

Environment in neoclassical growth models: Effects on growth, control, optimality.

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21.03.2018

Plan of the lecture

- ▶ The beginning: Limits to growth and discussion around it;
- ▶ Pollution is an externality: Coase's Theory;
- ▶ Optimal control theory and pollution: Keeler, Spence, Zeckhauser (1972).

Club of Rome

- ▶ Organization founded in 1968
- ▶ The initial goal of the Club was to promote sustainability solutions
- ▶ Regularly publishes simulations reports on future of the humankind
- ▶ These reports contain different scenarios of development
- ▶ Data is updated in accordance with discovery of new oil deposits, etc.
- ▶ Majority of predictions is rather pessimistic.

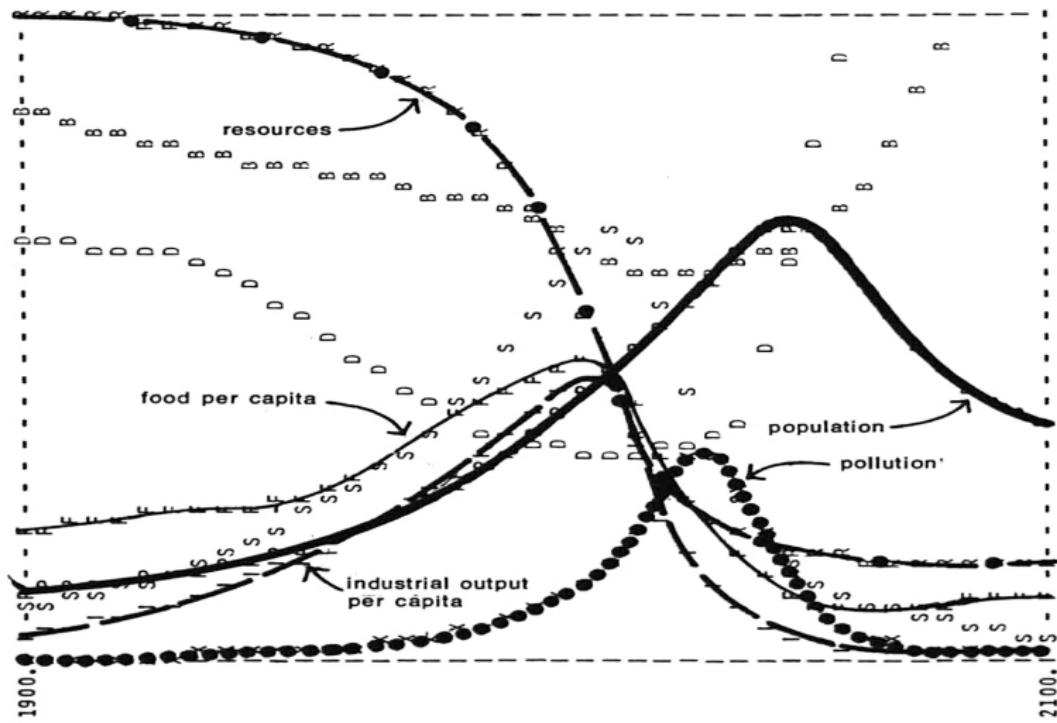
Result so far

“30 years of historical data compare favorably with key features of a business-as-usual scenario called the “standard run” scenario, which results in collapse of the global system midway through the 21st century.”

Basic arguments

- ▶ Main modelled quantities:
 - ▶ Population
 - ▶ Industrial production
 - ▶ Resources usage

are growing at exponential rates.
- ▶ This leads to:
 - ▶ Accelerating industrialization
 - ▶ Accelerating population growth
 - ▶ Widespread malnutrition
 - ▶ Depletion of natural resources
 - ▶ Deteriorating environment
- ▶ All these quantities are interrelated by some kind of positive feedback loops.

WORLD MODEL STANDARD RUN

Solow

- ▶ Price of the resource should increase as much as the interest rate
- ▶ There is a ceiling for resource extraction
- ▶ **Backstop technologies** would prevent the resource from total exploitation
- ▶ **Technical change** will reduce resource costs
- ▶ Gradual substitution of resources by capital
- ▶ The only condition: sufficient initial capital

Nordhaus

- ▶ The set of assumptions in Limits to growth is not robust
- ▶ Changing any of them will change results to more optimistic
- ▶ Ongoing *costless* technical change
- ▶ Empirical arguments:
 - ▶ There are plenty of recoverable resources
 - ▶ These resources are used more and more
 - ▶ Technology will enable us unlimited time of operation
 - ▶ Nuclear power and fusion provides resources for indefinite time.

Environment

- ▶ This discussion does not touch environmental issues altogether
- ▶ Environment can be treated as:
 - ▶ Renewable resource
 - ▶ Public good
- ▶ Recipe for environmental catastrophe:

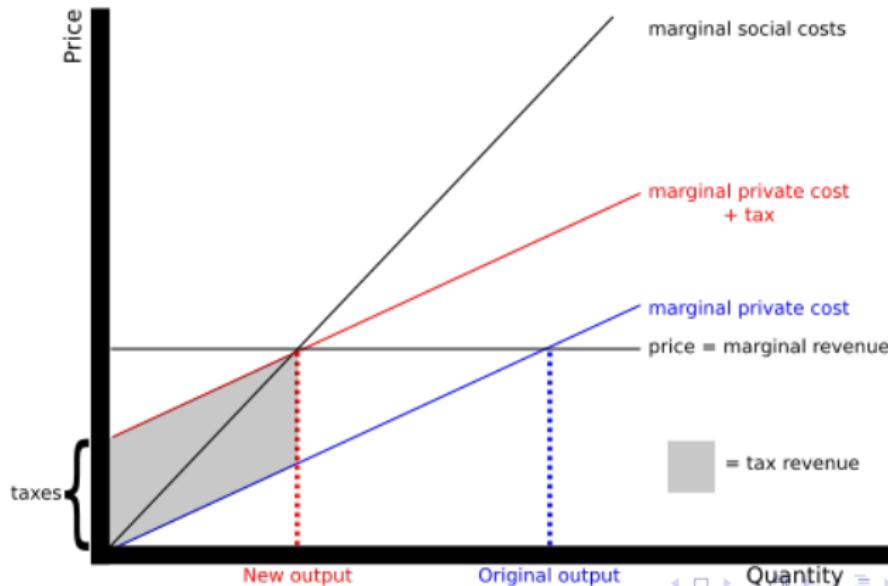
Growing production + growing population = environmental degradation!
- ▶ Pollution is a consequence of production and negatively impacts environment.

Pollution

- ▶ Pollution is modeled as a **negative externality**
- ▶ It results from industrial activity of firms
- ▶ Profit maximization does not include this
- ▶ Households utility is decreased and they cannot affect this
- ▶ Pollution is not a public good (antigood)
- ▶ It is not controlled by any single agent in the economy
- ▶ Two options: market can care of itself vs. optimal management

Pigou and social welfare

- ▶ Pigou suggested the tax to be imposed on externalities;
- ▶ The tax is precisely in the size of externality and is **distortion-free**



Double-dividend hypothesis

- ▶ Idea: Pollution is an externality, treat it with pigouvian logic!
- ▶ Coined already in Tullock (1967) “Excess Benefit”
- ▶ Environmental pigouvian tax may lead to double gain:
 1. From social welfare increase since pollution decrease
 2. From substituting usual taxes by environmental (distortion-free)
- ▶ Widely discussed from 1960s onwards
- ▶ Depends on the underlying model.

Main idea of Coase's Theorem

- ▶ Negative externality affects others
- ▶ Thus the price for a good with externality would include the negative externality already
- ▶ No need of interventions: agents will set up proper prices by themselves
- ▶ Is a widely used argument (till today!) against any government regulation of markets
- ▶ Still is valid in a **very** specific setup

Coase's Theory: Origins

- ▶ Based on the paper *The Problem of Social Cost* (1960)
- ▶ Does not have anything to do with Coase himself
- ▶ First formulated in the book of G. Stigler in 1966
- ▶ Is used everywhere since then, although:
 1. It is not game-theoretically sustainable
 2. Applicable only under perfect information
 3. Assumes zero transaction costs
 4. Assumes fully defined property rights **for any potential asset, good or service**

Think of futures markets: they cannot be complete *by definition*.

Coase's Theorem

1. A clear delineation of private property rights is an essential prelude to market transactions.
2. As long as private property rights are well defined under **zero** transaction cost, exchange will eliminate divergence and lead to efficient use of resources or highest valued use of resources.
3. The allocation of resources is **invariant** to the assignment of private property rights under zero transaction cost and zero income effect.

Implications

- ▶ Regardless of the nature of externality, private contracts will rule them out in the most efficient way
- ▶ Initial property rights should be assigned to the agents, to whom associated externality costs are the lowest
- ▶ Government should create institutions which would minimize transaction costs
- ▶ There is no place for central planner and/or environmental taxation!
- ▶ Dynamic pollution call for optimal management

Basic points

- ▶ Pollution is a special type of externality: affects all
- ▶ It may have not specific source (thus Coase's theorem does not apply)
- ▶ May be a stream or a stock
- ▶ May be factor of production and/or social welfare

Overview

- ▶ Was the first model to include pollution as an argument of utility
- ▶ Later environmental models follow the same pattern
- ▶ Discusses two alternative ways of modeling pollution
- ▶ Makes use of optimal control technique (as many later models)
- ▶ **Controls** are abatement and investments into capital
- ▶ Optimization is carried out for the *social planner*.

General setup

- ▶ Lifetime utility includes pollution stock P and pollution flow, \dot{P} as antigoods

$$\int_0^{\infty} e^{-\rho t} u(c, P, \dot{P}) \quad (1)$$

- ▶ Production depends on capital and both types of pollution:

$$\dot{K} = F(K_1, P, \dot{P}) - c - \beta F - aK \quad (2)$$

- ▶ Pollution changes due to production and abatement:

$$\dot{P} = g(K_1) - h(K_2) - d\beta F - bP \quad (3)$$

Model I: Pollution is not productive

Objective is to maximize lifetime utility (social welfare):

$$W = \int_0^{\infty} e^{-\rho t} u(c, P) \rightarrow \max_{\alpha, \beta}, \frac{\partial U}{\partial c} > 0, \frac{\partial U}{\partial P} < 0 \quad (4)$$

Production depends only on capital:

$$Y = f(K), f' > 0, f'' < 0 \quad (5)$$

Capital is accumulated due to investments:

$$\dot{K} = (1 - \alpha - \beta)f(K) - aK \quad (6)$$

Pollution grows proportional to output but slowly decreases:

$$\dot{P} = (1 - \beta d)f(K) - bP \quad (7)$$

Motivation

- ▶ Describes situations where environment does not play a productive role (water pollution)
- ▶ Combating pollution competes with output increase
- ▶ Technology may increase efficiency of abatement, d
- ▶ Environment regenerates itself (is renewable)
- ▶ Strong resemblance with R-C-K (previous lecture) economy corrected for pollution.

Steady states

Hamiltonian and FOCs Steady states are characterized by zero growth of state variables:

$$\begin{aligned}\dot{K} = 0 &\rightarrow f(K)(1 - \alpha - \beta) = aK, \\ \dot{P} = 0 &\rightarrow f(K)(1 - \beta d) = bP.\end{aligned}\tag{8}$$

and constant co-states:

$$\begin{aligned}u_c(\alpha f(K), P) &= \kappa, \\ \dot{\kappa} = 0 &= \kappa(r + a - f') - \pi f' + \beta(\pi d - \kappa)f', \\ \dot{\pi} = 0 &\rightarrow u_P = (r + b)\pi.\end{aligned}\tag{9}$$

There are two possible steady states in this model:

- ▶ Golden Age equilibrium with $\alpha > 0, \beta > 0$,
- ▶ Murky Age equilibrium with $\alpha > 0, \beta = 0$.

For **Golden Age** equilibrium two equations are to be satisfied:

$$\begin{aligned}dc &= bP - adK + (d - 1)f(K), \\(r + b)\pi &= -u_c \frac{r + b}{d}\end{aligned}\tag{10}$$

and capital is defined from

$$f'(K) = \frac{r + a}{1 - 1/d}.\tag{11}$$

Murky Age

Murky Age is defined as an equilibrium with no control on pollution ($\beta = 0$).

Capital is defined as:

$$f'(K) = \frac{r + a}{1 + \pi/\kappa} \quad (12)$$

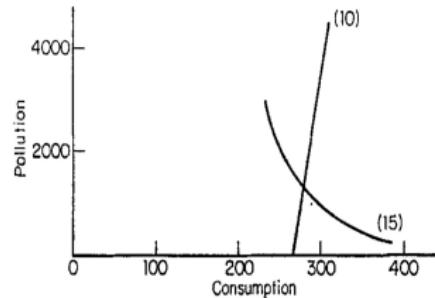
and pollution level from

$$P'(K) = \frac{C_1 f'' - C_2 \alpha f' [u_{cc} u_P - u_c u_{cP}]}{u_{cP} u_P - u_c u_{PP}} \quad (13)$$

together with (8) this defines unique no-depollution equilibrium.

Comparison

- ▶ In Golden Age pollution reduction efforts are non-zero;
- ▶ Golden Age equilibrium exists, if:
 1. The (11) is satisfied,
 2. Consumption defined by the pair (10) is between 0 and $f(K) - aK$.
- ▶ Murky Age equilibrium exists if:
 1. Capital defined by (12) is higher than golden age one.
- ▶ Only one equilibrium may exist at a time.



The Golden Age Equilibrium.

Model II: Pollution enters production

- ▶ Pollution enters both the utility and production;
- ▶ Utility is separable:

$$u(c, P) = g(c) - h(P), \quad (14)$$

- ▶ Labour has two competitive uses:
 1. Production with the use of pollutant, $j(L_1)$,
 2. And ordinary production with $L - L_1$:

$$c = F(L - L_1, j(L_1)) \rightarrow f(L_1), \quad (15)$$

- ▶ There is no capital.

Hamiltonian

Hamiltonian with dropped discount factor is then:

$$\mathcal{H} = g(f_1(L)) - h(P) + \pi(a(L_1 - bP) + q(L - L_1) + sL_1; \quad (16)$$

where q, s are nonnegativity lagrange multipliers.

F.O.C. for L_1 is:

$$\mathcal{H}_{L_1} = g'f' + \pi j' + s = 0, \quad s \geq 0, \quad sL_1 = 0. \quad (17)$$

Analysis

- ▶ First observe, that $L_1 < L$;
- ▶ As long as L_1 is positive, $s = 0$;
- ▶ There is a lower bound for π :

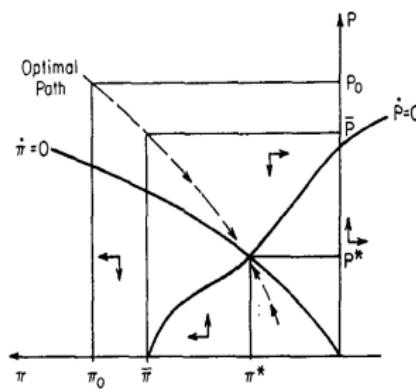
$$\bar{\pi} = \frac{g'(f(0))f'(0)}{j'(0)}; \quad (18)$$

- ▶ As long as $\pi < \bar{\pi}$ the usage of pollutant in production is zero, $L_1 = 0$.

Dynamics

The co-state evolution is

$$\dot{\pi} = (q + b)\pi + h'; \quad (19)$$



Phase diagram for Model II.

Implications

- ▶ It is not optimal to ignore pollution forever;
- ▶ However it is not optimal either to ban pollutant immediately and forever;
- ▶ Pollutant production is allowed below \bar{P} ;
- ▶ If $P_0 > \bar{P}$, pollutant is banned until its concentration is lowered to \bar{P} ;
- ▶ After reaching this point pollutant may be used while maintaining $\dot{P} < 0$.

Summary

- ▶ If pollution affects only utility but not production, policy depends on initial conditions:
 1. If initial capital is high enough, Golden Age policy may be realised;
 2. It has lower consumption and capital levels but lower pollution;
 3. Otherwise Murky Age policy is adopted granting higher consumption.
- ▶ This is the root of all “grow first clean up later” policies;
- ▶ If pollutant enters production function, then:
 1. Economy has always non-zero pollution levels;
 2. Optimal policy is to gradually reduce pollution by limited use of pollutant;
 3. Later models include feedback to pollutant stock from capital.

Summary on pollution

- ▶ Market economy cannot handle pollution problem properly;
- ▶ This is especially true for large-scale systems;
- ▶ Coase's theorem have a very limited application (local one);
- ▶ We need central planner;
- ▶ Depending on the structure of the model, optimal policy is different;
- ▶ There is no analogue for golden rule or etc.;
- ▶ The discussion on the proper way to include pollution into modelling is still ongoing;
- ▶ Today it is combined with exhaustible resources also (scarce);
- ▶ Still no technology influence.

Literature

- ▶ Nordhaus, W. D. (1974). Resources as a Constraint on Growth. *The American Economic Review*, 64(2), pp. 2226 .
- ▶ Coase R. (1960) The Problem of Social Cost. *Journal of Law and Economics*, 3, pp .1-44 ;
- ▶ Keeler E., Spence M., Zeckhauser R. (1971) The Optimal Control of Pollution. *Journal of Economic Theory*, No. 4, pp. 19-34.

What's next

Overall:

- ▶ Endogenous growth theory explicitly accounts for technical change;
- ▶ We consider ways to combine technical change *and* pollution control;
- ▶ These ways differ depending on the type of technical change and source of pollution!

Next lecture:

- ▶ Environmental Kuznets curve;
- ▶ Prototype examples of endogenous growth and pollution
- ▶ Paper: Gradus&Smulders (1993)

Hamiltonian

[Back](#)

Hamiltonian is linear in controls:

$$\mathcal{H} = e^{rt} [u(c, P) + \kappa[(1 - \alpha - \beta)f - aK] + \pi[(1 - \beta)d)f - bP]] \quad (20)$$

co-state equations are:

$$\begin{aligned}\dot{\kappa} &= -\mathcal{H}_\kappa + \kappa r = -u_c \alpha f' + \kappa[r + a - (1 - \alpha - \beta)f'] - \pi(1 - \beta)d)f', \\ \dot{\pi} &= -\mathcal{H}_\pi + \pi r = -u_P + (r + b)\pi.\end{aligned}\quad (21)$$

and F.O.C.s are:

$$\begin{aligned}\mathcal{H}_\alpha &= e^{-rt}(u_c - \kappa)f, \\ \mathcal{H}_\beta &= e^{-rt}(-\kappa - d\pi)f.\end{aligned}\quad (22)$$