits. We allow firms to choose among three modes of organization (plus exit). Strategy h entails investment in a single supply relationship in the home country in the hope of “onshoring.” Strategy f entails investment in a single relationship in the foreign country in the hope of “offshoring.” Strategy b (for “both”) involves diversification, i.e., investment in supply relationships in both places with the intention of sourcing from the low-cost foreign supplier if that is possible, and from the higher-cost domestic supplier if that is possible and the low-cost foreign option is not available.¹¹

Firms calculate expected profits with rational expectations about prices, sales, and costs in each state of the world, in view of the fraction of their competitors that pursues each strategy in equilibrium. Let μ_j be the fraction of firms that opt for strategy j , $j \in \{h, f, b\}$, with $\sum_j \mu_j \leq 1$. In state H , when all foreign sources of supply are disrupted, only those firms that have chosen strategy h or strategy b might operate, and among those, only the ones that avoid an idiosyncratic shock to their home supplier. Each such firm faces competition from $\rho(\mu_h + \mu_b)$ others, all of which have a unit cost of q_H . Analogously, in state F , it is the firms that pursued strategy f or strategy b that might produce. Again, only a fraction ρ can do so, because the others suffer relationship-specific supply disturbances. It follows that in state F , an active firm competes with $\rho(\mu_f + \mu_b)$ others, each of which has a unit cost of q_F . Recognizing that all firms operating in state H have common costs q_H and those operating in state F have common costs q_F , we can use (6) and (7) to calculate the values of $\pi^H(\omega)$ and $\pi^F(\omega)$ that accrue to all firms operating in those states.¹²

¹⁰Equations (6) and (7) reduce to the familiar pricing and profit expressions for the CES case, where σ is constant and $s(z) = \alpha z^{1-\sigma}$.

¹¹In principle, a firm that diversifies may choose to invest in multiple supply relationships in the same country. To avoid a taxonomy, we do not consider this possibility here; it will not be an attractive option for ρ close to one.

¹²Recognizing that all firms operating in state H source their inputs from H , and that all firms operating in state F source their inputs from F , we henceforth omit the superscript K for any variable $\xi^{J,K}$ that applies when $J = H$ or F . For example, we use π^H in place of $\pi^{H,H}$, z^H in place of $z^{H,H}$, etc. Also, with some abuse of notation, we write $\xi^J(\mu)$ for the variable $\xi^J(\omega)$, when the value of ξ^J is common to all firms operating in state J and that value

A firm's profit in state B in which supply chains in both countries are active is slightly more complicated. In this state, firms that adopt either strategy f or strategy b anticipate a cost of q_F with probability ρ . Those that diversify by choosing strategy b anticipate that they will rely on their backup supplier, at the higher cost q_H , with probability $\rho(1 - \rho)$. Meanwhile, firms that pursue strategy h also produce at q_H , but with probability ρ . It follows that all firms anticipate competition in state B from $(\mu_f + \mu_b)\rho$ others producing at cost q_F and from $\mu_h\rho + \mu_b\rho(1 - \rho)$ others producing at cost q_H .

Let Π_j be the expected profit that a firm can earn by pursuing strategy j , $j \in \{h, f, b\}$. Recalling that δ^J is the probability of state J , $J \in \{H, F, B\}$, we have using (6) and (7) that

$$\Pi_h = \Pi_h(\boldsymbol{\mu}) := \delta^H \frac{s[z^H(\boldsymbol{\mu})]}{\sigma[z^H(\boldsymbol{\mu})]} P^H [z^H(\boldsymbol{\mu})]^{1-\varepsilon} \rho + \delta^B \frac{s[z^{B,H}(\boldsymbol{\mu})]}{\sigma[z^{B,H}(\boldsymbol{\mu})]} P^B(\boldsymbol{\mu})^{1-\varepsilon} \rho - k, \quad (8)$$

$$\Pi_f = \Pi_f(\boldsymbol{\mu}) := \delta^F \frac{s[z^F(\boldsymbol{\mu})]}{\sigma[z^F(\boldsymbol{\mu})]} P^F [z^F(\boldsymbol{\mu})]^{1-\varepsilon} \rho + \delta^B \frac{s[z^{B,F}(\boldsymbol{\mu})]}{\sigma[z^{B,F}(\boldsymbol{\mu})]} P^B(\boldsymbol{\mu})^{1-\varepsilon} \rho - k, \quad (9)$$

and

$$\begin{aligned} \Pi_b = \Pi_b(\boldsymbol{\mu}) := & \sum_{J=H,F} \delta^J \frac{s[z^J(\boldsymbol{\mu})]}{\sigma[z^J(\boldsymbol{\mu})]} P^J [z^J(\boldsymbol{\mu})]^{1-\varepsilon} \rho \\ & + \delta^B \left\{ \frac{s[z^{B,F}(\boldsymbol{\mu})]}{\sigma[z^{B,F}(\boldsymbol{\mu})]} + \frac{s[z^{B,H}(\boldsymbol{\mu})]}{\sigma[z^{B,H}(\boldsymbol{\mu})]} (1 - \rho) \right\} P^B(\boldsymbol{\mu})^{1-\varepsilon} \rho - 2k. \end{aligned} \quad (10)$$

In equilibrium, if one strategy j dominates the other two, all active firms will make that choice, and so $\mu_\ell = 0$ for $\ell \neq j$. If two strategies yield positive and equally high expected profits and higher than the third, then these two will have positive fractions in equilibrium, while the third will find no takers. The fractions will be such as to generate indifference. Finally, if there exist $\mu_h > 0$, $\mu_f > 0$ and $\mu_b > 0$ such that $\Pi_h = \Pi_f = \Pi_b > 0$, then the equilibrium will exhibit a positive number of firms pursuing each of the available strategies.¹³

2.5 Welfare

We adopt expected indirect utility as our welfare metric, weighting utility in each aggregate state by the likelihood of that state. Indirect utility comprises labor income, profits, tax revenues (if any) and consumer surplus.

Expected welfare reflects the fractions of firms that choose each organizational mode, outcomes that can be influenced by government policy. When the fraction of firms that adopt strategies h , f and b are, respectively μ_h , μ_f , and μ_b , aggregate expected profits (net of any subsidies or taxes received or paid by firms in recognition of their supply chain choices) amount to $\sum_{j=h,f,b} \mu_j \Pi_j(\boldsymbol{\mu})$. Consumer surplus in state J is given by $\frac{1}{\varepsilon-1} P^J(\boldsymbol{\mu})^{1-\varepsilon}$ for $J \in \{H, F, B\}$. In the event that both

depends on the vector $\boldsymbol{\mu} := (\mu_h, \mu_f, \mu_b)$.

¹³Since firms have the option to exit, it is possible that $\sum_j \mu_j < 1$, in which case all firms that do not exit make zero expected profits net of the fixed costs.

countries are hit with supply disruptions, consumption of all differentiated products is zero ($X = 0$) and so consumer surplus vanishes. Therefore,

$$W(\boldsymbol{\mu}) = \bar{Y} + \sum_{J=H,F,B} \delta^J T^J(\boldsymbol{\mu}) + \sum_{j=h,f,b} \mu_j \Pi_j(\boldsymbol{\mu}) + \frac{1}{\varepsilon - 1} \sum_{J=H,F,B} \delta^J P^J(\boldsymbol{\mu})^{1-\varepsilon}, \quad (11)$$

where \bar{Y} is the (fixed) labor income from producing the numeraire good, $T^J(\boldsymbol{\mu})$ is tax revenues collected by the government and rebated to households in state J (possibly zero or negative) beyond what is paid to or collected from firms in connection with their supply chain choices.

2.6 The *Laissez-Faire* Equilibrium

In the absence of any government policy, we can use the fact that all strategies used in equilibrium maximize expected profits and the fact that product markets must clear in every state to solve for $\boldsymbol{\mu}$, as well as the state-contingent aggregators A^H , A^F , and A^B . Market shares must sum to one in every state; i.e.,

$$\rho(\mu_h + \mu_b) s[z^H(\boldsymbol{\mu})] = 1, \quad (12)$$

$$\rho(\mu_f + \mu_b) s[z^F(\boldsymbol{\mu})] = 1 \quad (13)$$

and

$$\rho(\mu_f + \mu_b) s[z^{B,F}(\boldsymbol{\mu})] + \rho[\mu_h + (1 - \rho)\mu_f] s[z^{B,H}(\boldsymbol{\mu})] = 1. \quad (14)$$

In state B , we need one more equation to solve for prices, which comes from comparing the optimal prices (6) for firms that source their inputs in H versus F . This gives

$$\frac{z^{B,F}(\boldsymbol{\mu})}{z^{B,H}(\boldsymbol{\mu})} = \frac{\frac{\sigma[z^{B,F}(\boldsymbol{\mu})]}{\sigma[z^{B,F}(\boldsymbol{\mu})]-1} q_F}{\frac{\sigma[z^{B,H}(\boldsymbol{\mu})]}{\sigma[z^{B,H}(\boldsymbol{\mu})]-1} q_H}.$$

Further details for computing the *laissez-faire* equilibrium can be found in Sections 2.4 and 2.6 of the appendix.¹⁴

Figure 1 illustrates the fraction of firms that choose each organizational form for different values of k . The figure is drawn for the case in which production costs are roughly similar ($q_H \approx q_F$), but sourcing from the home country is significantly safer than sourcing from abroad ($\gamma_H \gg \gamma_F$). For $k < k_1$ in the figure, the fixed cost of a sourcing relationship is sufficiently small that all firms find it worthwhile to invest in resilience, so $\mu_b = 1$ and $\mu_h = \mu_f = 0$. Next comes a range of fixed costs $k \in (k_1, k_2)$ for which some firms are diversified, and others source only from the safer country H . For higher fixed costs such that $k \in (k_2, k_3)$ in the figure, each of the three strategies is deployed in equilibrium by some positive number of firms. When k surpasses k_3 , it is no longer profitable

¹⁴Section numbers in the appendix correspond to the sections in the main text. Henceforth, when we refer to the appendix for formal arguments, we will only note the section number when it is an exception to this general rule.

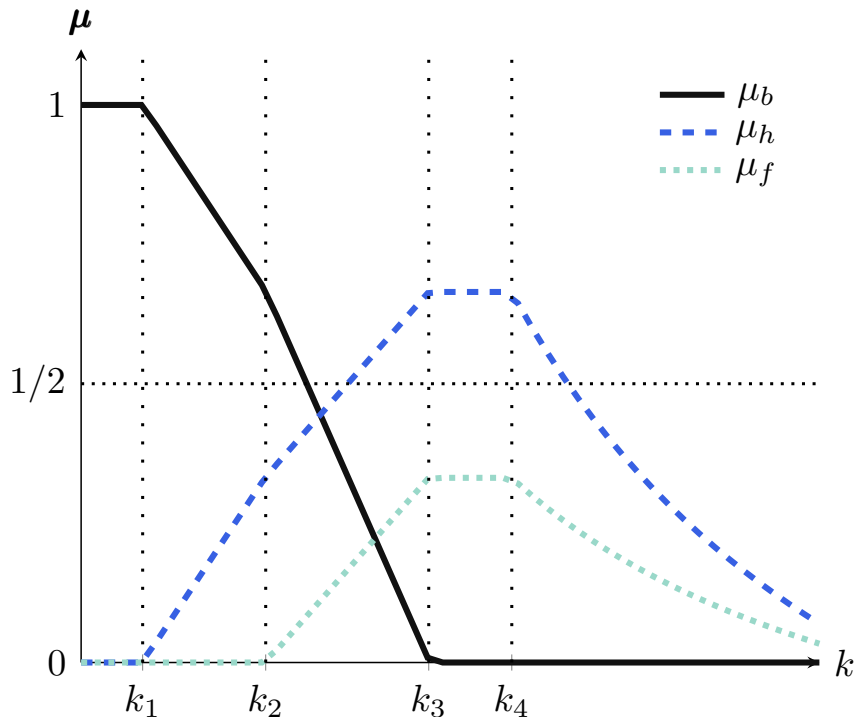


Figure 1: Supply Chain Outcomes for $\gamma_H \gg \gamma_F$, $q_H \approx q_F$

for any firm to diversify; $\mu_b = 0$. Then, for $k \in (k_3, k_4)$, a marginal change in the fixed cost has no effect on the relative profitability of strategy h versus strategy f . But once k increases beyond k_4 , the expected operating profits are not sufficient for the full unit measure of firms to cover fixed costs; some firms exit, so that $\mu_h + \mu_f < 0$ and $\Pi_h = \Pi_f = 0$. The total number of firms might remain positive but continue to fall with further increases in k , or else μ_f and then μ_h might reach zero for some finite values of $k > k_4$.¹⁵

Figures analogous to Figure 1 can be drawn for other configurations of cost and risk parameters. In what follows, we focus exclusively on circumstances that give rise to the use of all available strategies in equilibrium, i.e., $\mu_h > 0$, $\mu_f > 0$, and $\mu_b = 1 - \mu_h - \mu_f > 0$. This outcome seems to resemble most closely what we observe in reality.¹⁶

3 The Unconstrained Social Optimum

Do private incentives for firms to invest in safe and resilient supply relationships align with social incentives in the absence of government policy? If the answer is no, can the social planner intervene to restore social efficiency? The answer to the second question may depend on the set of policy

¹⁵For some preferences, such as symmetric CES, operating profits in a state approach infinity as the number of varieties available in the state approaches zero, in which case some (shrinking number) of firms will invest in supply relationships in each state of the world. For other preferences, the potential operating profits per variety may be bounded. Then, for k large enough, all firms exit the industry.

¹⁶The cases in which some strategies are not used by any firms could be analyzed similarly, but do not generate any interesting insights beyond what we recount below.

instruments that the government has at its disposal to influence resource allocation. As is well known, the markup pricing reflected in equation (6) creates a wedge between social and private incentives to consume differentiated products relative to the homogeneous good, because consumers face a price in excess of marginal cost for the former, but a price equal to marginal cost for the latter. As in other contexts (see, for example, Dhingra and Morrow, 2019, and Campolmi et al., 2021), this distortion can be eliminated, in principle, by an optimal set of consumption subsidies. In practice, such subsidies are difficult to implement and rarely observed; in our setting with non-constant markups, the subsidies must vary with both the state of nature (H, F , or B) and with the source of the inputs embodied in the final good.¹⁷ Nonetheless, it is instructive to begin our analysis under the assumption that optimal subsidies are feasible, to focus squarely on the wedges between private and social incentives for supply chain formation. In this section, we study the unconstrained (or “first-best”) planner’s problem, leaving the more realistic, constrained (or “second-best”) problem for the next section. By assuming away the distortions caused by markup pricing, we are able to develop intuition for whether and when the incentives firms face to invest in safety and resilience are excessive, insufficient or appropriate.

To characterize the optimal supply chain policies, we define the wedge between private and social incentives to pursue strategy j relative to strategy b when the existing mix of strategies is $\boldsymbol{\mu}$ as

$$\tilde{w}_j(\boldsymbol{\mu}) := \left[\tilde{\Pi}_j(\boldsymbol{\mu}) - \tilde{\Pi}_b(\boldsymbol{\mu}) \right] - \frac{d\tilde{W}(\boldsymbol{\mu})}{d\mu_j}, \quad j \in \{h, f\}, \quad (15)$$

where tildes indicate relationships that apply with optimal consumption subsidies in place and

$$\frac{d\tilde{W}(\boldsymbol{\mu})}{d\mu_j} := \frac{\partial \tilde{W}(\mu_h, \mu_f, \mu_b)}{\partial \mu_j} - \frac{\partial \tilde{W}(\mu_h, \mu_f, \mu_b)}{\partial \mu_b}, \quad j \in \{h, f\}$$

is the marginal change in welfare from a small change in μ_j at the expense of μ_b ; i.e., $d\mu_j = -d\mu_b$.¹⁸

At an (interior) first-best allocation $\boldsymbol{\mu}^o$, the first-order conditions for welfare maximization require $d\tilde{W}_j(\boldsymbol{\mu}^o)/d\mu_j = 0$ for $j \in \{h, f\}$. Therefore, the first best can be achieved by a set of subsidies that satisfy

$$\tilde{w}_j(\boldsymbol{\mu}^o) = \tilde{\Pi}_j(\boldsymbol{\mu}^o) - \tilde{\Pi}_b(\boldsymbol{\mu}^o) = \varphi_b - \varphi_j, \quad j \in \{h, f\}, \quad (16)$$

where φ_j is a subsidy (possibly negative) paid unconditionally to any firm that pursues strategy j and φ_b is a subsidy (possibly negative) paid to a firm that diversifies its sourcing options. The optimal supply chain policies offset the wedges that remain (if any) when only consumption subsidies

¹⁷In state B , some final producers source from suppliers in the foreign country at unit cost q_F while others source from the home country at the higher cost q_H . The subsidies needed to ensure that consumers see relative prices equal to relative marginal costs will vary, therefore, with the sourcing of the inputs, despite the fact that all final goods enter demand symmetrically.

¹⁸We henceforth use the notation of total derivatives, $dG(\boldsymbol{\mu})/d\mu_j$, for $j \in \{h, f\}$, to denote the marginal change in the function $G(\cdot)$ with respect to μ_j , taking into account that $\mu_b = 1 - \mu_h - \mu_f$.

are applied.

We have given the social planner three policy instruments to counteract two wedges. Clearly, she has a degree of freedom in her policy choices. The first best can be achieved with a continuum of combinations of subsidies/taxes, including ones that eschew the use of one instrument entirely.

In the appendix, we compute the two wedges, (45) and (46), which yields

$$\tilde{w}_f^o := \tilde{w}_f(\boldsymbol{\mu}^o) = \delta^H \Phi [z(\mu_f^o)] \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \rho + \delta^B \Phi [z^{B,H}(\boldsymbol{\mu}^o)] \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \rho (1 - \rho) \quad (17)$$

and

$$\begin{aligned} \tilde{w}_h^o := \tilde{w}_h(\boldsymbol{\mu}^o) &= \delta^F \Phi [z(\mu_h^o)] \tilde{P}^F(\boldsymbol{\mu}^o)^{1-\varepsilon} \rho + \delta^B \Phi [z^{B,H}(\boldsymbol{\mu}^o)] \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \rho (1 - \rho) \\ &\quad + \delta^B \{ \Phi [z^{B,F}(\boldsymbol{\mu}^o)] - \Phi [z^{B,H}(\boldsymbol{\mu}^o)] \} \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \rho, \end{aligned} \quad (18)$$

where

$$\Phi(z) := \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta - \frac{s(z)}{\sigma(z) - 1}.$$

Assumption 2(i) specifies that $\sigma'(z) > 0$ for all $z \in (0, \bar{z})$ (i.e., Marshall's Second Law of Demand) or else σ is constant for all $z \in (0, \bar{z})$. Taking the latter case first, it is straightforward to see that a constant elasticity of substitution implies $\Phi(z) = 0$ for all $z \in (0, \bar{z})$. This in turn implies $\tilde{w}_f^o = \tilde{w}_h^o = 0$; both wedges are zero in the market equilibrium when (only) optimal consumption subsidies are applied.

In contrast, when the elasticity of substitution rises with the relative price, we show in (25) in the appendix that $\Phi(z) < 0$ for all $z \in (0, \bar{z})$. Then (17) implies that $\tilde{w}_f^o < 0$, because both terms on the right-hand side are negative. As for strategy h , we have that $\tilde{z}^{B,H}(\boldsymbol{\mu}^o) > \tilde{z}^{B,F}(\boldsymbol{\mu}^o)$, because efficient relative prices are equal to relative marginal costs, and $q_H > q_F$. Together with $\Phi'(z) > 0$, (18) implies that $\tilde{w}_h^o < 0$ as well.

The negative wedges imply that, with only consumption subsidies but no subsidies or taxes to influence supply chain formation, firms have excessive incentives for diversification; that is, converting a firm with an exclusive relationship in either country to one that is diversified will reduce aggregate welfare. To interpret this finding, note that firms' investments in supply chains determine the number of differentiated products available in each state of the world, as well as (with MSLD) their markups and prices. Greater diversification is like additional entry in states H and F , because more firms survive the country-specific supply disruptions. At the same time, it generates greater competition in state B to the extent that idiosyncratic shocks ($\rho < 1$) impede product availability in that state.

When a firm chooses its investment strategy and thereby affects the number of varieties available in different states, it conveys two externalities. On the one hand, consumers love variety and they reap consumer surplus from greater availability at a given price. Firms do not take account of this positive effect of their product's availability on consumer surplus when forming their supply chains.

On the other hand, more variety spells less demand and less profits for any particular product at given prices. Firms do not take account of this adverse effect of their product's availability on the profits earned by others. The sign of the wedge at the optimal allocation reflects the relative sizes of these two countervailing externalities.

Now consider, for example, how a change in the number of products n^H available in state H affects the gap between the price index, P^H , and the demand aggregator, A^H . The former fully captures the effect of product availability on consumer surplus whereas the effect on aggregate profits also depends on the latter. Using (5), (6) and (12) we calculate

$$\frac{1}{P^H} \frac{dP^H}{dn^H} - \frac{1}{A^H} \frac{dA^H}{dn^H} = \frac{s(z^H)}{\sigma(z^H) - 1} - \int_{z^H}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta = -\Phi(z^H).$$

When preferences satisfy MSLD, an extra variety in state H reduces the price index for that state by proportionately less than it does the demand aggregator. Thus, the positive consumer-surplus externality from added availability in state H falls short of the negative business-stealing externality. In such circumstances, the private incentives for resilience exceed the social incentives.¹⁹

Similar forces are at work with respect to a firm's choice between strategy h and strategy b . An increase in μ_b at the expense of μ_h means greater availability in state F (when the home suppliers are disrupted) and in state B (when diversified firms stand a better chance of avoiding the disruption from idiosyncratic shocks). However, an increase in μ_b at the expense of μ_h has a further effect on the wedge \tilde{w}_h , as represented by the third term on the right-hand side of (18). When μ_b rises and μ_h falls, the extra products that become available in state B are low-cost goods, whereas when μ_b rises and μ_f falls, the marginal products are high-cost goods. Extra low-cost goods take a greater toll on the profits of competitors than do extra high-cost goods, which adds the additional negative term to the wedge \tilde{w}_h^o .

We turn now to the policies that the planner can introduce, alongside the optimal, state-and-product-contingent consumption subsidies, to implement the first best. Let us begin with the limiting case of symmetric, CES preferences. With $\tilde{w}_f^o = \tilde{w}_h^o = 0$, the optimum can be achieved without any intervention in supply chain formation whatsoever; i.e., $\varphi_h = \varphi_f = \varphi_b = 0$. This is because, with CES preferences, the price index P that (inversely) measures welfare is proportional to the demand aggregator A . Then the external effects of a product's availability on consumers and competitors are equal in magnitude and opposite in sign. Once optimal consumption subsidies are in place to counter the distortion created by markup pricing, there is no need for further government policy to influence the number of products available in any state.

Next consider the special case of symmetric translog preferences. We have seen that, for all HSA preferences that obey MSLD, the government must discourage investments in resilience. But, for the translog case, we can say more. Using $s(z) = -\theta \log z$, we find $\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta = \frac{1}{2} \frac{s(z)}{\sigma(z)-1}$ for all $z \in (0, 1)$. Then using the planner's first-order conditions for the optimal choice of μ_h and μ_f , along

¹⁹This result echoes that in Matsuyama and Uschev (2020a) that there is excessive entry under MSLD in a one-sector model of monopolistic competition and no supply shocks.

with (30)-(32) in the appendix, we find that $\tilde{w}_f^o = \tilde{w}_h^o = -k$; see Appendix Lemma 3. The two wedges coincide for all values of the cost and risk parameters and they are equal in absolute value to the fixed cost of forming a supply relationship. In the translog case, the planner can achieve the first best by combining the optimal consumption subsidies with a tax on diversification; $\varphi_b = -k$, with $\varphi_h = \varphi_f = 0$. Alternatively, she can leave diversified firms to face the private cost of their supply chains ($\varphi_b = 0$), while subsidizing firms that form exclusive supply relationships to the full extent of their investment costs ($\varphi_h = \varphi_f = k$). In either case, she has no reason to favor onshore investments relative to offshore investments.

These surprising results reflect a special property of symmetric translog preferences, namely that the ratio of $\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta$ to $\frac{s(z)}{\sigma(z)-1}$ is independent of price and always equal to one half. Since the consumer surplus loss from removing a variety in some state of the world is proportional to $\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta$, while the loss in operating profits for the firm that does not produce its variety is proportional to $\frac{s(z)}{\sigma(z)-1}$, translog preferences imply that the consumer surplus loss from switching a firm from having two suppliers to one is exactly half of the loss in operating profits. But the wedge \tilde{w}_j^o is equal to the difference in total expected profits per (16), which in turn is equal to the fixed cost of an extra relationship minus the loss in operating profits. Finally, the first-order condition for maximizing $\bar{W}(\boldsymbol{\mu})$ dictates that the marginal loss of consumer surplus from switching a firm from strategy b to strategy j should match the cost of an extra supplier, k .

With more general HSA preferences, the incentives created by optimal supply chain policy are not neutral with respect to the location of firms' input suppliers. The optimal policies favor onshore relationships relative to offshore relationships if $|\tilde{w}_h^o| > |\tilde{w}_f^o|$ and offshore relationships relative to onshore relationships if the ranking of the two wedges is reversed.

To shed further light on the desired national bias in first-best supply chain policy, we examine the limiting case when production costs are nearly the same, $q_H \approx q_F$. Then we find in (50) in the appendix that

$$|\tilde{w}_h^o| - |\tilde{w}_f^o| \propto \Psi[z^H(\boldsymbol{\mu}^o)] - \Psi[z^F(\boldsymbol{\mu}^o)]$$

where $\Psi(z) := \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta / \left[\frac{s(z)}{\sigma(z)-1} \right]$. In the appendix, we also show that $z^H(\boldsymbol{\mu}^o) < z^F(\boldsymbol{\mu}^o)$. It follows that, with nearly equal costs, the government should encourage the less risky investments at home relative to the more risky investments abroad if $\Psi(z)$ is a decreasing function, and the reverse if it is an increasing function; see Lemma 5 in the appendix.

When $q_H \gg q_F$, this simple reasoning does not apply, because the planner's preference for home sourcing on safety grounds is counteracted by her preference for foreign sourcing on cost grounds, so that $\mu_h^o \leq \mu_f^o$. Moreover, with unequal costs, an increase μ_b at the expense of μ_h makes a greater contribution to consumer surplus in state B while taking a greater toll on rivals' profits than does an increase in μ_b at the expense of μ_f ; although both increase product availability in state B by similar amounts, the former spells greater availability of low-cost products, whereas the latter generates greater availability of high-cost products.

We summarize our findings about first-best supply-chain policy when all three strategies are used in

Proposition 1 *Under Assumptions 1 and 2, the unconstrained planner uses consumption subsidies to undo the markup distortion for each good in each state of nature. With symmetric CES preferences, a hands-off policy with respect to supply chain formation ($\varphi_h = \varphi_f = \varphi_b = 0$) achieves the first best. Under MSLD, the planner encourages single sourcing relationships relative to diversification. With symmetric translog preferences, the planner can achieve the first best with a tax on diversification of size k . More generally, if cost differences are small ($q_H \approx q_F$), the planner encourages onshore sourcing relative to offshore sourcing if $\Psi'(z) > 0$ for all $z \in (0, \bar{z})$ and encourages offshore sourcing relative to onshore sourcing if $\Psi'(z) < 0$ for all $z \in (0, \bar{z})$. For larger cost differences, the national bias in optimal sourcing policy hinges not only on the sign of $\Psi'(z)$, but also on the magnitudes of the cross-country cost and risk differences.*

4 The Constrained Social Optimum

In the previous section, we characterized the first-best allocation of resources when firms in a monopolistically competitive industry face potential supply chain disruptions. We noted that attainment of the first best requires not only that government use policies to offset distortions in firms' incentives for forming supply relationships, but also a policy to counter the distortion created by monopoly pricing of differentiated products alongside the competitive pricing of goods elsewhere in the economy. As we discussed, the requisite consumption subsidies are rarely implemented in practice. In our context, not only would they need to be adjusted in response to realized disruptions, but they would also need to vary across otherwise symmetric products that differ only in the sourcing of their critical inputs. Nonetheless, by allowing for optimal consumption subsidies, we were able to lay bare the wedges between private and social incentives for supply diversification and for onshoring versus offshoring.

In this section, we consider the second-best problem that confronts a welfare-maximizing government that lacks the ability to implement state-contingent and sourcing-contingent consumption subsidies. We grant the policy maker only taxes or subsidies to encourage or discourage supply chain resilience and to influence whether sourcing partnerships are formed at home or abroad. As with the unconstrained optimum, the constrained social optimum can be achieved by a continuum of combinations of subsidies or taxes for the formation of home relationships, foreign relationships, and multiple relationships and, indeed, any two of these three instruments will suffice.

Let us begin with the limiting case in which the home and foreign countries are symmetric in terms of both input costs and disruption risks; i.e., $q_H \approx q_F$ and $\gamma_H \approx \gamma_F$. In Figure 2, we illustrate a *laissez-faire* equilibrium at E for a typical case in which all three strategies are employed by positive measures of firms. In such circumstances, we can use the equilibrium relationship $\mu_b = 1 - \mu_h - \mu_f$ to project the three-dimensional space (μ_f, μ_h, μ_b) onto two dimensions. Accordingly,

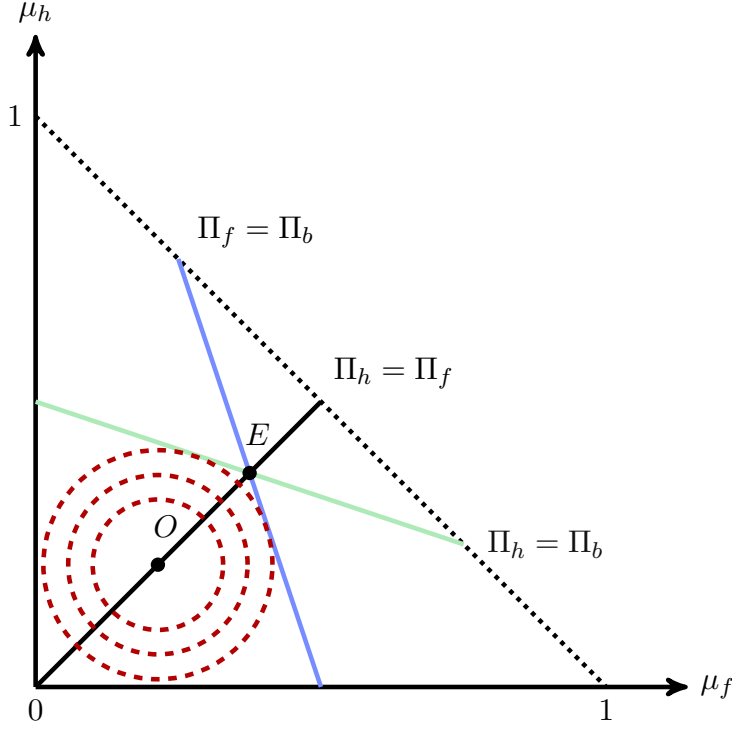


Figure 2: Equilibrium and Constrained Optimum for the Symmetric Case

the figure shows μ_h and μ_f on the vertical and horizontal axes, and the equilibrium falls inside the unit simplex.

The curve labeled $\Pi_h = \Pi_f$ represents combinations of μ_h and μ_f such that a strategy of forming a single supply relationship at home yields the same expected profit as that of forming a single supply relationship abroad. With similar production costs, the profits from strategies h and f are the same in state B . Hence, when choosing between these two strategies, firms compare realized profits in states H and F . Profits in state H are declining in the number of firms $n^H(\boldsymbol{\mu}) = \rho(1 - \mu_f)$ that are active in that state. Similarly, profits in state F are declining in $n^F(\boldsymbol{\mu}) = \rho(1 - \mu_h)$. It follows that firms will be indifferent between h and f if only if the expected competition in the two states is the same, i.e., $\mu_h = \mu_f$. Thus, we represent the $\Pi_h = \Pi_f$ curve by a 45° ray from the origin.

The downward sloping curve labelled $\Pi_h = \Pi_b$ shows combinations of μ_h and μ_f for which investing in a single relationship at home yields the same expected profits as a strategy of diversification. The downward slope of the curve can be understood as follows. Starting from a point on the curve suppose we raise μ_h and reduce μ_b so that μ_f remains constant. This does not affect the number of firms n^H active in state H . But it decreases the number of firms active in state F and also in state B , since $n^B(\boldsymbol{\mu}) = \rho + \rho(1 - \rho)\mu_b$. Therefore, π^F and π^B both rise, leaving a (positive) gap between Π_b and Π_h .²⁰ Now consider a fall in μ_f accompanied by an offsetting rise

²⁰The effect on expected profits of a diversified firm relative to a home-only firm conditional on state B are equal

in μ_b that leaves μ_h unchanged. This change in composition has no effect on the number of firms active in state F , but increases the number that are active in state H . However, the more intense competition in state H does not affect the *relative* attractiveness of strategy h versus b , because each of these strategies yields operating profits π^H with probability ρ in that state. Meanwhile, competition also intensifies in state B . With more firms active, π^B falls, which depresses expected profits more for diversified firm than for firms that have only a home supplier, because the diversified firms are more likely to survive. Thus, a decrease in μ_f offset by an increase in μ_b reduces Π_b relative to Π_h . It follows that a decrease in μ_f is needed to offset the effects of an increase in μ_h if strategies h and b are to remain equally profitable. We note further that the $\Pi_h = \Pi_b$ curve must have a slope less than one in absolute value.²¹ By an analogous argument, the curve $\Pi_f = \Pi_b$ also slopes downward in the figure, with a slope greater than one in absolute value.

In equilibrium, if all strategies are used, all must yield equal profits. So, the equilibrium is represented by the point E in Figure 2. The figure also illustrates a constrained optimum at O . The constrained optimum maximizes W over the choice of $\boldsymbol{\mu}$ in the presence of monopoly pricing of differentiated products. In the appendix, we show that the first-order conditions for a constrained maximum are satisfied when $\mu_h = \mu_f$.²² The figure depicts some iso-welfare loci for successively lower levels of expected welfare as we move away from O . These curves are symmetric about the 45-degree line, thanks to the symmetry across countries.

It should be clear that, if O falls on the 45° line, the constrained optimum can be achieved with a tax or subsidy on diversification alone, with $\varphi_f = \varphi_h = 0$. Such a policy shifts the equilibrium along the $\Pi_h = \Pi_f$ curve and thereby preserves the equality between μ_h and μ_f . What remains to be addressed is whether the government should encourage diversification with a subsidy for firms that form multiple relationships ($\varphi_b > 0$) or whether it should discourage diversification with a tax ($\varphi_b < 0$) on such firms. This amounts to the same question as to whether point O lies to the southwest of E along $\Pi_h = \Pi_f$ or whether it lies instead to the northeast of E .

We can answer these questions formally using methods similar to the ones we applied in Section 3. We begin with the planner's objective in (11). The wedge between social and private incentives for diversification is given by

$$w_j^* := \Pi_j(\boldsymbol{\mu}^*) - \Pi_b(\boldsymbol{\mu}^*) - \frac{dW(\boldsymbol{\mu}^*)}{d\mu_j}, \quad j \in \{h, f\},$$

and opposite for a given increase in μ_h and comparable decrease in μ_f . But the increase in μ_h (and accompanying decrease in μ_b) gives an added boost to the relative profitability of diversification, because it raises the expected profits for a b firm if state F arises.

²¹The effect on expected profits of a diversified firm relative to a home-only firm conditional on state B are equal and opposite for a given increase in μ_h and comparable decrease in μ_f . But the increase in μ_h (and accompanying decrease in μ_b) gives an added boost to the relative profitability of diversification, because it raises the expected profits for a b firm if state F arises.

²²This statement is valid for all HSA preferences. In the appendix, we also show that the welfare function $W(\boldsymbol{\mu})$ is globally concave when X takes a CES form and that the constrained optimum must have $\mu_h = \mu_f$ when preferences take the symmetric translog form. Evaluating the second-order conditions for more general HSA preferences is challenging, but it seems compelling that the planner would want equal numbers of firms with single relationships at home and abroad.

where $\boldsymbol{\mu}^*$ represents the allocation in the constrained optimum and recall that $dG(\boldsymbol{\mu})/d\mu_j$ denotes the variation in any function $G(\boldsymbol{\mu})$ for $d\mu_j = -d\mu_b > 0$. Using the first-order condition for the second-best allocation, this wedge is given by

$$w_j^* = - \sum_{i=h,f,b} \mu_i \frac{d\Pi_i(\boldsymbol{\mu}^*)}{d\mu_j} - \frac{1}{\varepsilon - 1} \sum_{J=H,F,B} \delta^J \frac{d \left[P^J(\boldsymbol{\mu}^*)^{1-\varepsilon} \right]}{d\mu_j}, \quad j \in \{h, f\}. \quad (19)$$

The first term on the right-hand side of (19) represents the business-stealing externality; i.e., the change in other firms' profits that results from shifting a marginal firm from diversified sourcing to sole sourcing in country j . The second term represents the consumer-surplus externality; i.e., the change in consumer-surplus that results from reduced product availability and higher prices in the three states. The difference from the analogous expressions in Section 3 reflects the fact that the constrained policy maker needs to take account not only of the *direct* effects on profits and consumer surplus of changing the numbers of firms in each state (holding prices constant), but also the *indirect* effects on profits and consumer surplus that come from marginal adjustments in the markups. The unconstrained planner can ignore these latter effects when deciding $\boldsymbol{\mu}^o$, because the choice of optimal consumption subsidies ensures that the induced changes in markups have a negligible effect on aggregate utility.

In the appendix, we provide a general formula for the wedge w_j^* for an arbitrary share function $s(z)$ that satisfies Assumptions 1 and 2. Then we turn to the symmetric case depicted in Figure 2, where $w_h^* = w_f^* = w^*$. Point E lies above point O whenever $w^* > 0$ and below point O whenever $w^* < 0$.

The results for our two special cases of HSA preferences are instructive. First, with *symmetric CES preferences*, we find that $w^* > 0$ and thus $\varphi_b^* > 0$ for all $\sigma > 1$.²³ Recall that with optimal consumption subsidies in place, the optimal policy has $\varphi_b^o = 0$, because the extra consumer surplus generated by adding firms in a given state exactly matches the loss in aggregate profits. Now, with consumption subsidies unavailable to the policy maker, the monopoly pricing of differentiated products generates too little consumption of these goods relative to the numeraire good in the *laissez-faire* equilibrium. A subsidy for diversification increases the number of available products in every state, which reduces P^J for all $J \in \{H, F, B\}$, even though prices of marketed products do not change. The fall in the price index in state J stimulates consumption of differentiated products in that state, thereby mitigating the consumption distortion.

Second, with *symmetric translog preferences*, we show that $w^* > 0$ if $\varepsilon > \frac{\theta\rho(2-\rho)[1+\theta\rho(2-\rho)]}{1+3\theta\rho(2-\rho)}$ and $w^* < 0$ if $\varepsilon < \frac{\theta\rho(2+\theta\rho)}{2(2+3\theta\rho)}$; see Lemma 7. Recall that a tax on diversification is needed to align social and private incentives for supply chain formation for any HSA preferences other than CES when a consumption subsidy is available to correct the distortion otherwise generated by markup pricing. In the absence of consumption subsidies, the tendency for firms to overinvest in resilience continues to figure in the policy maker's calculus, because the business-stealing externality is large relative

²³Equivalently, the planner can set $\varphi_b^* = 0$ and $\varphi_h^* = \varphi_f^* < 0$

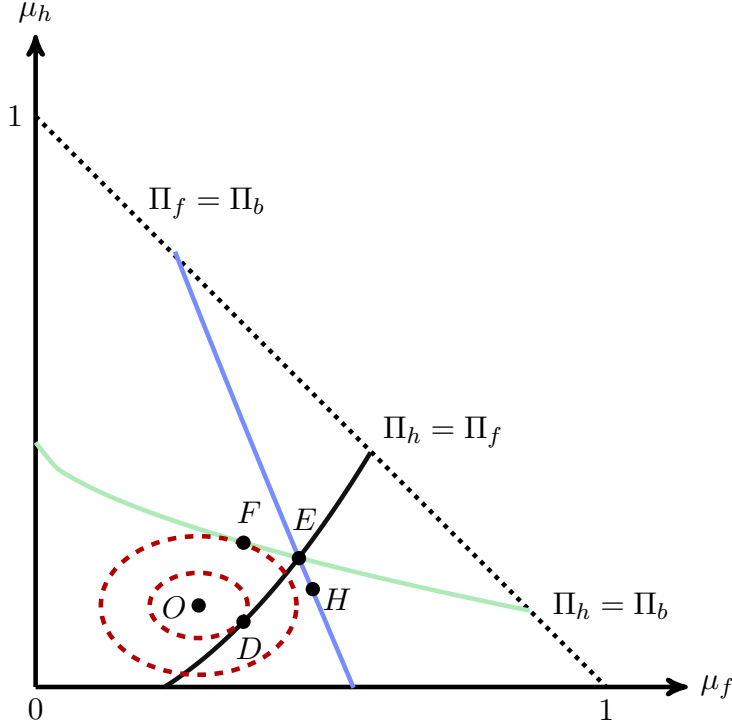


Figure 3: Equilibrium and Constrained Optimum for the Asymmetric Case

to the consumer-surplus externality. However, the distortion arising from monopoly pricing points in the opposite direction; there is too little consumption of differentiated products relative to the numeraire good and a subsidy for diversification would boost consumption of these goods. When demand for differentiated goods is highly elastic, the distortion from monopoly pricing looms large and the planner's imperative to encourage consumption of these goods outweighs her concern about firms' excessive investments in resilience, much as with CES preferences. In contrast, when demand for differentiated products is not so elastic, the welfare effects of the consumption distortion are muted and the planner acts to dampen firms' excessive incentive to be present in the market.

Let us return now to the case in which input costs are lower abroad than at home ($q_H > q_F$) but foreign sourcing entails greater risk of disruption than home sourcing ($\gamma_H > \gamma_F$). Figure 3 depicts the *laissez-faire* equilibrium and the constrained optimum in such a setting for general HSA preferences. Again we consider fixed costs of sourcing relationships in the range that a positive measure of firms chooses each of the available investment strategies.

We observe first that, for general HSA preferences, the constrained optimum, O , need not fall on any of the three equiprofitability curves. This means that, generically, the government cannot achieve the constrained optimum with a single policy instrument. For the case illustrated in Figure 3, a subsidy for diversification improves welfare relative to E , but since such a policy preserves $\Pi_h = \Pi_f$, such a policy can achieve at best the utility associated with the iso-welfare curve through point D . A tax to discourage sourcing abroad ($\varphi_f < 0$) shifts the equilibrium to the left along the

$\Pi_h = \Pi_b$ curve, but at best can achieve the utility associated with the iso-welfare curve through point F . Finally, a tax on onshore relationships with a single partner ($\varphi_h < 0$) can be used to achieve point H . For the scenario depicted in the figure, the constrained optimum could be achieved with a combination of a subsidy for diversification and a tax on sole-sourcing offshore or with a subsidy to diversification and a subsidy for sole-sourcing at home.

Although the constrained optimum can be characterized for particular preferences and parameters, in general the wedges w_h^* and w_f^* that dictate the second-best policy combinations can take any sign and a range of relative magnitudes. The reason for this reflects the complexity of the planner's constrained maximization problem. While the planner faces a general tradeoff between alleviating the markup distortion by supporting greater resilience and mitigating the business-stealing externality, the size of this tradeoff will vary across states of the world and the planner cannot separately address the tradeoff state by state. For example, a policy that encourages greater diversification at the expense of sole-sourcing offshore generates an increase in the number of products available both in state H and in state B . As a result, the optimal policy is dictated by some weighted average of the tradeoff between consumption distortion and business stealing externality in each state of the world, and this depends on the exact form of preferences, the various preference parameters, and the sizes of the cross-country differences in costs and riskiness.

In the next section, we resort to numerical methods to explore some of these tradeoffs. Before that, we return briefly to the special case of symmetric CES preferences, for which a strong characterization of the second-best policies is possible even with asymmetric costs and risks. With CES preferences, the price index plays a dual role as both welfare metric and demand aggregator. We show in the appendix that this exceptional feature of the CES implies that the constrained optimum is characterized by $\Pi_h = \Pi_f$, much like the *laissez-faire* equilibrium. That is, the planner has no reason to tilt supplier relationships toward one location or the other. This means that the second best can be achieved with a single policy instrument, namely a tax or subsidy for diversification. However, as we also show in the appendix, point O always lies *below* point E on the $\Pi_h = \Pi_f$ curve, so, with CES preferences, it is always desirable for the government to promote resiliency with a subsidy to strategy b for all values of the cost and risk parameters. The explanation is the same as in the symmetric case; with CES preferences, the consumer-surplus externality and the business-stealing externality exactly offset one another *in every state of the world*. What remains are the distortions that result from the fixed and positive markup of consumer prices over marginal costs. The constrained policy maker who cannot eliminate the consumption distortions directly can instead partially alleviate the distortion by promoting greater product availability in all states of the world.

We summarize our analytical findings about second-best supply-chain policy in

Proposition 2 *Suppose that consumption subsidies are infeasible. If consumers have symmetric CES preferences, the planner can achieve a constrained optimum with a single policy instrument, namely a subsidy for diversification ($\varphi_b > 0$). If consumers have symmetric translog preferences and the input costs and disruption risks in the two countries are symmetric, the constrained optimum*

can again be achieved with a single policy, which must be a tax on diversification if $\varepsilon < \frac{\theta\rho(2+\theta\rho)}{2(2+3\theta\rho)}$ and a subsidy for diversification if $\varepsilon > \frac{\theta\rho(2-\rho)[1+\theta\rho(2-\rho)]}{1+3\theta\rho(2-\rho)}$. In other circumstances, two policy instruments are generally needed to alter both the incentives for diversification and the incentives for sourcing at home versus abroad.

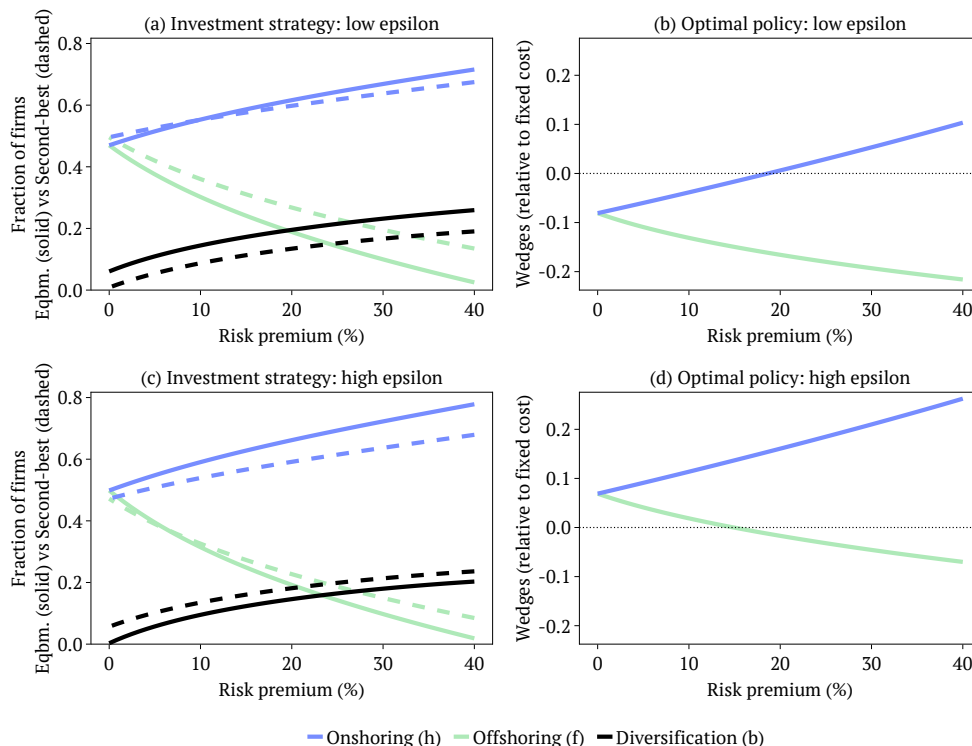
5 Numerical Exploration of the Constrained Optimum

When monopolistically-competitive firms form their supply chains with an eye to potential disruptions, the market equilibrium features several sources of inefficiency. The consumer-surplus externality associated with product availability suggests underinvestment in resilience, whereas the business-stealing externality implies just the opposite. Meanwhile, monopoly pricing generates insufficient consumption of differentiated products relative to the numeraire good in realistic situations when fiscal policies cannot be used to align relative prices with relative marginal costs. We have been able to characterize the policy imperatives that these distortions create under CES preferences and, with more general HSA preferences, when the home and foreign suppliers are similar with respect to costs and risks. Armed with our understanding of the nature of the distortions, we turn now to numerical methods to explore the constrained optimal policies in situations when costs and risks differ in the two countries. To this end, we henceforth assume that preferences take the symmetric translog form.

Figure 4 depicts the constrained optimal fractions of firms (on the left) and the policy wedges at the second-best allocation (on the right) for two different values of ε , the elasticity of demand for differentiated products. The figure is drawn for the case when production costs are similar in the two countries ($q_H = q_F$), but we show in the appendix (see Figures 6 and 7) that qualitatively similar patterns emerge when costs differ. Figure 4 illustrates the comparative statics of the equilibrium, constrained optimum and optimal supply-chain policies with respect to variation in the cross-country risk differential.

In panels (a) and (b), we see the outcomes for a relatively low value of ε , namely $\varepsilon = 1.2$. Panel (a) shows the fraction of firms that choose each of the investment strategies in the laissez-faire equilibrium (solid curves) and in the constrained optimum (dashed curves). When $\gamma_H = \gamma_F$, at the left side of the panel, the market equilibrium features excess investment in resilience ($\mu_b > \mu_b^*$) and insufficient investment in exclusive supply relationships ($\mu_h^* = \mu_f^* = \mu^* > \mu$). These numerical outcomes mirror the theoretical results from Section 4. They reflect the fact that, under MSLD, the business-stealing effect dominates the consumer surplus effect. Moreover, with ε relatively small, the consumption distortion caused by markup pricing is not too severe. In panel (b), we see that $w_h^* = w_f^* = w^* < 0$, so the constrained optimum can be achieved either with a tax on firms that diversify, or with equal subsidies to firms that invest in exclusive supply relationships either at home or abroad. As we increase the risk of disruption in F —so that the “safety premium” in the home country rises—both the competitive equilibrium and the constrained optimum are characterized by greater fractions of diversified firms and greater fractions of firms that form relationships only

Figure 4: Second-Best Policies: Risk Differences Across Locations



Note: Baseline simulation has $\gamma_H = \gamma_F = 0.9$, $q_H = q_F = 0.1$, $\theta = 8.0$, and $\rho = 0.7$. Low and high epsilon correspond to $\varepsilon = 1.2$ and $\varepsilon = 1.7$ respectively. Fixed cost chosen so that $\min(\mu_b^*, \mu_b^o) \approx 0$ in the baseline symmetric simulation. This yields $k = 0.13$ for $\varepsilon = 1.2$ and $k = 0.37$ for $\varepsilon = 1.7$. The risk premium is computed as $-(\gamma_F - \gamma_H)/\gamma_H$, where we keep γ_H constant at its baseline value.

onshore. These findings are intuitive, but what is less obvious is what happens to the wedges between social and private incentives. In panel (b) we see that w_h^* rises while w_f^* falls. This implies, for example, that second-best subsidies for exclusive offshore relationships grow (φ_f^*) while subsidies for sourcing relationships at home (φ_h^*) shrink, if the planner eschews taxes or subsidies on diversification ($\varphi_b^* = 0$).

How do we understand this finding? In panel (a), we see that the fraction of firms with sourcing relationships exclusively in the home country rises above the fraction with sourcing relationships exclusively offshore. The increase in product diversity and in competition in state H relative to state F generates a decline in the price index P^H relative to P^F . But the monopoly distortion is more severe when the price index is high, so the consumption shortfall is greater in state F than in state H . The planner wishes to combat the higher price index in state F with a policy that tilts sourcing toward the foreign country.

As the foreign country becomes even riskier, the planner continues to discourage diversification; we continue to find the second-best fraction of diversified firms, μ_b^* , below the free-market level. But the social cost of the market's misallocation between home sourcing and foreign sourcing also

grows, and so the gap between the two wedges w_h^* and w_f^* widens. At some risk differential close to 20% in the figure, the planner's desire to shift the location of exclusive sourcing from the home country to the foreign country implies a second-best *tax* on onshore relationships, combined with an even larger subsidy for investing in a single relationship abroad.²⁴

The situation is similar for larger values of ε , such as depicted in panels (c) and (d) of Figure 4, except in one important respect. With a more elastic demand for differentiated products, the misallocation generated by markup pricing weighs more heavily in the planner's calculus compared to the net effect of the business-stealing and consumer-surplus externalities. The optimal policy in the symmetric environment entails a net subsidy to diversification, which can be achieved with $\varphi_b > 0 = \varphi_h = \varphi_f$ or with $\varphi_h = \varphi_f < 0 = \varphi_b$. As the risk differential grows, the planner once again tilts policy in favor of exclusive sourcing relationships abroad, to offset the increasingly deleterious effects of under-consumption of differentiated products when foreign supply is disrupted. For a sufficiently great probability of supply disruption in the foreign country, the planner subsidizes strategy f , while still ensuring that the net effect of supply chain policy is to induce more diversification and greater resilience.

Notice too the scale of the optimal subsidies. Recall from Section 3 that, when able to implement the optimal, state-and-product-contingent consumption subsidies, the planner taxes diversification (or subsidizes the two strategies involving exclusive relationships) at 100% of the fixed cost k , regardless of the configuration of cost and risk parameters.²⁵ In the second best described here, the impetus to tax diversification in order to dampen incentives for business stealing is offset by an urge to subsidize diversification to stimulate consumption of differentiated goods. The offsetting forces result in second-best policies that are an order of magnitude smaller than in the first best.

Figure 5 depicts the comparative statics with respect to foreign production costs, holding risk-iness in the two locations constant (and, in this figure, equal to one another).²⁶ The symmetric equilibrium again requires a second-best tax on diversification when ε is small (top panels) and a subsidy when ε is larger (bottom panels). A fall in the cost of producing inputs abroad, which expands the cost discount in the offshore location, reduces the price index in state F relative to that in state H .²⁷ Thus, the social benefit from promoting consumption in state H comes to exceed that in state F . In panel (b), the planner alters the composition of exclusive supply relationships by offering a larger subsidy for onshore sourcing than for offshore sourcing (or, equivalently, a subsidy for onshoring combined with a tax on diversification). For a high enough cost discount, the wedge for offshore relationships actually turns positive. In panel (c), with more elastic demand, the planner encourages resilience at the expense of exclusive relationships at home and abroad.

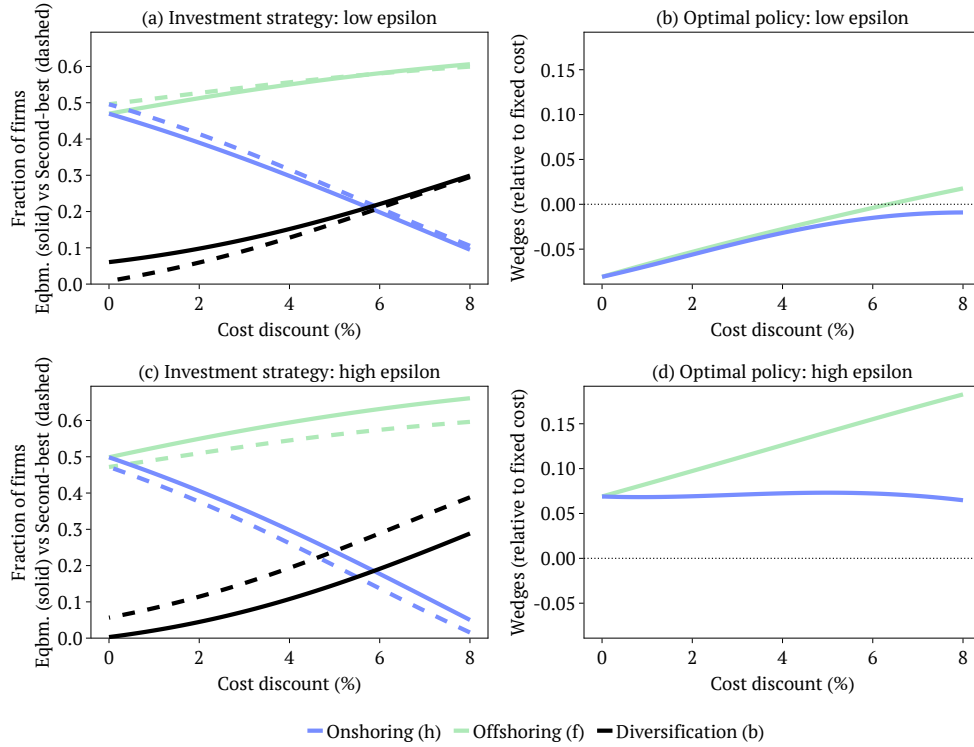
²⁴Alternatively, the planner can achieve the same allocation with a subsidy for diversification and an even larger subsidy for offshore relationships (and $\varphi_h = 0$), so that μ_f grows at the expense of both μ_h and μ_b .

²⁵This statement applies to situations, as here, with symmetric translog preferences

²⁶The parameters used for this figure are the same as for Figure 4, so the baseline (symmetric) outcome is the same at the left-most point in both figures.

²⁷In this case there are two reasons: more firms choose strategy f than strategy h and hence the market is more competitive in state F than in state H ; and products containing inputs produced in F bear a lower cost than those produced in H .

Figure 5: Second-Best Policies: Cost Differences Across Locations



Note: Baseline simulation has $\gamma_H = \gamma_F = 0.9$, $q_H = q_F = 0.1$, $\theta = 8.0$, and $\rho = 0.7$. Low and high epsilon correspond to $\varepsilon = 1.2$ and $\varepsilon = 1.7$ respectively. Fixed cost chosen so that $\min(\mu_b^*, \mu_b^o) \approx 0$ in the baseline symmetric simulation. This yields $k = 0.13$ for $\varepsilon = 1.2$ and $k = 0.37$ for $\varepsilon = 1.7$. The cost discount is computed as $-(q_F - q_H)/q_H$, where we keep q_H constant at its baseline value.

As seen in panel (d), the taxes on single relationships that are used to encourage diversification diverge; onshore relationships face a lower tax than their offshore counterparts (or else the planner can subsidize both diversification and onshoring). This policy combination reflects the fact that consumption distortion is more harmful in state H than in state F .

When both cost and risk parameters differ in the two possible locations for producing inputs, the ranking of the price index in states H and F is less clear-cut. Greater risk of supply disruption in the foreign country discourages private investment there, contributing to a relatively higher price index in state F . But lower production costs offshore raises the relative attractiveness of strategy f compared to strategy h , and it also has a direct effect on comparative prices in the two states reflecting the relatively lower foreign unit cost. The relative size of the wedges, w_h^* versus w_f^* , and thus the net effect on the incentives for exclusive offshoring versus exclusive onshoring, hinges on the relative strength of these forces.

6 Conclusion

Global supply chain disruptions are increasingly salient and often costly. Many commentators have been quick to conclude that governments ought to be doing something to promote greater market resilience. But the welfare-theoretic calculus around government intervention is rather subtle. Private actors have a clear self-interest in taking measures to avoid disruptions to their production processes. Only when the private incentives for resilience fall short of the social benefits will government encouragement be warranted. Pointing in that direction is the observation that consumers capture part of the surplus created by the ongoing availability of firms' products. But firms also have an incentive to be in a position to reap extra profits when their rivals are suffering. The temptation for "business stealing" suggests that excess resilience is also a possible market outcome.

Surprisingly little research has addressed the desirability of government policy to promote resilience or to encourage sourcing from safer locations. In this paper, we have taken a first step. We have proposed a simple framework in which the supply of any product requires the availability of a critical input. Idiosyncratic and aggregate shocks can disrupt firms' relationships with their suppliers. Firms face the choice of where to develop a relationship and whether to protect their operation with backup sources of supply. We study the simplest case of two potential supply sources, one at home and one abroad and focus on a situation where domestic sourcing is costlier than sourcing abroad, but also less risky.

Since consumer gains from product availability reflect their preferences, the form of demand plays a critical role in the policy calculus. The CES demand system is popular and tractable for analysis such as ours. But it also introduces restrictions that color the findings. We allow for a CES utility function, but also for a broader class of preferences that Matsuyama and Ushchev (2017,2020a) have developed and termed Homothetic with a Single Aggregator. The more general preferences admit non-constant markups and, in particular, application of Marshall's Second Law of Demand.

Our analysis yields several broad lessons. First, the government generally needs at least two supply-chain policies to achieve efficient sourcing (first or second best). One instrument regulates the margin between sourcing from one location or two. The other guides the choice between sourcing at home and abroad. For example, the government might subsidize or tax supply-chain diversification, while subsidizing or taxing firms that source only at home. Or it might subsidize or tax diversification, while subsidizing or taxing offshoring.

When preferences take the CES form, the first best can be achieved simply with a state-independent consumption subsidy and with no interference in supply chain organization. The second best requires a subsidy to diversification but no bias for home versus foreign sourcing. But with more general forms of HSA preferences that obey Marshall's Second Law of Demand, the planner requires state-and-product-specific consumption subsidies to achieve the first best, along with a tax on firms that diversify, and a policy that tilts sourcing to one country or the other depending on the relative sizes of the consumer-surplus externality and the business-stealing

externality. In the second best, the optimal policies are qualitatively similar to the ones that achieve the first best if the elasticity of demand for differentiated products is small, but a large demand elasticity tilts the policy toward smaller taxes or even subsidies for diversification.

Needless to say, there are many ways that our analysis could be enriched. For example, we could introduce a richer technology with potential substitution between manufactured inputs and primary factors of production. We could entertain more complex supply chains, with multiple inputs and with a sequencing of them such that some inputs enter the production process upstream from others. We could allow for dynamics, which would render inventories an additional tool for firms to invest in resilience and give governments additional policy instruments such as stockpiling supplies or allowing accelerated depreciation of inventory costs. We could introduce political-economy considerations that might drive a wedge between the parameters that capture the risk aversion of managers versus that of policy makers. We see all of these potential extensions as worthwhile and germane to the ultimate policy assessment. We believe that our simpler setting suggests a way to pose the question and that our analysis provides a “proof of concept.”

References

- [1] Arad, Ruth W. and Arye L. Hillman, 1979. “Embargo Threat, Learning and Departure from Comparative Advantage,” *Journal of International Economics* 9, 265-275.
- [2] Baqaee, David and Emmanuel Farhi, 2020. “Entry vs. Rents: Aggregation with Economies of Scale,” NBER Working Paper No. 27140.
- [3] Baldwin, Richard and Rebecca Freeman, 2022. “Risks and Global Supply Chains: What We Know and What We Need to Know,” *Annual Review of Economics* 14, 153-180.
- [4] Bergström, Clas, Loury, Glenn C. and Mats Persson, 1985. “Embargo Threats and the Management of Emergency Reserves,” *Journal of Political Economy* 93(1), 26-42.
- [5] Bhagwati, Jagdish N. and T.N. Srinivasan, 1976. “Optimal Trade Policy and Compensation under Endogenous Uncertainty: The Phenomenon of Market Disruption,” *Journal of International Economics* 6, 317-336.
- [6] Bilbiie, Florin O., Ghironi, Fabio, and Mark J. Melitz, 2012. “Endogenous Entry, Product Variety, and Business Cycles” *Journal of Political Economy* 120(4), 304-345.
- [7] Campolmi, Alessia, Fadinger, Harald, and Chiata Forlati, 2021. “Trade and Domestic Policies in Models with Monopolistic Competition,” http://fadinger.vwl.uni-mannheim.de/Research_files/CFF_20210722.pdf.
- [8] Cheng, Leonard K., 1989. “Intermittent Trade Disruptions and Optimal Production,” *International Economic Review* 30(4), 753-74.
- [9] Dhingra, Swati and John Morrow, 2019. “Monopolistic Competition and Optimum Product Diversity under Firm Heterogeneity,” *Journal of Political Economy* 127(1), 196-232.
- [10] Diewert, W.E., 1974. “Applications of Duality Theory,” in M. Intriligator and D. Kendrick (eds.), *Frontiers of Quantitative Economics, vol. II*, Amsterdam: North Holland.
- [11] Dixit, Avinash K. and Joseph E. Stiglitz, 1977. “Monopolistic Competition and Optimum Product Diversity,” *American Economic Review* 67(3): 297-308.
- [12] Elliot, Matthew, Golub, Benjamin and Matthew V. Leduc, 2022. “Supply Network Formation and Fragility,” *American Economic Review* 112(8): 2701-47.
- [13] Fajgelbaum, Pablo, Goldberg, Pinelopi, Kennedy, Patrick and Amit Khandelwal, 2020. “The Return to Protectionism,” *Quarterly Journal of Economics* 135(1): 1-55.
- [14] Feenstra, Robert C., 2003. “A Homothetic Utility Function for Monopolistic Competition Models, without Constant Price Elasticity,” *Economic Letters* 78(1): 79-86.

- [15] Iakovou, Eleftherios and Chelsea C. White III, 2020. “How to Build More Secure, Resilient, Next-Gen U.S. Supply Chains,” *TechStream*, Brookings Institution.
- [16] Matsuyama, Kiminori, 2019. “Supplement to ‘Engel’s Law in the Global Economy: Demand-Induced Patterns of Structural Change, Innovation, and Trade’,” *Econometrica Supplementary Material*, *Econometrica* 87(2), 497-528.
- [17] Matsuyama, Kiminori and Philip Ushchev, 2017. “Beyond CES: Three Alternative Classes of Flexible Homothetic Demand Systems,” CEPR Discussion Paper No. 12210.
- [18] Matsuyama, Kiminori and Philip Ushchev, 2020a. “When Does Procompetitive Entry Imply Excessive Entry,” CEPR Discussion Paper No. 14991.
- [19] Matsuyama, Kiminori and Philip Ushchev, 2020b. “Constant Pass Through,” CEPR Discussion Paper No. 15475.
- [20] Matsuyama, Kiminori and Philip Ushchev, 2022. “Destabilizing Effects of Market Size in the Dynamics of Innovation,” *Journal of Economic Theory* 200: 105415.
- [21] Mayer, Wolfgang, 1977. “The National Defense Tariff Argument Reconsidered,” *Journal of International Economics* 7, 363-77.
- [22] McKinsey Global Institute, 2020. *Risk, Resilience and Rebalancing in Global Value Chains*.
- [23] Mrázová, Monika and J. Peter Neary, 2017. “Not So Demanding: Demand Structure and Firm Behavior,” *American Economic Review* 107(12): 3835-74.
- [24] Shih, Willy C., 2020a. “Global Supply Chains in a Post-Pandemic World,” *Harvard Business Review* 98(5): 82-9.
- [25] Shih, Willy C., 2020b. “Is it Time to Rethink Globalized Supply Chains,” *MIT Sloan Management Review* 61(4): 16-18.
- [26] Zhelobodko, Evgeny. Kokovin, Sergey, Parenti, Mathieu and Jacques-François Thisse, 2012. “Monopolistic Competition: Beyond the Elasticity of Substitution,” *Econometrica* 80(6): 2765-2784.

Online Appendix for

Supply Chain Resilience:

Should Governments Promote International Diversification or Reshoring?

By

Gene M. Grossman Elhanan Helpman Hugo Lhuillier

We provide in this appendix derivations of expressions discussed in the main text, as well as proofs of arguments that are not shown there. The appendix is organized according to sections in the body of the paper in order to make it easy for the reader to find these items.

Section 2

Section 2.4

We begin by deriving expected profits $\Pi_j := \Pi_j(\boldsymbol{\mu})$, $j \in \{f, h, b\}$, where $\boldsymbol{\mu} := (\mu_h, \mu_f, \mu_b)$. To this end, recall the profit function (7),

$$\pi^{J,K}(\omega) = \frac{s[p(\omega)/A]}{\sigma[p(\omega)/A]} (P^J)^{1-\varepsilon},$$

for $J \in \{H, J, B\}$ the state of the world and $K \in \{H, F\}$ the country from which the input is supplied from. Given a state J , all firms sourcing from the same location choose the same prices. In states H and F , only sourcing from one country is feasible, and we use $\pi^J := \pi^{J,J}$ to denote the realized profits in state J for firms that have an active supply chain in country J .

First consider a state $J \in \{H, F\}$ in which supply chains from one country are disrupted but not so in the other country. In such a state, only firms that adopted a strategy of investing only in country J and those that invested in both countries might be able to produce, provided that their bilateral relations do not suffer an idiosyncratic shock. Each such firm pays q_J for its input. In this case, the market clearing condition (4) becomes

$$1 \equiv n^J(\boldsymbol{\mu}) s[z^J(\boldsymbol{\mu})], \quad J \in \{H, F\}, \quad (20)$$

where

$$n^J(\boldsymbol{\mu}) = (\mu_j + \mu_b) \rho$$

and $z^J = p^J/A^J$. These equations yield relative prices z^J in state $J \in \{H, F\}$ as functions of $\boldsymbol{\mu}$, denoted $z^J(\boldsymbol{\mu})$.

Next note that, in state $J \in \{H, F\}$, the price index (5) can be expressed as

$$\log P^J = C_P + \log \frac{p^J}{z^J} - n^J \int_{z^J}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta,$$

where from (6),

$$p^J = \frac{\sigma(z^J)}{\sigma(z^J) - 1} q_J.$$

Using the function $z^J(\boldsymbol{\mu})$ and (20), we can express the price index P^J as a function of $z^J(\boldsymbol{\mu})$,

$$\log P^J [z^J(\boldsymbol{\mu})] := C_P + \log \frac{\sigma[z^J(\boldsymbol{\mu})]}{\sigma[z^J(\boldsymbol{\mu})] - 1} + \log \frac{q_J}{z^J(\boldsymbol{\mu})} - \frac{1}{s[z^J(\boldsymbol{\mu})]} \int_{z^J(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta, \quad J \in \{H, F\}. \quad (21)$$

This function, together with (7) and $z^J(\boldsymbol{\mu})$, can be used to compute the profits of an active firm in state J , which are

$$\pi^J [z^J(\boldsymbol{\mu})] := \frac{s[z^J(\boldsymbol{\mu})]}{\sigma[z^J(\boldsymbol{\mu})]} P^J [z^J(\boldsymbol{\mu})]^{1-\varepsilon}, \quad J \in \{H, F\}. \quad (22)$$

The functions $P^J(z)$ and $\pi^J(z)$, defined in (21) and (22), are decreasing in z . To see this, differentiate $\log P^J(z)$ with respect to z , which yields²⁸

$$\frac{1}{P^J(z)} \frac{dP^J(z)}{dz} = -\frac{\sigma'(z)}{\sigma(z)[\sigma(z) - 1]} + \frac{s'(z)}{s(z)^2} \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta < 0, \quad J \in \{H, F\}. \quad (23)$$

Next, differentiate $\log \pi^J(z)$ with respect to z , which gives

$$\frac{1}{\pi^J(z)} \frac{d\pi^J(z)}{dz} = -\frac{\sigma'(z) \sigma(z) - \varepsilon}{\sigma(z) \sigma(z) - 1} + \frac{s'(z)}{s(z)} \left[1 - \frac{\varepsilon - 1}{s(z)} \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right], \quad J \in \{H, F\}. \quad (24)$$

Equation (3) in the main text implies (see Matsuyama and Ushchev (2020)):

$$\frac{s(\zeta)}{\zeta} = \frac{s'(\zeta)}{1 - \sigma(\zeta)}.$$

Therefore

$$\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta = \int_{z^J}^{\bar{z}} \frac{-s'(\zeta)}{\sigma(\zeta) - 1} d\zeta < \int_{z^J}^{\bar{z}} \frac{-s'(\zeta)}{\sigma(z^J) - 1} d\zeta = \frac{s(z) - s(\bar{z})}{\sigma(z) - 1} = \frac{s(z)}{\sigma(z) - 1}. \quad (25)$$

Using this inequality, we obtain

$$\frac{1}{\pi^J(z)} \frac{d\pi^J(z)}{dz} < \left[\frac{s'(z)}{s(z)} - \frac{\sigma'(z)}{\sigma(z)} \right] \frac{\sigma(z) - \varepsilon}{\sigma(z) - 1} < 0, \quad J \in \{H, F\},$$

which we summarize in the following

²⁸Recall that $\sigma(z) > \varepsilon$ at our equilibrium points while $\sigma'(z) \geq 0$ and $s'(z) < 0$.

Lemma 1 *The functions $P^J(z)$ and $\pi^J(z)$ are declining in z for $J \in \{H, F\}$.*

In state B , in which supply chains from both countries are viable, diversified firms prefer to source from the cheaper country F (recall that $q_F < q_H$), if they can. In this case, the number of firms that source from F and pay q_F for their inputs is $n^{B,F}(\boldsymbol{\mu}) = (\mu_f + \mu_b)\rho$. The number of firms that source from country H and pay q_H for inputs is $n^{B,H}(\boldsymbol{\mu}) = \mu_h\rho + \mu_b\rho(1 - \rho)$. The market clearing condition (4) implies

$$1 \equiv n^{B,H}(\boldsymbol{\mu})s[z^{B,H}(\boldsymbol{\mu})] + n^{B,F}(\boldsymbol{\mu})s[z^{B,F}(\boldsymbol{\mu})], \quad (26)$$

which is equation (14) in the main text. The pricing equation (6) implies

$$\frac{z^{B,H}(\boldsymbol{\mu})}{z^{B,F}(\boldsymbol{\mu})} \equiv \left\{ \frac{\sigma[z^{B,H}(\boldsymbol{\mu})]}{\sigma[z^{B,H}(\boldsymbol{\mu})] - 1} \right\} / \left\{ \frac{\sigma[z^{B,F}(\boldsymbol{\mu})]}{\sigma[z^{B,F}(\boldsymbol{\mu})] - 1} \right\} \frac{q_H}{q_F}. \quad (27)$$

From here, we obtain solutions to the relative prices $z^{B,i}$, $i = H, F$, as functions of the vector $\boldsymbol{\mu}$, $z^{B,i}(\boldsymbol{\mu})$, $i \in \{H, F\}$. Furthermore, equation (27) implies that prices of the goods produced with inputs from country F are strictly cheaper than goods produced with inputs from country H in state B . To see this, suppose not, such that $p^{B,H} \leq p^{B,F}$ and therefore $z^{B,H} \leq z^{B,F}$. Equation (27) then returns

$$p^{B,H} = \left(\frac{\sigma(z^{B,H})}{\sigma(z^{B,H}) - 1} \right) q_H \leq \left(\frac{\sigma(z^{B,F})}{\sigma(z^{B,F}) - 1} \right) q_F = p^{B,F} < \left(\frac{\sigma(z^{B,F})}{\sigma(z^{B,F}) - 1} \right) q_H.$$

However, the mark-up function $z \rightarrow \sigma(z)/(\sigma(z) - 1)$ is (weakly) increasing in p under Assumption 2, thus contradicting the strict inequality above. It follows that, for any vector $\boldsymbol{\mu}$, we have $z^{B,H}(\boldsymbol{\mu}) > z^{B,F}(\boldsymbol{\mu})$.

To derive the price index (5) for state B , first note that the pricing equation (6) implies

$$\frac{1}{A^B(\boldsymbol{\mu})} = \frac{z^{B,i}(\boldsymbol{\mu}) \{ \sigma[z^{B,i}(\boldsymbol{\mu})] - 1 \}}{q_i \sigma[z^{B,i}(\boldsymbol{\mu})]}, \quad i \in \{H, F\}.$$

Using (14), we can write

$$\log A^B(\boldsymbol{\mu}) = \sum_{i=H,F} n^{B,i}(\boldsymbol{\mu})s[z^{B,i}(\boldsymbol{\mu})] \log \left\{ \frac{q_i}{z^{B,i}(\boldsymbol{\mu}) \sigma[z^{B,i}(\boldsymbol{\mu})] - 1} \right\}.$$

Now, the price index (5) can be expressed as

$$\log P^B(\boldsymbol{\mu}) := \sum_{i=H,F} n^{B,i}(\boldsymbol{\mu})s[z^{B,i}(\boldsymbol{\mu})] \log P^B[z^{B,i}(\boldsymbol{\mu})], \quad (28)$$

where the function $\log P^J(z)$ is defined in (21). Using this result for the price index, profits of a

firm that sources from country J in state B amount to

$$\pi^{B,i}(\boldsymbol{\mu}) := \frac{s[z^{B,i}(\boldsymbol{\mu})]}{\sigma[z^{B,i}(\boldsymbol{\mu})]} P^B(\boldsymbol{\mu})^{1-\varepsilon}, \quad i \in \{H, F\}. \quad (29)$$

Now consider expected profits from strategy j , Π_j , $j \in \{h, f, b\}$. For a firm that invests in a single supply chain, expected profits are

$$\Pi_h = \delta^H \pi^H \rho + \delta^B \pi^{B,H} \rho - k,$$

$$\Pi_f = \delta^F \pi^F \rho + \delta^B \pi^{B,F} \rho - k,$$

where δ^J is the probability that only supply chains from country J will be available, $J \in \{H, F\}$, and δ^B is the probability that supply chains from both countries will be available. These probabilities are $\delta^H = \gamma_H(1 - \gamma_F)$, $\delta^F = \gamma_F(1 - \gamma_H)$, and $\delta^B = \gamma_F \gamma_H$. Using the profit functions (22) and (29), this yields

$$\Pi_h = \Pi_h(\boldsymbol{\mu}) := \delta^H \frac{s[z^H(\boldsymbol{\mu})]}{\sigma[z^H(\boldsymbol{\mu})]} P^H [z^H(\boldsymbol{\mu})]^{1-\varepsilon} \rho + \delta^B \frac{s[z^{B,H}(\boldsymbol{\mu})]}{\sigma[z^{B,H}(\boldsymbol{\mu})]} P^B(\boldsymbol{\mu})^{1-\varepsilon} \rho - k, \quad (30)$$

$$\Pi_f = \Pi_f(\boldsymbol{\mu}) := \delta^F \frac{s[z^F(\boldsymbol{\mu})]}{\sigma[z^F(\boldsymbol{\mu})]} P^F [z^F(\boldsymbol{\mu})]^{1-\varepsilon} \rho + \delta^B \frac{s[z^{B,F}(\boldsymbol{\mu})]}{\sigma[z^{B,F}(\boldsymbol{\mu})]} P^B(\boldsymbol{\mu}, \mathbf{q})^{1-\varepsilon} \rho - k. \quad (31)$$

For a firm that invests in supply chains in both countries, expected profits are

$$\Pi_b = \sum_{J=H,F} \delta^J \pi^J \rho + \delta^B [\pi^{B,F} \rho + \pi^{B,H} (1 - \rho) \rho] - 2k.$$

A firm that adopts this strategy expects profits π^F if the supply chains survive only in country F , provided it does not suffer an idiosyncratic disruption there. Similarly, it expects profits π^H if the supply chains survive only in country H , provided it does not suffer an idiosyncratic disruption there. In case supply chains in both countries are viable, the firm expects profits $\pi^{B,F}$ if its bilateral relation survives in country F and profits $\pi^{B,H}$ if its bilateral relation in F does not survive but that in H does survive. Using (22) and (29), this yields

$$\begin{aligned} \Pi_b = \Pi_b(\boldsymbol{\mu}) := & \sum_{J=H,F} \delta^J \frac{s[z^J(\boldsymbol{\mu})]}{\sigma[z^J(\boldsymbol{\mu})]} P^J [z^J(\boldsymbol{\mu})]^{1-\varepsilon} \rho \\ & + \delta^B \left\{ \frac{s[z^{B,F}(\boldsymbol{\mu})]}{\sigma[z^{B,F}(\boldsymbol{\mu})]} + \frac{s[z^{B,H}(\boldsymbol{\mu})]}{\sigma[z^{B,H}(\boldsymbol{\mu})]} (1 - \rho) \right\} P^B(\boldsymbol{\mu})^{1-\varepsilon} \rho - 2k. \end{aligned} \quad (32)$$

Using these functions and $P^J(\boldsymbol{\mu}) := P^J [z^J(\boldsymbol{\mu})]$, $J \in \{H, F\}$, we obtain the welfare function (11) in the main text.

Section 2.6

Armed with these expressions, we now prove Figure 1. Suppose that $q_F \nearrow q_H$ and $\gamma_F < \gamma_H$. In this partially asymmetric world, given an aggregate state J , the country from which the input is supplied is irrelevant. In particular, in state B , equation (27) dictates that $z^{B,F} \rightarrow z^{B,H}$. As in state H and F , we can then use the notation $z^B(\boldsymbol{\mu}) := z^{B,H}(\boldsymbol{\mu}) = z^{B,F}(\boldsymbol{\mu})$. Consequently, only the total number of products available in state B matters, $n^B(\boldsymbol{\mu}) := n^{B,F}(\boldsymbol{\mu}) + n^{B,H}(\boldsymbol{\mu}) = \rho(1 + (1 - \rho)(1 - \mu_h - \mu_f))$, and the market clearing condition (26) rewrites $1 = n^B(\boldsymbol{\mu})s[z^B(\boldsymbol{\mu})]$.

Inasmuch as country H is safer than country F , relatively more firms want to settle a single supply chain in H than in F . To see this, suppose the contrary: firms invest relatively more in the risky country, $\mu_f > 0$ and $\mu_f \geq \mu_h$. From the market clearing conditions, we then have

$$s[z^F(\boldsymbol{\mu})] = \frac{1}{\rho(\mu_f + \mu_b)} \leq \frac{1}{\rho(\mu_h + \mu_b)} = s[z^H(\boldsymbol{\mu})].$$

Since $s'(z) < 0$, it must be that $z^H(\boldsymbol{\mu}) \leq z^F(\boldsymbol{\mu})$. But $\pi'(z) < 0$, so that $\delta^F \pi[z^F(\boldsymbol{\mu})] \leq \delta^F \pi[z^H(\boldsymbol{\mu})] < \delta^H \pi[z^H(\boldsymbol{\mu})]$. However, this in turn implies that the expected profits of the foreign strategy are lower, $\Pi_f < \Pi_h$, and therefore $\mu_f = 0$, a contradiction. Hence, in equilibrium, it must either be that no firms invest in the risky country, $\mu_f = 0$, or if some firms do, relatively more firms need to invest in the safe country, $\mu_f > 0$ and $\mu_h > \mu_f$. Accordingly, it must also be that the expected profits of the safer strategy are (weakly) higher than the expected profits of the less safe strategy, $\Pi_h \geq \Pi_f$.

Given that the expected profits of the home supply chain are weakly higher than those with a supplier in the foreign country, firms' investments are dictated by two comparisons: home versus foreign supply chains, $\Pi_h(\mu_h, \mu_f, \mu_b) - \Pi_f(\mu_h, \mu_f, \mu_b)$, and single supply chain at home versus diversification, $\Pi_h(\mu_h, \mu_f, \mu_b) - \Pi_b(\mu_h, \mu_f, \mu_b)$.²⁹ Using the expressions for expected profits (30:32), these two optimality conditions respectively read

$$\Pi_h(\mu_h, \mu_f, \mu_b) \geq \Pi_f(\mu_h, \mu_f, \mu_b) \iff \delta^H \pi[z^H(\mu_h, \mu_f, \mu_b)] \geq \delta^F \pi[z^F(\mu_h, \mu_f, \mu_b)],$$

and

$$\Pi_b(\mu_h, \mu_f, \mu_b) \geq \Pi_h(\mu_h, \mu_f, \mu_b) \iff \delta^F \pi[z^F(\mu_h, \mu_f, \mu_b)] + \delta^B \rho(1 - \rho)\pi[z^B(\mu_h, \mu_f, \mu_b)] \geq k.$$

In addition, profits must be positive, $\Pi_j(\mu_h, \mu_f, \mu_b) \geq 0$ for $j \in \{h, f, b\}$. These three conditions together dictate the features of the equilibrium.

Figure 1 depicts the fraction of firms choosing each strategy as a function of k when profits are unbounded; that is when $\lim_{z \rightarrow 0^+} \pi(z) = \infty$. We make this assumption throughout the proof, and come back to the case of bounded profit at the end of the section.

²⁹Without $\Pi_h \geq \Pi_f$, we would also need to compare $\Pi_f - \Pi_b$.

Existence of k_1 For $k \rightarrow 0^+$, investing in resilience is clearly the most profitable option, $\Pi_b > \Pi_h > \Pi_f$, where the second inequality follows from $\delta^H \pi[z^H(0, 0, 1)] > \delta^F \pi[z^F(0, 0, 1)]$. Hence, for low k , $\mu_h = 0 = \mu_f$ and $\mu_b = 1$. As the fixed cost increases, the gap between $\Pi_h(0, 0, 1) - \Pi_b(0, 0, 1)$ shrinks to the point where the two strategies yield the same expected profits. This occurs at k_1 , defined by

$$k_1 := \delta^F \rho \pi[z^F(0, 0, 1)] + \delta^B \rho (1 - \rho) \pi[z^B(0, 0, 1)].$$

Furthermore, at k_1 , expected profits of strategy h reads

$$\Pi_h = \delta^B \rho^2 \pi[z^B(0, 0, 1)] + \rho (\delta^H \pi[z^H(0, 0, 1)] - \delta^F \pi[z^F(0, 0, 1)]) > 0,$$

where the inequality follows from $z^H(0, 0, 1) = z^F(0, 0, 1)$ and $\delta^H > \delta^F$. Hence, $\Pi_b > 0$ for all $k \in [0, k_1]$.

Existence of k_2 At $k = k_1$, we thus have $\Pi_b(0, 0, 1) = \Pi_h(0, 0, 1) > \Pi_f(0, 0, 1)$. For $k \in B^+(k_1)$, $\Pi_b(0, 0, 1) < \Pi_h(0, 0, 1)$, such that $(0, 0, 1)$ cannot be an equilibrium.³⁰ Instead, it must be that $\mu_h > 0$ and $\mu_b = 1 - \mu_h > 0$. When that is the case, firms must be indifferent between the two strategies and must prefer them to the offshoring strategy,

$$\begin{aligned} k &= \delta^F \rho \pi[z^F(\mu_h, 0, 1 - \mu_h)] + \delta^B \rho (1 - \rho) \pi[z^B(\mu_h, 0, 1 - \mu_h)], \\ 0 &> \delta^F \pi[z^F(\mu_h, 0, 1 - \mu_h)] - \delta^H \pi[z^H(\mu_h, 0, 1 - \mu_b)], \\ \mu_f &= 0, \mu_b = 1 - \mu_h > 0. \end{aligned}$$

First, note that the first and second conditions imply that expected profits are positive. For instance, the expected profits of strategy h is given by

$$\Pi_h = \delta^B \rho^2 \pi[z^B(\mu_h, 0, 1 - \mu_h)] + \rho \{ \delta^H \pi[z^H(\mu_h, 0, 1 - \mu_h)] - \delta^F \rho \pi[z^F(\mu_h, 0, 1 - \mu_h)] \} > 0,$$

where the first equality follows from the first condition and the inequality follows from the second condition. Second, when $\mu_h > 0$ and $\mu_b = 1 - \mu_h > 0$, the market clearing conditions in states F , H and B read $s[z^F(\boldsymbol{\mu})] \rho (1 - \mu_h) = 1$, $s[z^H(\boldsymbol{\mu})] \rho = 1$ and $s[z^B(\boldsymbol{\mu})] \rho [1 + (1 - \mu_h)(1 - \rho)] = 1$ respectively. Hence, $\pi[z^F(\boldsymbol{\mu})]$ and $\pi[z^B(\boldsymbol{\mu})]$ are increasing in μ_h , while $\pi[z^H(\boldsymbol{\mu})]$ is independent of $\boldsymbol{\mu}$. This implies that μ_h is increasing in k for $k \in B^+(k_1)$. Finally, unbounded profits imply that there exists a $\bar{\mu}_h^2$ such that the second condition cannot hold for any $\mu_h > \bar{\mu}_h^2$.³¹ This limiting μ_h is defined by

$$\delta^H \pi(\bar{z}) = \delta^F \pi[z^F(\bar{\mu}_h^2, 0, 1 - \bar{\mu}_h^2)].$$

³⁰The correspondence $B^+ : \mathbb{R} \mapsto 2^{\mathbb{R}}$ is defined as $B^+(x) = [x, x + \vartheta)$ for $\vartheta > 0$ small.

³¹Otherwise, the equality would hold for $\mu_h \nearrow 1 \iff z^F \searrow 0$, at which point $\pi(z^F) \rightarrow \infty > \pi[z^H(1, 0, 0)]$, a contradiction.

Accordingly, we define the second fixed cost threshold k_2 as

$$k_2 = \delta^F \rho \pi [z^F(\bar{\mu}_h^2, 0, 1 - \bar{\mu}_h^2)] + \delta^B \rho (1 - \rho) \pi [z^B(\bar{\mu}_h^2, 0, 1 - \bar{\mu}_h^2)].$$

For all $k \in B^+(k_2)$, we would have $\mu_h > \bar{\mu}_h^2$, which in turn would imply $\Pi_f > \Pi_h$ so that $(\mu_h, 0, 1 - \mu_h)$ cannot be an equilibrium allocation.

Existence of k_3 For $k \in B^+(k_2)$, the equilibrium must be of the type $\mu_h > 0$, $\mu_f > 0$ and $\mu_b = 1 - \mu_h - \mu_f > 0$. When that is the case, it must be that $\Pi_b = \Pi_h = \Pi_f$, or

$$\begin{aligned} k &= \delta^F \rho \pi [z^F(\boldsymbol{\mu})] + \delta^B \rho (1 - \rho) \pi [z^B(\boldsymbol{\mu})], \\ 0 &= \delta^H [z^H(\boldsymbol{\mu})] - \delta^F \pi [z^F(\boldsymbol{\mu})], \\ 1 &\geq \mu_h + \mu_f(\mu_h). \end{aligned}$$

As before, note that the first and second conditions together imply that the expected profits of the three strategies are positive. The market clearing condition in each state are $s[z^F(\boldsymbol{\mu})]\rho(1 - \mu_h) = 1$, $s[z^H(\boldsymbol{\mu})]\rho(1 - \mu_f) = 1$, and $s[z^B(\boldsymbol{\mu})]\rho[1 + (1 - \rho)(1 - \mu_f - \mu_h)] = 1$. In particular, z^F , z^H and z^B are only functions of μ_h , μ_f and $\mu_h + \mu_f$ respectively. Accordingly, let $\tilde{z}(\mu)$ and $\tilde{z}^B(\mu)$ be defined respectively by $s[\tilde{z}(\mu)]\rho(1 - \mu) = 1$ and $s[\tilde{z}^B(\mu)]\rho[1 + (1 - \rho)(1 - \mu)] = 1$. The first two equilibrium conditions then rewrite

$$\begin{aligned} k &= \delta^F \rho \pi [\tilde{z}(\mu_h)] + \delta^B \rho (1 - \rho) \pi [\tilde{z}^B(\mu_h + \mu_f)], \\ 0 &= \delta^H \pi [\tilde{z}(\mu_f)] - \delta^F \pi [\tilde{z}(\mu_h)]. \end{aligned}$$

Both \tilde{z} and \tilde{z}^B are decreasing functions, such that $d\pi[\tilde{z}(\mu)]/d\mu > 0$. The second condition thus implies that μ_f is increasing in μ_h , and the first condition implies that μ_h is increasing in k for $k \in B^+(k_2)$. Finally, unbounded profits imply that there always exists an upper bound $\bar{\mu}_h^3$ such that

$$\delta^F \pi [\tilde{z}(\bar{\mu}_h^3)] = \delta^H \pi [\tilde{z}(1 - \bar{\mu}_h^3)].$$

The first and third condition together then imply that there exists a fixed cost threshold k_3 such that $(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0)$ is the equilibrium allocation, and $\Pi_b(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0) < \Pi_h(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0) = \Pi_f(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0)$ for $k \in B^+(k_3)$. This cutoff is defined by

$$k_3 = \delta^F \rho \pi [\tilde{z}(\bar{\mu}_h^3)] + \delta^B \rho (1 - \rho) \pi [\tilde{z}^B(1)].$$

Existence of k_4 At k_3 , we have already argued that $\Pi_h(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0) = \Pi_f(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0) > 0$. Since $\Pi_h(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0)$ is monotonically decreasing in k , there exists a $k_4 > k_3$ such that profits of

the h and f strategy are nil,

$$k_4 = \delta^F \rho \pi[\tilde{z}(\bar{\mu}_h^3)] + \delta^B \rho \pi[\tilde{z}^B(1)].$$

Beyond k_4 For $k \in B^+(k_4)$, it clearly cannot be that $(\bar{\mu}_h^3, 1 - \bar{\mu}_h^3, 0)$ is an equilibrium. We first show that, locally, it must be that $\mu_h + \mu_f < 1$ and $\mu_b = 0$. For this to be an equilibrium, it clearly cannot be that $\Pi_h > 0$, for otherwise other firms would enter till either $\Pi_h = 0$ or $\mu_h + \mu_f = 1$. A symmetric argument exists for Π_f . Hence, for $k \in B^+(k_4)$, it must be that $\Pi_h = \Pi_f = 0 > \Pi_b$. Furthermore, when $\mu_h + \mu_f < 1$ and $\mu_b = 0$, the market clearing conditions in state H , F and B respectively read

$$s[z^H(\boldsymbol{\mu})]\rho\mu_h = 1, \quad s[z^F(\boldsymbol{\mu})]\rho\mu_f = 1, \quad s[z^B(\boldsymbol{\mu})](\mu_f + \mu_h)\rho = 1.$$

Let $\zeta(\mu)$ denote the (increasing) function that solves $s[\zeta(\mu)]\rho\mu = 1$. The equilibrium conditions $\Pi_h = \Pi_f = 0$ can then be written as

$$\begin{aligned} \delta^H \rho \pi[\zeta(\mu_h)] + \delta^B \rho \pi[\zeta(\mu_f + \mu_h)] &= k, \\ \delta^F \pi[\zeta(\mu_f)] - \delta^H \pi[\zeta(\mu_h)] &= 0, \\ \mu_f + \mu_h &< 1. \end{aligned}$$

From the second condition, μ_f is increasing in μ_h . From the first condition, the right hand side is increasing in k and the left-hand is decreasing in μ_h . Hence, μ_h is decreasing in k for $k \in B^+(k_4)$. Finally, when profits are unbounded, as k becomes infinitely large, the left-hand side of the first condition has to be large as well, which requires $\mu_h \searrow 0$. From the second condition, $\mu_h \searrow 0$ implies $\mu_f \searrow 0$. Hence, the two conditions above hold jointly for any $k > k_4$, which is depicted in Figure 1.

The proof of Figure 1 holds when profits are unbounded, $\lim_{z \searrow 0} \pi(z) = \infty$. Yet, with HSA preferences and $\varepsilon > 1$, profits may be bounded even as prices tend to zero. When that is the case, there may exist two further thresholds k_5 and k_6 such that, for k between k_5 and k_6 , we have $\mu_h > 0$ and $\mu_f = 0$, and for $k > k_6$, no firms enter, $\mu_f = \mu_h = \mu_b = 0$. Furthermore, when profits are bounded, the interval (k_2, k_3) may be empty. However, $k_2 < k_3$ is guaranteed if the difference between γ_F and γ_H is not too large, or alternatively, if $\varepsilon - 1$ is small – in which case profits are necessarily unbounded. Numerically, in Section 5, we do find that $k_2 < k_3$ for relatively large risk premium and elasticity of substitution, namely $\gamma_F/\gamma_H = 0.7$ and $\varepsilon = 1.7$.

Section 3

We begin by deriving the social welfare function in the presence of consumption subsidies that equate consumer prices to marginal costs according to where inputs are sourced.

First, consider the pricing problem facing a producer that pays q per unit for its inputs that faces an aggregator A and that recognizes that consumers will pay only a fraction ν of the sticker price in view of the consumption subsidy at rate $1 - \nu$. Then the consumer price of the final product is νp , where p is the producer price. As noted, the government sets the subsidy so that $\nu p = q$, and firms take the subsidy rate as given. They choose the sticker price as

$$p = \arg \max_{\check{p}} P^{1-\varepsilon} s \left(\frac{\nu \check{p}}{A} \right) (\nu \check{p})^{-1} (\check{p} - q).$$

The solution to this problem yields

$$p = \frac{\sigma(p/A)}{\sigma(p/A) - 1} q.$$

Therefore, the optimal subsidy rates are

$$v(z^J) = \frac{\sigma(z^J) - 1}{\sigma(z^J)}, \quad J \in \{H, F\},$$

$$v(z^{B,i}) = \frac{\sigma(z^{B,i}) - 1}{\sigma(z^{B,i})}, \quad i \in \{H, F\}.$$

These optimal subsidies vary across states of the world if the elasticity of substitution is not constant, and they vary in state B according to the source of the inputs embodied in the final good.

We consider outcomes with $\boldsymbol{\mu} \gg 0$. Now, the market clearing conditions (12) to (14) must still be satisfied, but (27) is replaced with

$$\frac{z^{B,H}}{z^{B,F}} = \lambda := \frac{q_H}{q_F}. \quad (33)$$

It follows that the functions $z^J(\boldsymbol{\mu})$, $J \in \{H, F\}$ are the same as before, but the functions $z^{B,H}(\boldsymbol{\mu})$ and $z^{B,F}(\boldsymbol{\mu})$ are replaced by $\tilde{z}^{B,F}(\boldsymbol{\mu})$ and $\tilde{z}^{B,H}(\boldsymbol{\mu}) \equiv \lambda \tilde{z}^{B,F}(\boldsymbol{\mu})$, where the latter functions are obtained as solutions to (33) and (14). In what follows, we denote with a tilde any function that arise when the consumption subsidies are in place, except for those functions—like $z^H(\boldsymbol{\mu})$ and $z^F(\boldsymbol{\mu})$ —that do not change as a result of the subsidies.

With the consumption subsidies in place, firms' operating profits in the various states are

$$\tilde{\pi}^J(\boldsymbol{\mu}) := \frac{s[z^J(\boldsymbol{\mu})]}{\sigma[z^J(\boldsymbol{\mu})] - 1} \tilde{P}^J [z^J(\boldsymbol{\mu})]^{1-\varepsilon}, \quad J \in \{H, F\}, \quad (34)$$

$$\tilde{\pi}^{B,i}(\boldsymbol{\mu}) := \frac{s[\tilde{z}^{B,i}(\boldsymbol{\mu})]}{\sigma[\tilde{z}^{B,i}(\boldsymbol{\mu})] - 1} \tilde{P}^B(\boldsymbol{\mu})^{1-\varepsilon}, \quad i \in \{H, F\}, \quad (35)$$

where, using (5), the price indexes are

$$\log \tilde{P}^J(\boldsymbol{\mu}) := \log \tilde{P}^J [z^J(\boldsymbol{\mu})] = C_P + \log \frac{q_J}{z^J(\boldsymbol{\mu})} - n^J(\boldsymbol{\mu}) \int_{z^J(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta, \quad J \in \{H, F\}, \quad (36)$$

$$\log \tilde{P}^B(\boldsymbol{\mu}) = C_P + \log \tilde{A}^B(\boldsymbol{\mu}) - \sum_{i=H,F} n^{B,i}(\boldsymbol{\mu}) \int_{z^{B,i}(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta, \quad (37)$$

and $\tilde{A}^B(\boldsymbol{\mu})$ is obtained from

$$1 \equiv n^{B,H}(\boldsymbol{\mu}) s \left[\frac{q_H}{\tilde{A}^B(\boldsymbol{\mu})} \right] + n^{B,F}(\boldsymbol{\mu}) s \left[\frac{q_F}{\tilde{A}^B(\boldsymbol{\mu})} \right].$$

Therefore,

$$\tilde{A}^B(\boldsymbol{\mu}) \equiv \frac{q_F}{\tilde{z}^{B,F}(\boldsymbol{\mu})} \equiv \frac{q_F}{\tilde{z}^{B,F}(\boldsymbol{\mu})}. \quad (38)$$

Lump-sum taxes are levied in state J to finance the consumption subsidies paid in that state. Using the subsidy rates $v(z) = [\sigma(z) - 1] / \sigma(z)$, the required taxes are

$$\begin{aligned} \tilde{T}^H(\boldsymbol{\mu}) &= -(\mu_h + \mu_b) \tilde{\pi}^H(\boldsymbol{\mu}) \rho, \\ \tilde{T}^F(\boldsymbol{\mu}) &= -(\mu_f + \mu_b) \tilde{\pi}^F(\boldsymbol{\mu}) \rho, \\ \tilde{T}^B(\boldsymbol{\mu}) &= -(\mu_f + \mu_b) \tilde{\pi}^{B,F}(\boldsymbol{\mu}) \rho - [\mu_h + \mu_b (1 - \rho)] \tilde{\pi}^{B,H}(\boldsymbol{\mu}) \rho. \end{aligned}$$

It follows that

$$\sum_{J=H,F,B} \delta^J \tilde{T}^J(\boldsymbol{\mu}) + \sum_{j=h,f,b} \mu_j \tilde{\Pi}_j(\boldsymbol{\mu}) = -(\mu_h + \mu_f + 2\mu_b) k.$$

The welfare function (11) therefore becomes

$$\tilde{W}(\boldsymbol{\mu}) = \bar{Y} + \frac{1}{\varepsilon - 1} \sum_{J=H,F,B} \delta^J \tilde{P}^J(\boldsymbol{\mu})^{1-\varepsilon} - (\mu_h + \mu_f + 2\mu_b) k. \quad (39)$$

We next characterize the wedges that determine optimal supply chain policies. To this end, we first derive the first-order conditions for the optimal allocation $\boldsymbol{\mu}^o \gg 0$, which are characterized by $\frac{d\tilde{W}(\boldsymbol{\mu}^o)}{d\mu_j} = 0$, $j = h, f$, where, for a general function $G(\boldsymbol{\mu})$, $dG(\boldsymbol{\mu})/d\mu_j$ is the change in $G(\cdot)$ from the variation $d\mu_j = -d\mu_b > 0$. Using the price indexes (36) and (37), together with (12), (13) and

(38), we obtain

$$\begin{aligned} \frac{d\tilde{W}(\boldsymbol{\mu}^o)}{d\mu_j} &= - \sum_{J=H,F} \delta^J \tilde{P}^J(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\int_{z^J(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \frac{dn^J(\boldsymbol{\mu}^o)}{d\mu_j} \\ &\quad - \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\frac{d \log \tilde{A}^B(\boldsymbol{\mu}^o)}{d\mu_j} + \sum_{i=H,F} n^{B,i}(\boldsymbol{\mu}^o) \frac{s[\tilde{z}^{B,i}(\boldsymbol{\mu}^o)]}{\tilde{z}^{B,i}(\boldsymbol{\mu}^o)} \frac{d\tilde{z}^{B,i}(\boldsymbol{\mu}^o)}{d\mu_j} \right] \\ &\quad + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \sum_{i=H,F} \left[\int_{z^{B,i}(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \frac{dn^{B,i}(\boldsymbol{\mu}^o)}{d\mu_j} + k = 0, \end{aligned}$$

for $j \in \{h, f\}$. Note, however, that $d \log \tilde{z}^{B,F}(\boldsymbol{\mu}^o)/d\mu_j = d \log \tilde{z}^{B,H}(\boldsymbol{\mu}^o)/d\mu_j$. Then, using (14),

$$\begin{aligned} &\frac{d \log \tilde{A}^B(\boldsymbol{\mu}^o)}{d\mu_j} + \sum_{i=H,F} n^{B,i}(\boldsymbol{\mu}^o) \frac{s[\tilde{z}^{B,i}(\boldsymbol{\mu}^o)]}{\tilde{z}^{B,i}(\boldsymbol{\mu}^o)} \frac{d\tilde{z}^{B,i}(\boldsymbol{\mu}^o)}{d\mu_j} \\ &= - \frac{d \log \tilde{z}^{B,F}(\boldsymbol{\mu}^o)}{d\mu_j} \left[1 - \sum_{i=H,F} n^{B,i}(\boldsymbol{\mu}^o) s[\tilde{z}^{B,i}(\boldsymbol{\mu}^o)] \right] = 0. \end{aligned}$$

In other words,

$$\frac{d \log \tilde{P}^B(\boldsymbol{\mu}^o)}{d\mu_j} = - \sum_{i=H,F} \left[\int_{z^{B,i}(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \frac{dn^{B,i}(\boldsymbol{\mu}^o)}{d\mu_j}. \quad (40)$$

The first-order conditions for the first-best allocation can therefore be written as

$$\begin{aligned} \frac{d\tilde{W}(\boldsymbol{\mu}^o)}{d\mu_j} &= - \sum_{J=H,F} \delta^J \tilde{P}^J(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\int_{z^J(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \frac{dn^J(\boldsymbol{\mu}^o)}{d\mu_j} \\ &\quad + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \sum_{i=H,F} \left[\int_{z^{B,i}(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \frac{dn^{B,i}(\boldsymbol{\mu}^o)}{d\mu_j} + k = 0, \end{aligned}$$

for $j = h, f$.

Next use $n^F(\boldsymbol{\mu}) = (1 - \mu_h) \rho$, $n^H(\boldsymbol{\mu}) = (1 - \mu_f) \rho$, $n^{B,F}(\boldsymbol{\mu}) = (\mu_f + \mu_b) \rho$, and $n^{B,H}(\boldsymbol{\mu}) = [\mu_h + \mu_b(1 - \rho)] \rho$ to obtain $dn^F(\boldsymbol{\mu})/d\mu_f = 0$, $dn^F(\boldsymbol{\mu})/d\mu_h = -\rho$, $dn^H(\boldsymbol{\mu})/d\mu_h = 0$, $dn^H(\boldsymbol{\mu})/d\mu_f = -\rho$, $dn^{B,F}(\boldsymbol{\mu})/d\mu_f = 0$, $dn^{B,F}(\boldsymbol{\mu})/d\mu_h = -\rho$, $dn^{B,H}(\boldsymbol{\mu})/d\mu_f = -(1 - \rho) \rho$, $dn^{B,H}(\boldsymbol{\mu})/d\mu_h = \rho^2$ for $\boldsymbol{\mu} \gg 0$. These expressions allow us to represent $d\tilde{W}(\boldsymbol{\mu}^o)/d\mu_j = 0$ for $j \in \{h, f\}$ as

$$k = \delta^H \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\int_{z^H(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \rho + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\int_{z^{B,H}(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] (1 - \rho) \rho \quad (41)$$

and

$$k = \delta^F \tilde{P}^F(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\int_{z^F(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \rho + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \left[\int_{\tilde{z}^{B,F}(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta - \rho \int_{\tilde{z}^{B,H}(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \rho. \quad (42)$$

By definition,

$$w_j^o := \tilde{\Pi}_j(\boldsymbol{\mu}^o) - \tilde{\Pi}_b(\boldsymbol{\mu}^o) - \frac{d\tilde{W}(\boldsymbol{\mu}^o)}{d\mu_j}, \quad j \in \{h, f\}.$$

We therefore obtain

$$w_f^o = k - \delta^H \tilde{\pi}^H(\boldsymbol{\mu}^o) \rho - \delta^B \tilde{\pi}^{B,H}(\boldsymbol{\mu}^o) (1 - \rho) \rho, \quad (43)$$

and

$$w_h^o = k - \delta^F \tilde{\pi}^F(\boldsymbol{\mu}^o) \rho - \delta^B [\tilde{\pi}^{B,F}(\boldsymbol{\mu}^o) - \rho \tilde{\pi}^{B,H}(\boldsymbol{\mu}^o)] \rho. \quad (44)$$

Next we use (34), (35) and (41) to derive

$$w_f^o = \delta^H \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \Phi[\tilde{z}^H(\boldsymbol{\mu}^o)] \rho + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \Phi[\tilde{z}^{B,H}(\boldsymbol{\mu}^o)] (1 - \rho) \rho, \quad (45)$$

where

$$\Phi(z) := \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta - \frac{s(z)}{\sigma(z) - 1},$$

which is equation (17) in the main text. Moreover, using (34), (35) and (42), we obtain

$$w_h^o = \delta^F \tilde{P}^F(\boldsymbol{\mu}^o)^{1-\varepsilon} \Phi[\tilde{z}^F(\boldsymbol{\mu}^o)] \rho + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \Phi[\tilde{z}^{B,H}(\boldsymbol{\mu}^o)] \rho (1 - \rho) + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \{ \Phi[\tilde{z}^{B,F}(\boldsymbol{\mu}^o)] - \Phi[\tilde{z}^{B,H}(\boldsymbol{\mu}^o)] \} \rho, \quad (46)$$

which is equation (18) in the main text.

We now want to characterize the absolute and relative sign of these wedges. First, note that (25) implies $\Phi(z) < 0$ under Marshall's Second Law of Demand. Therefore, $w_f^o < 0$. Second,

$$\Phi'(z) = -\frac{s(z)}{z} - \frac{s'(z)}{\sigma(z) - 1} + \frac{s(z)}{[\sigma(z) - 1]^2} \sigma'(z) = \frac{s(z)}{[\sigma(z) - 1]^2} \sigma'(z) > 0.$$

Since $\tilde{z}^{B,H}(\boldsymbol{\mu}^o) = \lambda \tilde{z}^{B,F}(\boldsymbol{\mu}^o) > \tilde{z}^{B,F}(\boldsymbol{\mu}^o)$, this implies $\Phi[\tilde{z}^{B,F}(\boldsymbol{\mu}^o)] - \Phi[\lambda \tilde{z}^{B,F}(\boldsymbol{\mu}^o)] < 0$ and, therefore, $w_h^o < 0$. These findings are summarized in

Lemma 2 *Let $\sigma'(z) > 0$ for $z \in (0, \bar{z})$. Then $w_j^o < 0$ for $j \in \{h, f\}$.*

Now consider two special cases. In the limiting case of symmetric CES preferences, σ is constant and $s(z) := \alpha z^{1-\sigma}$, where $\alpha > 0$ is a constant. In this case $\Phi(z) = 0$ for all z and thus $w_h^o = w_f^o = 0$. That is, the optimal allocation is achieved with no government intervention in the formation of supply chains; i.e., $\varphi_j = 0$ for $j \in \{h, f, b\}$.

In the case of symmetric translog preferences, $s(z) := -\theta \log z$, where $\theta > 0$ is a constant and $z \in (0, 1)$. These preferences imply

$$\int_z^1 \frac{s(\zeta)}{\zeta} d\zeta = \frac{1}{2} \frac{s(z)}{\sigma(z) - 1}.$$

The first-order conditions (41) and (42) become

$$2k = \delta^H \tilde{\pi}^H(\boldsymbol{\mu}^o) \rho + \delta^B \tilde{\pi}^{B,H}(\boldsymbol{\mu}^o) (1 - \rho) \rho,$$

$$2k = \delta^F \tilde{\pi}^{F,F}(\boldsymbol{\mu}^o) \rho + \delta^B [\tilde{\pi}^{B,F}(\boldsymbol{\mu}^o) - \rho \tilde{\pi}^{B,H}(\boldsymbol{\mu}^o)] \rho.$$

Combining these with (43) and (44) yields

$$w_f^o = w_h^o = -k. \quad (47)$$

That is, in the translog case, the optimal allocation is achieved by a policy that subsidizes fully the cost of all investments in single-country supply chains, i.e., $\varphi_b = 0$ and $\varphi_h = \varphi_f = k$.³² We summarize these findings in

Lemma 3 (a) *In the case of symmetric CES preferences, $w_j^o = 0$ for $j \in \{h, f\}$, which implies that $\varphi_j = 0$ for $j \in \{h, f, b\}$ induces the optimal allocation.* (b) *In the case of symmetric translog preferences $w_f^o = w_h^o = -k$, which implies that $\varphi_b = 0$ and $\varphi_h = \varphi_f = k$ induces the optimal allocation.*

Finally, consider the difference in the absolute sizes of the wedges. Using (45) and (46), we have

$$\begin{aligned} |w_h^o| - |w_f^o| &= \delta^H \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \Phi[\tilde{z}^H(\boldsymbol{\mu}^o)] \rho - \delta^F \tilde{P}^F(\boldsymbol{\mu}^o)^{1-\varepsilon} \Phi[\tilde{z}^F(\boldsymbol{\mu}^o)] \rho \\ &\quad + \delta^B \tilde{P}^B(\boldsymbol{\mu}^o)^{1-\varepsilon} \{ \Phi[\tilde{z}^{B,H}(\boldsymbol{\mu}^o)] - \Phi[\tilde{z}^{B,F}(\boldsymbol{\mu}^o)] \} \rho. \end{aligned} \quad (48)$$

In the limit case $q_H \searrow q_F =: q$, the last term on the right-hand side of this equation equals zero. Moreover, the first-order conditions (41) and (42) imply

$$\delta^H \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \int_{z^H(\boldsymbol{\mu}^o)}^{\tilde{z}} \frac{s(\zeta)}{\zeta} d\zeta = \delta^F \tilde{P}^F(\boldsymbol{\mu}^o)^{1-\varepsilon} \int_{z^F(\boldsymbol{\mu}^o)}^{\tilde{z}} \frac{s(\zeta)}{\zeta} d\zeta. \quad (49)$$

³²Alternatively, the planner can tax diversification with $\varphi_b = -k$, while leaving $\varphi_h = \varphi_f = 0$.

Therefore,

$$|w_h^o| - |w_f^o| = \delta^H \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \frac{s[z^H(\boldsymbol{\mu}^o)]}{\sigma[z^H(\boldsymbol{\mu}^o)]-1} \rho - \delta^F \tilde{P}^F(\boldsymbol{\mu}^o)^{1-\varepsilon} \frac{s[z^F(\boldsymbol{\mu}^o)]}{\sigma[z^F(\boldsymbol{\mu}^o)]-1} \rho.$$

Using (49), this difference can be expressed as

$$|w_h^o| - |w_f^o| = \rho \delta^H \tilde{P}^H(\boldsymbol{\mu}^o)^{1-\varepsilon} \frac{\left\{ \frac{s[z^H(\boldsymbol{\mu}^o)]}{\sigma[z^H(\boldsymbol{\mu}^o)]-1} \right\} \left\{ \frac{s[z^F(\boldsymbol{\mu}^o)]}{\sigma[z^F(\boldsymbol{\mu}^o)]-1} \right\}}{\int_{z^F(\boldsymbol{\mu}^o)}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta} \left\{ \Psi[z^F(\boldsymbol{\mu}^o)] - \Psi[z^H(\boldsymbol{\mu}^o)] \right\}, \quad (50)$$

where

$$\Psi(z) := \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta / \frac{s(z)}{\sigma(z)-1}.$$

We have established

Lemma 4 *Let $q_H \searrow q_F$. Then $|w_h^o| > |w_f^o|$ if and only if $\Psi[z^F(\boldsymbol{\mu}^o)] > \Psi[z^H(\boldsymbol{\mu}^o)]$.*

Next note from (36) that with equal costs in both countries, and $n^J(\boldsymbol{\mu}) s[z^J(\boldsymbol{\mu})] = 1$,

$$\log \tilde{P}^J(\boldsymbol{\mu}) = \log \check{P}[z^J(\boldsymbol{\mu})],$$

where

$$\log \check{P}(z) := C_P + \log \frac{q}{z} - \frac{1}{s(z)} \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta.$$

It follows that $\check{P}(z) \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta$ is a declining function of z . To see this, consider

$$\frac{d}{dz} \log \left\{ \check{P}(z)^{1-\varepsilon} \left[\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \right\} = -(\varepsilon - 1) \frac{s'(z)}{s(z)^2} \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta - \frac{s(z)}{z \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta}.$$

We use

$$\frac{s'(z)}{s(z)} = -\frac{\sigma(z)-1}{z}$$

to obtain

$$\frac{d}{dz} \log \left\{ \check{P}(z)^{1-\varepsilon} \left[\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \right\} = (\varepsilon - 1) \frac{\sigma(z)-1}{zs(z)} \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta - \frac{s(z)}{z \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta}.$$

Finally, from (25), we have

$$\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta < \frac{s(z)}{\sigma(z)-1},$$

which implies

$$\begin{aligned} \frac{d}{dz} \log \left\{ P(z)^{1-\varepsilon} \left[\int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right] \right\} &= (\varepsilon - 1) \frac{\sigma(z) - 1}{zs(z)} \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta - \frac{s(z)}{z \int_z^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta} \\ &< -\frac{\sigma(z) - \varepsilon}{z} < 0. \end{aligned}$$

Applied to (49), this result implies

$$z^H(\boldsymbol{\mu}^o) > z^F(\boldsymbol{\mu}^o). \quad (51)$$

Therefore $|w_h^o| > |w_f^o|$ when $\Psi(z)$ is a decreasing function and $|w_h^o| < |w_f^o|$ when $\Psi(z)$ is an increasing function. We summarize this finding in

Lemma 5 *Let $q_H \searrow q_F$ and $\sigma'(z) > 0$ for $z \in (0, \bar{z})$. If $\Psi'(z) < 0$ for all $z \in (0, \bar{z})$, then $|w_h^o| > |w_f^o|$ and if $\Psi'(z) > 0$ for all $z \in (0, \bar{z})$, then $|w_h^o| < |w_f^o|$.*

Section 4

We divide this section in two parts. First, we prove the theoretical foundation of Figure 2. Then, we derive the second-best supply chain policy.

Let $q_F \approx q_H$ and $\gamma_F \approx \gamma_H$ so that both the home and the foreign country are symmetric. When $\boldsymbol{\mu} \gg 0$, all strategies must yield equal expected profits, such that the following conditions must hold jointly

$$\begin{aligned} \Pi_h(\mu_h, \mu_f, 1 - \mu_h - \mu_f) &= \Pi_f(\mu_h, \mu_f, 1 - \mu_h - \mu_f), \\ \Pi_h(\mu_h, \mu_f, 1 - \mu_h - \mu_f) &= \Pi_b(\mu_h, \mu_f, 1 - \mu_h - \mu_f), \\ \Pi_f(\mu_h, \mu_f, 1 - \mu_h - \mu_f) &= \Pi_b(\mu_h, \mu_f, 1 - \mu_h - \mu_f). \end{aligned}$$

Using the expressions for expected profits (30) and (31), the first condition rewrites $\pi[z^H(\mu_h, \mu_f, 1 - \mu_h - \mu_f)] = \pi[z^F(\mu_h, \mu_f, 1 - \mu_h - \mu_f)]$, where the functions z^H and z^F solve, respectively, $s[z^H(\boldsymbol{\mu})]\rho(1 - \mu_f) = 1$ and $s[z^F(\boldsymbol{\mu})]\rho(1 - \mu_h) = 1$. That is, the functions z^H and z^F are identical. Together with the monotonicity of $z \rightarrow \pi(z)$, this implies that $\Pi_h(\boldsymbol{\mu}) = \Pi_f(\boldsymbol{\mu})$ if and only if $\mu_h = \mu_f$.

Using (30) and (32), the second condition is

$$\delta\pi[z^F(\mu_h, \mu_f, 1 - \mu_h - \mu_f)]\rho + \delta^B\pi[z^B(\mu_h, \mu_f, 1 - \mu_h - \mu_f)](1 - \rho)\rho = k.$$

The function z^F and z^B are given respectively by $s[z^F(\boldsymbol{\mu})]\rho(1 - \mu_h) = 1$ and $s[z^B(\boldsymbol{\mu})]\rho[1 + (1 - \rho)(1 - \mu_h - \mu_f)] = 1$, so that z^F is solely a function of μ_h and z^B is solely a function of $\mu_h + \mu_f$.

Totally differentiating the equality above thus yields

$$\left. \frac{d\mu_h}{d\mu_f} \right|_{\Pi_h=\Pi_b} = -\frac{\delta^B d_{\mu_f} \pi[z^B(\mu_h, \mu_f, 1 - \mu_h - \mu_f)](1 - \rho)\rho}{\delta d_{\mu_h} \pi[z^F(\mu_h, \mu_f, 1 - \mu_h - \mu_f)]\rho + \delta^B d_{\mu_h} \pi[z^B(\mu_h, \mu_f, 1 - \mu_h - \mu_f)](1 - \rho)\rho}.$$

In the above expression, the notation $d_x f[g(x)]$ refers to the total derivative of f with respect to x , $d_x f[g(x)] = f'[g(x)]g'(x)$. Since z^B only depends on $\mu_h + \mu_f$, we have that $d_{\mu_f} \pi(z^B) = d_{\mu_h} \pi(z^B)$. Furthermore, $d_{\mu_f} \pi(z^B) = d_{\mu_h} \pi(z^B) > 0$ and $d_{\mu_h} \pi(z^F) > 0$. Hence, it follows that the curve $\Pi_h = \Pi_b$ slopes downward with a slope in $(-1, 0)$. Finally, proceeding similarly with the third condition returns

$$\left. \frac{d\mu_h}{d\mu_f} \right|_{\Pi_f=\Pi_b} = -\frac{\delta d_{\mu_f} \pi[z^H(\mu_h, \mu_f, 1 - \mu_h - \mu_f)]\rho + \delta^B d_{\mu_f} \pi[z^B(\mu_h, \mu_f, 1 - \mu_h - \mu_f)](1 - \rho)\rho}{\delta^B d_{\mu_h} \pi[z^B(\mu_h, \mu_f, 1 - \mu_h - \mu_f)](1 - \rho)\rho} < -1.$$

These results explain the properties of Figure 2.

We now turn to deriving the general expressions for the wedges w_f and w_h in the constrained optimum, when consumption subsidies are not feasible. We use (11) to calculate $dW(\boldsymbol{\mu})/d\mu_j$. Evaluated at the constrained optimum $\boldsymbol{\mu}^*$, where $dW(\boldsymbol{\mu}^*)/d\mu_j = 0$, we obtain

$$\frac{dW(\boldsymbol{\mu}^*)}{d\mu_j} = \Pi_j(\boldsymbol{\mu}^*) - \Pi_b(\boldsymbol{\mu}^*) + \sum_{i=h,f,b} \mu_i \frac{d\Pi_i(\boldsymbol{\mu}^*)}{d\mu_j} - \sum_{J=H,F,B} \delta^J P^J(\boldsymbol{\mu}^*)^{1-\varepsilon} \frac{d \log P^J(\boldsymbol{\mu}^*)}{d\mu_j} = 0, \quad j \in \{h, f\}.$$

Rearranging terms, and using the definition of the wedges in the constrained optimum, i.e., $w_j^* = \Pi_j(\boldsymbol{\mu}^*) - \Pi_b(\boldsymbol{\mu}^*)$, yields (19) in the main text. Next, from the expressions for expected profits, (30)-(32), we have

$$\begin{aligned} \frac{d\Pi_h(\boldsymbol{\mu}^*)}{d\mu_h} &= \delta^B \rho \frac{d\pi^{B,H}(\boldsymbol{\mu}^*)}{d\mu_h}, \\ \frac{d\Pi_h(\boldsymbol{\mu}^*)}{d\mu_f} &= \delta^H \rho \frac{\partial \pi[z^H(\boldsymbol{\mu}^*)]}{\partial z} \frac{\partial z^H(\boldsymbol{\mu}^*)}{\partial \mu_f} + \delta^B \rho \frac{d\pi^{B,H}(\boldsymbol{\mu}^*)}{d\mu_f}, \\ \frac{d\Pi_f(\boldsymbol{\mu}^*)}{d\mu_f} &= \delta^B \rho \frac{d\pi^{B,F}(\boldsymbol{\mu}^*)}{d\mu_f}, \\ \frac{d\Pi_f(\boldsymbol{\mu}^*)}{d\mu_h} &= \delta^F \rho \frac{\partial \pi[z^F(\boldsymbol{\mu}^*)]}{\partial z} \frac{dz^F(\boldsymbol{\mu}^*)}{d\mu_h} + \delta^B \rho \frac{d\pi^{B,F}(\boldsymbol{\mu}^*)}{d\mu_h}, \\ \frac{d\Pi_b(\boldsymbol{\mu}^*)}{d\mu_h} &= \delta^F \rho \frac{\partial \pi[z^F(\boldsymbol{\mu}^*), q_F]}{\partial z} \frac{dz^F(\boldsymbol{\mu}^*)}{d\mu_h} + \delta^B \left[\rho \frac{d\pi^{B,F}(\boldsymbol{\mu}^*)}{d\mu_h} + \rho(1 - \rho) \frac{d\pi^{B,H}(\boldsymbol{\mu}^*)}{d\mu_h} \right], \\ \frac{d\Pi_b(\boldsymbol{\mu}^*)}{d\mu_f} &= \delta^H \rho \frac{\partial \pi[z^H(\boldsymbol{\mu}^*), q_H]}{\partial z} \frac{dz^H(\boldsymbol{\mu}^*)}{d\mu_f} + \delta^B \left[\rho \frac{d\pi^{B,F}(\boldsymbol{\mu}^*)}{d\mu_f} + \rho(1 - \rho) \frac{d\pi^{B,H}(\boldsymbol{\mu}^*)}{d\mu_f} \right]. \end{aligned}$$

Substituting these derivatives into the expression for the wedges (19), we obtain

$$w_j^* = -\delta^K \left\{ \frac{1}{\sigma[z^K(\boldsymbol{\mu}^*)]} \frac{\partial \log \pi^K[z^K(\boldsymbol{\mu}^*)]}{\partial z} - \frac{\partial \log P^K[z^K(\boldsymbol{\mu}^*)]}{\partial z} \right\} P^K[z^K(\boldsymbol{\mu}^*)]^{1-\varepsilon} \frac{dz^K(\boldsymbol{\mu}^*)}{d\mu_j} \\ - \delta^B \left\{ \sum_K \frac{n^{B,K}(\boldsymbol{\mu}^*) s[z^{B,K}(\boldsymbol{\mu}^*)]}{\sigma[z^{B,K}(\boldsymbol{\mu}^*)]} \frac{d \log \pi^{B,K}(\boldsymbol{\mu}^*)}{d\mu_j} - \frac{d \log P^B(\boldsymbol{\mu}^*)}{d\mu_j} \right\} P^B(\boldsymbol{\mu}^*)^{1-\varepsilon}, \quad (52)$$

where $K = F$ if $j = h$ and $K = H$ if $j = f$. The first term on the right-hand side of (52) represents the net externality in state K , i.e., the business-stealing externality combined with the consumer-surplus externality. The second term represents the net externality in state B .

To compute these wedges, we need explicit expressions for the partial derivatives in (52). First note that the expressions for the semi-elasticities of the price index and profits in state $K \in \{H, F\}$ are given by (23) and (24), respectively. For state B , differentiate the expression for relative prices (27) to obtain

$$\frac{d \log z^{B,H}(\boldsymbol{\mu})}{d\mu_j} / \frac{d \log z^{B,F}(\boldsymbol{\mu})}{d\mu_j} = \left\{ 1 - z^{B,F}(\boldsymbol{\mu}) \frac{\partial \log \eta[z^{B,F}(\boldsymbol{\mu})]}{\partial z} \right\} / \left\{ 1 - z^{B,H}(\boldsymbol{\mu}) \frac{\partial \log \eta[z^{B,H}(\boldsymbol{\mu})]}{\partial z} \right\},$$

where $\eta(z) := \sigma(z)/(\sigma(z) - 1)$ is the markup factor. Together with condition (14), we obtain

$$\frac{d \log z^{B,K}(\boldsymbol{\mu})}{d\mu_h} = - \frac{\rho s[z^{B,F}(\boldsymbol{\mu})] - \rho^2 s[z^{B,H}(\boldsymbol{\mu})]}{\phi(\boldsymbol{\mu}) \left\{ 1 - z^{B,K}(\boldsymbol{\mu}) \frac{\partial \log \eta[z^{B,K}(\boldsymbol{\mu})]}{\partial z} \right\}}, \quad K \in \{H, F\} \quad (53)$$

and

$$\frac{d \log z^{B,K}(\boldsymbol{\mu})}{d\mu_f} = - \frac{\rho(1 - \rho) s[z^{B,H}(\boldsymbol{\mu})]}{\phi(\boldsymbol{\mu}) \left\{ 1 - z^{B,K}(\boldsymbol{\mu}) \frac{\partial \log \eta[z^{B,K}(\boldsymbol{\mu})]}{\partial z} \right\}}, \quad K \in \{H, F\}, \quad (54)$$

where

$$\phi(\boldsymbol{\mu}) := \sum_{L=H,F} n^{B,L}(\boldsymbol{\mu}) s[z^{B,L}(\boldsymbol{\mu})] \left\{ \frac{\sigma[z^{B,L}(\boldsymbol{\mu})] - 1}{1 - z^{B,L}(\boldsymbol{\mu}) \frac{\partial \log \eta[z^{B,L}(\boldsymbol{\mu})]}{\partial z}} \right\}.$$

Differentiating the price index in state B , (28), we obtain

$$\frac{d \log P^B(\boldsymbol{\mu})}{d\mu_h} = \frac{d \log z^{B,H}(\boldsymbol{\mu})}{d\mu_h} \frac{\partial \log \eta[z^{B,H}(\boldsymbol{\mu})]}{\partial \log z} \\ + n^{B,F}(\boldsymbol{\mu}) s[z^{B,F}(\boldsymbol{\mu})] \left[\frac{d \log z^{B,F}(\boldsymbol{\mu})}{d\mu_h} - \frac{d \log z^{B,H}(\boldsymbol{\mu})}{d\mu_h} \right] \\ + \rho \left[\int_{z^{B,F}(\boldsymbol{\mu})}^{z^{B,H}(\boldsymbol{\mu})} \frac{s(\zeta)}{\zeta} d\zeta + (1 - \rho) \int_{z^{B,H}(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta \right], \quad (55)$$

and

$$\begin{aligned}
\frac{d \log P^B(\boldsymbol{\mu})}{d\mu_f} &= \frac{d \log z^{B,F}(\boldsymbol{\mu})}{d\mu_f} \frac{\partial \log \eta[z^{B,F}(\boldsymbol{\mu})]}{\partial \log z} \\
&\quad + n^{B,H}(\boldsymbol{\mu}) s[z^{B,H}(\boldsymbol{\mu})] \left[\frac{d \log z^{B,H}(\boldsymbol{\mu})}{d\mu_f} - \frac{d \log z^{B,F}(\boldsymbol{\mu})}{d\mu_f} \right] \\
&\quad + \rho(1-\rho) \int_{z^{B,H}(\boldsymbol{\mu})}^{\bar{z}} \frac{s(\zeta)}{\zeta} d\zeta.
\end{aligned} \tag{56}$$

Finally, the change in profits is given by

$$\begin{aligned}
\frac{d \log \pi^{B,K}(\boldsymbol{\mu})}{d\mu_j} &= - \left(\sigma[z^{B,K}(\boldsymbol{\mu})] - 1 + \frac{\partial \log \sigma[z^{B,K}(\boldsymbol{\mu})]}{\partial \log z} \right) \frac{d \log z^{B,K}(\boldsymbol{\mu})}{d\mu_j} \\
&\quad - (\varepsilon - 1) \frac{d \log P^B(\boldsymbol{\mu})}{d\mu_j}, \quad j \in \{h, f\}, \quad K \in \{H, F\}.
\end{aligned} \tag{57}$$

To better understand these expressions, we consider the symmetric limiting case where $q_H \approx q_F = q$ and $\gamma_H \approx \gamma_F = \gamma$. In this setting, $\delta^F \approx \delta^H = \delta$, and $z^{B,F}(\boldsymbol{\mu}) \approx z^{B,H}(\boldsymbol{\mu}) =: z^B(\boldsymbol{\mu})$. As a result, the expression for the wedge (52) becomes

$$\begin{aligned}
w_j^* &= -\delta \left\{ \frac{\frac{\partial \log \pi[z^K(\boldsymbol{\mu}^*)]}{\partial z}}{\sigma[z^K(\boldsymbol{\mu}^*)]} - \frac{\partial \log P[z^K(\boldsymbol{\mu}^*)]}{\partial z} \right\} P[z^K(\boldsymbol{\mu}^*)]^{1-\varepsilon} \frac{dz^K(\boldsymbol{\mu}^*)}{d\mu_j} \\
&\quad - \delta^B \left\{ \frac{\frac{\partial \log \pi[z^B(\boldsymbol{\mu}^*), q]}{\partial z}}{\sigma[z^B(\boldsymbol{\mu}^*)]} - \frac{\partial \log P[z^B(\boldsymbol{\mu}^*)]}{\partial z} \right\} P[z^B(\boldsymbol{\mu}^*)]^{1-\varepsilon} \frac{dz^B(\boldsymbol{\mu}^*)}{d\mu_j}.
\end{aligned} \tag{58}$$

The term $\partial \log P / \partial z$ represents the consumer-surplus externality, whereas the term $(\partial \log \pi / \partial z) / \sigma$ represents the business-stealing externality.

Before considering the signs of the wedges, we need to show that $\mu_h^* = \mu_f^*$. Recall that the necessary first-order conditions for an interior allocation are

$$W_j(\boldsymbol{\mu}^*) = \Pi_j(\boldsymbol{\mu}^*) - \Pi_b(\boldsymbol{\mu}^*) - w_j^* = 0, \quad j = h, f.$$

For these two necessary conditions to hold jointly, it must be that

$$\Pi_h(\boldsymbol{\mu}^*) - w_h^* = \Pi_f(\boldsymbol{\mu}^*) - w_f^*.$$

Using (58) and the expressions for expected profits, we find that this equality indeed holds when $\mu_h^* = \mu_f^*$. This allocation corresponds to the unique optimal constrained allocation if W is globally concave. Proving the global concavity of W for general HSA preferences turns out to be a tricky task. Instead, we now show that $\mu_h^* = \mu_f^*$ is an optimum when preferences are symmetric translog. Additionally, we prove at the end of this Section that W is indeed globally concave when preferences are CES.

To prove that $\mu_h^* = \mu_f^*$ is an optimum when preferences are symmetric translog, we show that increasing μ_f is welfare-improving if and only if $\mu_f < \mu_h$. Specifically, we consider the variation $d\mu = (d\mu_h, d\mu_f, 0)$ with $d\mu_h = -d\mu_f$. Totally differentiating the welfare function (11) and imposing $d\mu_h - d\mu_f$ returns

$$\frac{dW(\boldsymbol{\mu})}{d\mu_f} \propto \frac{\partial\Omega(\mu_h)}{\partial\mu_h} - \frac{\partial\Omega(\mu_f)}{\partial\mu_f},$$

where

$$\Omega(\mu) := - \left(n(\mu)\pi[z(\mu)] + \frac{1}{\varepsilon - 1} P[z(\mu)]^{1-\varepsilon} \right),$$

and $n(\mu) = \rho(1 - \mu)$, the function z solves $s[z(\mu)]n(\mu) = 1$, P is given by (21) and $\pi(z)$ by (22). When preferences are symmetric translog, $s(z) = -\theta \log(z)$, and the function Ω becomes³³

$$\Omega(\mu) \propto - \left(\frac{1}{1 + \theta n(\mu)} + \frac{1}{\varepsilon - 1} \right) \left(\frac{1 + \theta n(\mu)}{\theta n(\mu)} \right)^{1-\varepsilon} \exp \left(\frac{1 - \varepsilon}{2\theta n(\mu)} \right).$$

The function Ω is convex as long as $\sigma(\mu) = 1 + \theta n(\mu) > \varepsilon$, which holds through Assumption 2. Hence, $\partial_\mu \Omega(\mu)$ is increasing, and $d_{\mu_f} W(\boldsymbol{\mu}) > 0 \iff \partial_{\mu_h} \Omega(\mu_h) > \partial_{\mu_f} \Omega(\mu_f) \iff \mu_h > \mu_f$.

With these results in mind, we turn to signing the wedges. Since $\mu_h^* = \mu_f^* =: \mu^*$, the wedges for the two sole-sourcing strategies are equal, i.e., $w_h^* = w_f^* =: w^*$. Furthermore, from (58), we have

$$w^* > 0 \quad \text{if} \quad \frac{\partial \log \pi(z)}{\partial z} > \sigma(z) \frac{\partial \log P(z)}{\partial z} \quad \text{for } z \in \{z^K(\mu^*), z^B(\mu^*)\},$$

and

$$w^* < 0 \quad \text{if} \quad \frac{\partial \log \pi(z)}{\partial z} < \sigma(z) \frac{\partial \log P(z)}{\partial z} \quad \text{for } z \in \{z^K(\mu^*), z^B(\mu^*)\},$$

which follows from the fact that z^K and z^B are decreasing in μ_j . General HSA preferences do not yield simple parametric conditions that satisfy these inequalities. But we can gain further insight by considering the special cases of CES preferences and translog preferences.

First, with symmetric CES preferences, $s(z) = \alpha z^{1-\sigma}$ and $\sigma(z) = \sigma$ is a constant. Using (23) with this market-share function, the consumer-surplus externality becomes

$$\frac{\partial \log P(z)}{\partial z} = \frac{s'(z)}{s(z)} \frac{1}{\sigma - 1} < 0.$$

Next, using (24), the business-stealing externality simplifies to

$$\frac{\partial \log \pi(z)}{\partial z} = \frac{s'(z)}{s(z)} \frac{\sigma - \varepsilon}{\sigma - 1} < 0.$$

³³Recall that under symmetric translog preferences, the elasticity of substitution is $\sigma(z) = 1 - 1/\log(z)$, the market clearing condition implies $\log z(\mu) = -1/[\theta\rho(1 - \mu)]$, and finally $[1/s(z)] \int_z^1 s(\zeta)/\zeta d\zeta = -\log(z)/2$.

Together they imply

$$\frac{\partial \log \pi(z)}{\partial z} - \sigma \frac{\partial \log P(z)}{\partial z} = -\frac{s'(z)}{s(z)} \frac{\varepsilon}{\sigma - 1} > 0 \text{ for all } z.$$

We have established

Lemma 6 *Let $q_H \searrow q_F$, $\gamma_H \searrow \gamma_F$, and let consumers hold symmetric CES preferences. Then, $w_h^* = w_f^* > 0$.*

Turning to symmetric translog preferences, let $s(z) = -\theta \log(z)$ for $z \in (0, 1)$. Now (23) implies

$$\frac{\partial \log P(z)}{\partial \log z} = \frac{1}{\log z - 1} - \frac{1}{2}$$

while (24) implies

$$\frac{\partial \log \pi(z)}{\partial \log z} = \left(1 - \frac{1}{\log z} - \varepsilon\right) \left(\frac{1}{\log z - 1} - \frac{1}{2}\right) + \frac{1}{2 \log z}.$$

Together, these two expressions imply

$$\frac{\partial \log \pi(z)}{\partial \log z} - \sigma(z) \frac{\partial \log P(z)}{\partial \log z} = \varepsilon + \frac{1}{\log z} \frac{\log z - 1}{\log z - 3}.$$

Under symmetric translog preferences, the adding up constraints of market shares generate relative prices $\log z^J(\mu) = -1/[\theta n(\mu)]$ for $n^J(\mu) = n(\mu) := \rho(1 - \mu)$, $J \in \{H, F\}$, and $\log z^B(\mu) = -1/[\theta n^B(\mu)]$ for $n^B(\mu) := \rho[1 + (1 - \rho)(1 - 2\mu)]$. It follows that

$$\frac{\partial \log \pi[z(\mu^*)]}{\partial z} > \sigma[z(\mu^*)] \frac{\partial \log P[z(\mu^*)]}{\partial z} \iff \varepsilon > \theta n^K(\mu^*) \frac{1 + \theta n^K(\mu^*)}{1 + 3\theta n^K(\mu^*)}, \quad K \in \{H, F, B\}.$$

Finally, we note that $n^B(\mu) > n(\mu)$ for $\mu < 1/2$, and that the product $x(1+x)/(1+3x)$ is increasing in x . We conclude that

$$\varepsilon < \theta n(\mu^*) \frac{1 + \theta n(\mu^*)}{1 + 3\theta n(\mu^*)} \implies w^* < 0,$$

and

$$\varepsilon > \theta n^B(\mu^*) \frac{1 + \theta n^B(\mu^*)}{1 + 3\theta n^B(\mu^*)} \implies w^* > 0.$$

Although the values of $n(\mu^*)$ and $n^B(\mu^*)$ are endogenous, it is possible to derive parametric restrictions that guarantee that one or the other of these inequalities holds. Specifically, if $\varepsilon < \theta n(\mu^*) \frac{1 + \theta n(\mu^*)}{1 + 3\theta n(\mu^*)}$ holds for the smallest possible value of n , then it must hold for all n . Therefore $w^* < 0$ if $\varepsilon < \theta \rho(2 + \theta \rho)/2(2 + 3\theta \rho)$. Similarly, if $\varepsilon > \theta n^B(\mu^*) \frac{1 + \theta n^B(\mu^*)}{1 + 3\theta n^B(\mu^*)}$ holds for the largest possible value of n^B , then it must hold for all n . Therefore $w^* > 0$ if $\varepsilon > \theta \rho(2 - \rho)[1 + \theta \rho(2 - \rho)]/(1 + 3\theta \rho(2 - \rho))$.³⁴

³⁴Technically, we also need to ensure that $\min\{\sigma[z(\mu^*)], \sigma[z^B(\mu^*)]\} = \sigma[z(\mu^*)] = 1 + \theta n(\mu^*) > \varepsilon$. This is not a

Lemma 7 Let $q_H \searrow q_F$, $\gamma_H \searrow \gamma_F$ and suppose that consumers have symmetric translog preferences. Then

$$\varepsilon < \frac{\theta\rho(2 + \theta\rho)}{2(2 + 3\theta\rho)} \implies w^* < 0,$$

and

$$\varepsilon > \frac{\theta\rho(2 - \rho)[1 + \theta\rho(2 - \rho)]}{1 + 3\theta\rho(2 - \rho)} \implies w^* > 0.$$

To conclude this section, we return to the special case of CES preferences to show that Lemma 6 generalizes to settings with asymmetric costs and risks. Returning to (52), we have already shown that the first term in parenthesis is negative. In state B , constant mark-ups simplify equations (53) and (54) to

$$\frac{d \log z^{B,K}}{d\mu_h} = -\frac{\rho \{s[z^{B,F}(\boldsymbol{\mu}^*)] - \rho s[z^{B,H}(\boldsymbol{\mu}^*)]\}}{\sigma - 1} < 0, \quad K \in \{H, F\},$$

and

$$\frac{d \log z^{B,K}}{d\mu_f} = -\frac{\rho(1 - \rho)s[z^{B,H}(\boldsymbol{\mu}^*)]}{\sigma - 1} < 0, \quad K \in \{H, F\}.$$

Furthermore, the semi-elasticity of the price index (55) and (56) becomes

$$\frac{d \log P^B(\boldsymbol{\mu}^*)}{d\mu_j} = -\frac{d \log z^{B,H}(\boldsymbol{\mu}^*)}{d\mu_j} = -\frac{d \log z^{B,F}(\boldsymbol{\mu}^*)}{d\mu_j} > 0, \quad j \in \{h, f\}.$$

Similarly, the semi-elasticity of profits (57) becomes

$$\frac{d \log \pi^{B,K}(\boldsymbol{\mu}^*)}{d\mu_j} = -(\sigma - \varepsilon) \frac{d \log z^{B,F}(\boldsymbol{\mu}^*)}{d\mu_j} = -(\sigma - \varepsilon) \frac{d \log z^{B,H}(\boldsymbol{\mu}^*)}{d\mu_j} > 0, \quad j \in \{h, f\}.$$

Combining these expressions, the second term in (52) becomes

$$\begin{aligned} & \sum_{K=H,F} \frac{n^{B,K}(\boldsymbol{\mu}^*)s[z^{B,K}(\boldsymbol{\mu}^*)]}{\sigma} \frac{d \log \pi^{B,K}(\boldsymbol{\mu}^*)}{d\mu_j} - \frac{d \log P^B(\boldsymbol{\mu}^*)}{d\mu_j} \\ &= \frac{\varepsilon}{\sigma} \frac{d \log z^{B,K}(\boldsymbol{\mu}^*)}{d\mu_j} < 0, \quad j \in \{h, f\} \text{ and } K \in \{H, F\}. \end{aligned}$$

Then (52) implies

$$\begin{aligned} w_h^* &= \rho \left(\frac{\varepsilon}{\sigma - 1} \right) (\delta^F \pi[z^F(\boldsymbol{\mu}^*)] + \delta^B \{ \pi[z^{B,F}(\boldsymbol{\mu}^*)] - \rho \pi[z^{B,H}(\boldsymbol{\mu}^*)] \}), \\ w_f^* &= \rho \left(\frac{\varepsilon}{\sigma - 1} \right) \{ \delta^H \pi[z^H(\boldsymbol{\mu}^*)] + \delta^B (1 - \rho) \pi[z^{B,H}(\boldsymbol{\mu}^*)] \}. \end{aligned}$$

Together with the planner's first-order conditions, these expressions yield

concern for the sufficient condition $\varepsilon < \theta n(\boldsymbol{\mu}^*) \frac{1 + \theta n(\boldsymbol{\mu}^*)}{1 + 3\theta n(\boldsymbol{\mu}^*)}$. Regarding $\varepsilon > \theta n^B(\boldsymbol{\mu}^*) \frac{1 + \theta n^B(\boldsymbol{\mu}^*)}{1 + 3\theta n^B(\boldsymbol{\mu}^*)}$, a sufficient condition for $\sigma[z(\boldsymbol{\mu}^*)] > \varepsilon$ for all $\boldsymbol{\mu}^*$ is $1 + \theta n(1/2) = 1 + \theta\rho/2 > \varepsilon$ since n is decreasing in μ .

Lemma 8 *Suppose consumers have symmetric CES preferences. Then*

$$w_h^* = w_f^* = \left(\frac{\varepsilon}{\sigma + \varepsilon - 1} \right) k > 0.$$

Evidently, in the CES case, the two wedges are positive and equal to one another, which implies that the constrained optimum can be achieved with a subsidy for diversification, i.e., $\varphi_b > 0$, with $\varphi_h = \varphi_f = 0$.

Finally, we conclude this section by showing that the first order conditions are necessary and sufficient when preferences are CES – that is, that the welfare function W is globally concave. When preferences are symmetric CES, the price index (21) in state $J \in \{H, F\}$ simplifies to

$$P[z^J(\boldsymbol{\mu}), q_J] = \frac{q_J}{z^J(\boldsymbol{\mu})} = n^J(\boldsymbol{\mu})^{\frac{1}{1-\sigma}} \cdot q_J, \quad (59)$$

while the price index in state B becomes

$$P^B(\boldsymbol{\mu}) = \left(\sum_{J=H,F} n^{B,J}(\boldsymbol{\mu}) q_J^{1-\sigma} \right)^{\frac{1}{1-\sigma}}. \quad (60)$$

Additionally, the profit of an active firm in state $J \in \{H, F\}$ is

$$\pi[z^J(\boldsymbol{\mu}), q_J] = \left(\frac{q_J^{1-\varepsilon}}{\sigma} \right) n^J(\boldsymbol{\mu})^{\frac{\varepsilon-\sigma}{\sigma-1}}.$$

and the profit of an active firm in state B purchasing an input from country $J \in \{H, F\}$ is

$$\pi^{B,J}(\boldsymbol{\mu}) = \left(\frac{q_J^{1-\sigma}}{\sigma} \right) \left(\sum_{\ell=H,F} n^{B,\ell}(\boldsymbol{\mu}) q_\ell^{1-\sigma} \right)^{\frac{\varepsilon-\sigma}{\sigma-1}}.$$

Under this special functional form, when the allocation is interior, $\mu_f > 0$, $\mu_h > 0$ and $\mu_b = 1 - \mu_f - \mu_h > 0$, the welfare function then simplifies to

$$W(\mu_h, \mu_f) = c \sum_{J=H,F,B} \delta^J P^J(\boldsymbol{\mu})^{1-\varepsilon} - k(2 - \mu_h - \mu_f),$$

where $c := 1/\sigma + 1/(\varepsilon - 1)$. Plugging in the expression for the price indices, (59) and (60), we have

$$W(\mu_h, \mu_f) = c \left[\sum_{J=H,F} \delta^J n^J(\boldsymbol{\mu})^{\frac{1-\varepsilon}{1-\sigma}} q_J^{1-\varepsilon} + \delta^B \left(\sum_{\ell=H,F} n^{B,\ell}(\boldsymbol{\mu}) q_\ell^{1-\sigma} \right)^{\frac{1-\varepsilon}{1-\sigma}} \right] - k(2 - \mu_h - \mu_f).$$

Double differentiating W , we obtain that the elements of the Hessian matrix are

$$\begin{aligned}\frac{\partial^2 W(\mu_h, \mu_f)}{\partial(\mu_f)^2} &\propto - \left(\delta^H n^H(\boldsymbol{\mu})^{\frac{\varepsilon-\sigma}{\sigma-1}-1} q_H^{1-\varepsilon} + \delta^B (1-\rho)^2 q_H^{2(1-\sigma)} P^B(\boldsymbol{\mu})^{2\sigma-1-\varepsilon} \right) < 0, \\ \frac{\partial^2 W(\mu_h, \mu_f)}{\partial(\mu_h)^2} &\propto - \left(\delta^F n^F(\boldsymbol{\mu})^{\frac{\varepsilon-\sigma}{\sigma-1}-1} q_F^{1-\varepsilon} + \delta^B [q_F^{1-\sigma} - \rho q_H^{1-\sigma}]^2 P^B(\boldsymbol{\mu})^{2\sigma-1-\varepsilon} \right) < 0, \\ \frac{\partial^2 W(\mu_h, \mu_f)}{\partial\mu_f \partial\mu_h} &\propto -\delta^B (1-\rho) q_H^{1-\sigma} [(q_F^{1-\sigma} - \rho q_H^{1-\sigma})] P^B(\boldsymbol{\mu})^{2\sigma-1-\varepsilon} < 0,\end{aligned}$$

where the constant of proportionality is the same. Inspection of the Hessian matrix shows that W is globally concave.

Section 5

In this section, we extend the numerical results of Section 6 in the main text to include simulations with both asymmetric risks *and* costs. Figure 6 extends the comparative statics of panels (c) and (d) in Figure 4 by comparing the effect of cross-country differences in risk on the optimal supply-chain policies under two different cost discounts.³⁵ Panels (a) and (b) in Figure 6 depict, respectively, the fraction of firms that adopt a particular supply chain strategy and the optimal policy under the symmetric cost simulation of Figure 4. Panels (c) and (d) plot the same variables for a positive cost discount of 5%.

When the cost discount is large but the risk premium is minimal, offshoring is *ceteris paribus* more profitable than onshoring, and firms locate their supply chains disproportionately in the foreign country, both in the equilibrium and in the constrained optimum. The wedges remain positive for both strategies, although they are no longer equal. Indeed, as discussed in Section 5, when risks are identical across countries but the input cost is lower in the foreign country, the social planner wants to tax relatively more the exclusive offshore relationships as the price index is lower in state F .

As in the case with symmetric costs depicted in Figure 4, when the cost differential is positive, an increase in the risk premium is associated with a greater fraction of diversified firms, a greater fraction of firms that form relationships only onshore, and a smaller fraction of firms that form relationships only abroad. However, in this case, firms face a tension between safe-but-expensive and riskier-but-cheaper suppliers. In panel (c), we see that for risk differentials greater than 10%, a cost discount of 5% is no longer enough to favor offshore investments, and firms locate disproportionately their supply chains in the safe-but-expensive home country.

Qualitatively, the effect of an increase in the risk premium on the optimal policies when the cost differential is positive also mimics what we have seen for symmetric costs. As the foreign risk increases, relatively more firms locate their supply chains exclusively in the home country, which triggers a relative increase in the price index in state F compared to state H , and with it an increase

³⁵The effect of a positive cost differential on the comparative statics for the risk premium is qualitatively similar for the cases of $\varepsilon = 1.2$ and $\varepsilon = 1.7$. To conserve space, we present only the latter.

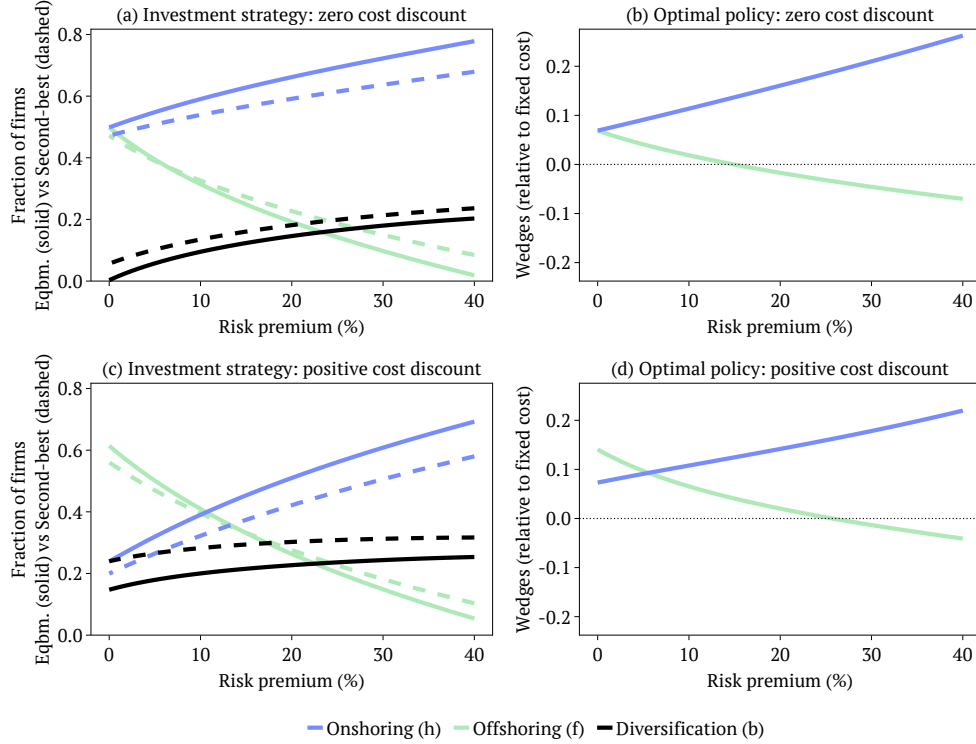


Figure 6: Second-Best Policies: Risk Differences Across Locations with Two Cost Scenarios

Note: Baseline simulation is $\varepsilon = 1.7$, $\gamma_H = \gamma_F = 0.9$, $q_H = q_F = 0.1$, $\theta = 8.0$, and $\rho = 0.7$. Fixed cost chosen so that $\min(\mu_b^*, \mu_b^0) \approx 0$ in the baseline symmetric simulation. This yields $k = 0.37$. The risk premium is computed as $-(\gamma_F - \gamma_H)/\gamma_H$, where we keep γ_H constant at its baseline value. The cost discount in panels (b) and (d) is 5%.

in w_h^* but a decrease in w_f^* . Compared with the symmetric cost simulation, the difference is now that the price index was initially lower in state F relative to state H due to the lower input cost in the foreign country. Thus, an increase in foreign risk initially shrinks the market's misallocation between home sourcing and foreign sourcing, and the wedges converge for a risk premium of 5%. Then, as the risk premium continues to grow, the price index in state F continues to increase, and the planner wants to tax relatively more the exclusive onshore relationships. Finally, for a sufficiently large risk premium, the planner's desire to shift the location of exclusive-sourcing from the home country to the foreign country implies again a tax on onshore relationships but a subsidy for investing in a single relationship abroad.

Figure 7 extends the comparative statics of panels (c) and (d) in Figure 5 by allowing for a positive risk premium. Panel (a) and (b) reproduce the results illustrated in panels (c) and (d) of the earlier figure, where $\gamma_H = \gamma_F$, while panels (c) and (d) in Figure 7 depict outcomes and policies with a positive risk premium of 15%.³⁶ When the cost discount is small relative to the risk premium, onshore sourcing relationships are relatively more attractive and a larger fraction of firms opt for strategy h . As the cost discount grows, the relative advantage of the foreign country

³⁶Once again the qualitative properties of the figure are similar for $\varepsilon = 1.2$ and $\varepsilon = 1.7$, so we present only the latter.

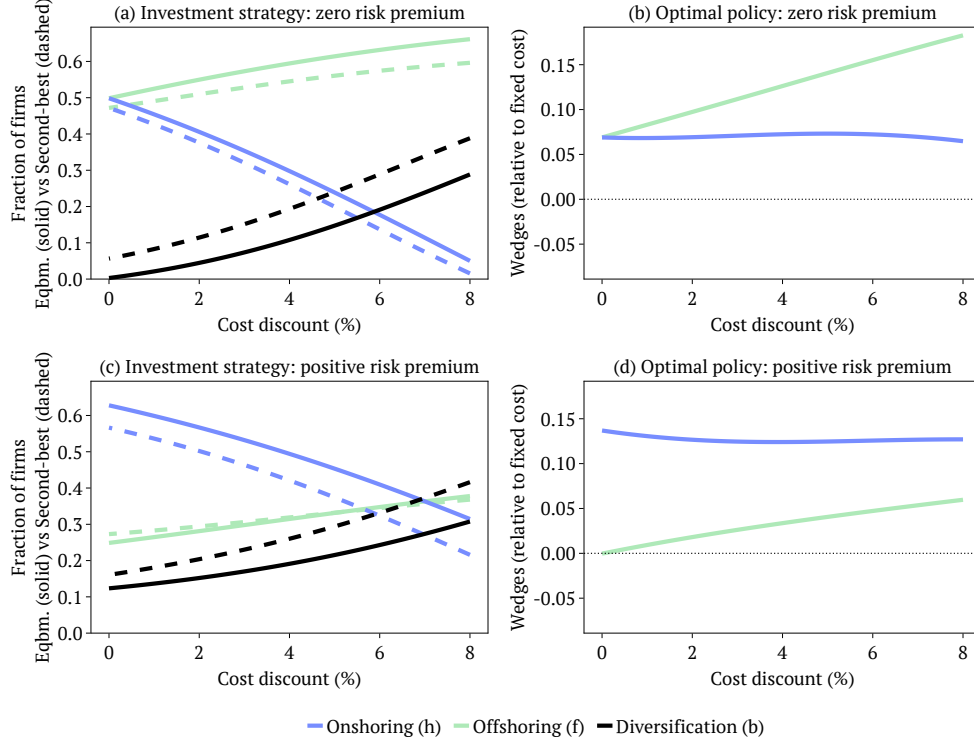


Figure 7: Second-Best Policies: Cost Differences Across Locations with Two Risk Scenarios

Note: Baseline simulation is $\varepsilon = 1.7$, $\gamma_H = \gamma_F = 0.9$, $q_H = q_F = 0.1$, $\theta = 8.0$, and $\rho = 0.7$. Fixed cost chosen so that $\min(\mu_b^*, \mu_b^0) \approx 0$ in the baseline symmetric simulation. This yields $k = 0.37$. The cost discount is computed as $-(q_F - q_H)/q_H$, where we keep q_H constant at its baseline value. The risk premium in panels (b) and (d) is 15%.

increases, and a larger fraction of firms decide to form their exclusive relationship with foreign suppliers. This intuitive pattern mimics the findings for the case where risks are symmetric.

Regarding the optimal policies, the wedge for strategy f is relatively smaller than that for strategy h when the cost discount is relatively small. This echoes the discussion of Figure 4; when the risk premium is large but the cost discount is small, the monopoly distortion is more severe in state F when the price index is higher, and the planner wishes to combat the higher prices in this state with a policy that tilts sourcing towards the foreign country. As the cost discount grows further, the fraction of firms that form exclusive relationships with foreign supplier rises, which, as in the scenario with symmetric risks, reduces the social benefit from promoting consumption in state F , and thus the gap between w_f^* and w_h^* .

We have explored a large variety of parameters besides those illustrated here. In general, the optimal policies hinge on which country is more attractive for exclusive sourcing based on the tradeoff between risk and cost and the implications of these asymmetric investments on the sizes of the monopoly distortions in the various states of the world.