

# Complexity

*Computational Economics, spring term 2012*

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# complex systems

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## ▶ complex systems

- ▶ unpredictable
- ▶ robust
- ▶ large events
  - ❖ magnitude of effect not foreseeable
  - ❖ “power law”
- ▶ dynamic
  - ❖ neither (static) equilibrium nor chaos
  - ❖ somewhere in between “order” and “chaos”
- ▶ emerging phenomena
  - ❖ bottom up
  - ❖ self-organization
  - ❖ novelty
  
- ▶ complex  $\neq$  complicated

# complex systems

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- ▶ entities in a complex system
  - ▶ agents
    - ❖ diverse
    - ❖ interdependent
    - ❖ connected
    - ❖ adaptive
  - ▶ operate within environment
  
- ▶ is the economy getting more complex?
  - ▶ yes, on all levels:
    - ❖ people are more connected
    - ❖ actions become more interdependent and require more coordination
    - ❖ work is more diverse
    - ❖ companies / strategies / products / ... change must faster

# complex systems

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## ▶ what are the interesting aspects?

### ▶ emergence

- ❖ macro level  $\Leftrightarrow$  micro level
- ❖ differs in kind
- ❖ bottom up, no central control
- ❖ self organization

### ▶ phase transition

- ❖ “tipping points”
- ❖ non-linear
  - ▶ marginal responses change

### ▶ innovation

- ❖ adaptation
- ❖ novelty

# complex systems

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## ▶ what is required

- ▶ precise definitions
  - ❖ evaluate & compare situations
- ▶ new tools
  - ❖ mostly computational
  - ❖ e.g., simulation
- ▶ new vocabulary
  - ❖ “self organized criticality”, “cellular automata”, “agent-based modelling”, “adaptive systems”, “learning”, ...

# diversity

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## ▶ why is it important?

- ▶ innovation
- ▶ robustness

## ▶ important aspects

- ▶ positive feedback
  - ❖ “diversity begets diversity”
- ▶ harshness of environment
  - ❖ weak selection pressure
- ▶ situation dependent objectives and requirements
  - ❖ strategy must be fit for purpose
- ▶ changing requirements
  - ❖ co-evolution

# diversity

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## ▶ how to measure it

- ▶ measures of variation
- ▶ entropy measures
- ▶ distance measures
- ▶ attribute measures

## ▶ complex systems in economy ↔ ecology

- ▶ representation
- ▶ size of leaps
- ▶ interim viability
- ▶ retrievability

# emergence

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## ▶ what it is

- ▶ spontaneous creation of order and / or functionality
- ▶ bottom up, no central planning
- ▶ breaking symmetry
- ▶ “more is different” (Philip Warren Anderson)

## ▶ types

- ▶ simple  $\Leftrightarrow$  complex
- ▶ weak  $\Leftrightarrow$  strong



# emergence

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## ▶ example: culture

- ▶ shared set of beliefs, behaviours, routines
- ▶ when people meet
  - ❖ action sets, belief systems
  - ❖ actions are interdependent
  
- ▶ model
  - ❖ consistency of beliefs and actions
  - ❖ avoid cognitive dissonance
  - ❖ “coordination game”
  - ❖ → culture is emerging pattern
  
- ▶ functionalities
  - ❖ predictions about other people’s behaviour
  - ❖ dealing with new situations

# networks

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## ▶ “space matters”

- ▶ connections between agents
  - ❖ (not) everybody is connected with everybody
  - ❖ influence actions, reactions, adaptations
- ▶ importance of networks can depend on situation
  - ❖ e.g., spread of diseases

## ▶ properties

- ▶ nodes and edges
  - ❖ degree: *number of connections to other agents*
  - ❖ path length: *minimum number of edges from A to B*
- ▶ some types
  - ❖ random nets
  - ❖ hub and spokes
  - ❖ small world

# networks

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## ▶ example: www

- ▶ many sites with few links; few sites with many links
- ▶ power law:
  - ❖ number of nodes of degree  $k$  is proportional to  $1/k^2$

## ▶ how do networks emerge?

### ▶ examples

- ❖ social networks
  - ▶ agents with common attributes, preferences, etc.
- ❖ preferential attachment model
  - ▶ links to already highly connected nodes
  - ▶ “first mover advantage”
- ❖ alternatively / additionally: quality of nodes
  - ▶ example: Google wasn't the first search engine

# feedback

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## ▶ main types

### ▶ positive feedback

- ❖ “more creates more”
- ❖ examples
  - ▶ ants' pheromone trails (reinforcement)
  - ▶ fashions (within limits) & trends
  - ▶ panic reactions
  - ▶ contagion in markets

### ▶ negative feedback

- ❖ “more creates less”
- ❖ examples
  - ▶ queues
  - ▶ trend followers ↔ individualists / contrarians

## ▶ feedback ↔ externalities

# feedback

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## ▶ path dependences

- ▶ current decisions affect future outcome and possibilities
- ▶ a few actions can trigger large scale changes
- ▶ tipping point

## ▶ feedback & diversity

- ▶ combination can make systems robust / instable

	positive feedback	negative feedback
no / little diversity		
much diversity		

# positive feedback

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- ▶ example: Thomas Schelling's "Segregation model"
  - ▶ grid; each cell represents one household
  - ▶ two types of households: red / blue
  - ▶ households don't want all neighbors to be different from themselves
    - ❖ if minimum level of similarity is exceeded, households are happy
    - ❖ if not, they move
  - ▶ effects
    - ❖ increase similarity in new neighborhood
    - ❖ decrease similarity in old neighborhood (old neighbors likely to follow)
  - ▶ results
    - ❖ fairly tolerant on micro level, strong segregation on macro level
    - ❖ once beyond tipping point, system will not "de-segregate"
  - ▶ extensions
    - ❖ households have different thresholds for minimum similarity

# negative feedback

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## ▶ examples

- ▶ increasing (decreasing) tourist numbers will decrease (increase) attractiveness of resort
- ▶ price increases will lower demand

## ▶ in combination with ...

- ▶ externalities
  - example: air fares for short-hall trips  $\Leftrightarrow$  train ticket prices
- ▶ positive feedback
  - example: increased prices  $\rightarrow$  increased supply & decreased demand
- ▶ network structures
  - example: local / global players in locally regulated markets

# self-organised criticality

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- ▶ self organisation ...
  - ▶ emergence phenomenon
  - ▶ aggregate exhibits patterns & structure not present in individuals
  
- ▶ + criticality ...
  - ▶ small events trigger large cascades of events
  - ▶ tipping point
  
- ▶ = self-organized criticality
  - ▶ self-organisation towards critical states
  - ▶ big events *can* results
    - ❖ often: no big events => false sense of security
    - ❖ power law



# self-organised criticality

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## ▶ power laws

- ▶ probability of event of size  $k$  is proportional to  $1/(k^b)$
- ▶ important properties:
  - ❖ fat tails
  - ❖ scale invariant

## ▶ general examples

- ❖ sandpile models
- ❖ traffic jams
- ❖ certain contagion / herding models
- ❖ network effects

## ▶ actual outcome depends on

- ❖ network structure
- ❖ type of feedback
- ❖ adaption within system

# randomness

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- ▶ potential sources of randomness in models
  - ▶ by definition / engineering
    - ❖ e.g., Monte Carlo approach
  - ▶ error terms
    - ❖ e.g., (external) randomness causes (further) randomness
  - ▶ fundamental randomness
    - ❖ e.g., quantum mechanics
  - ▶ complexity
    - ❖ e.g., cellular automata
    - ❖ interdependence & interactions

# randomness

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## ▶ randomness due to complexity

- ▶ main characteristics
  - ❖ interdependent rules create changing events and responses
  - ❖ adaptiveness system
- ▶ distributions are not necessarily stationary

## ▶ learning in complex systems

- ▶ co-evolution
- ▶ learning assumes (some sort of) stationary (within limits)
- ▶ lessons learned might have a “sell-by” date

# randomness

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## ▶ examples in economics & finance

- ▶ collapse of LCTM (Long Term Capital Management)
  - ❖ “bets” on long term equilibria → problems if bubbles persist too long
  - ❖ pricing models assume stationary distributions → problems if violated
- ▶ subprime crisis
  - ❖ flawed assumptions (ex post)
    - ▶ mark to model
    - ▶ bundles of loans → central limit theorem should hold
    - ▶ stationary distributions
    - ▶ little inter-connectedness
  - ❖ positive feedback
    - ▶ necessary down-payments lowered
      - subprime market reacts first to economic problems
    - ▶ insurance via CDO (pay off when bundles go bad)
      - insufficient deposits

# complex systems

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- ▶ the ingredients revisited
  - ▶ agents are
    - ❖ diverse
    - ❖ interdependent
    - ❖ connected
    - ❖ adaptive
  - → influence everything, control nothing
- ▶ systems
  - ❖ exhibit emergence & self organisation
  - ❖ become unpredictable (i.e., random)
  - ❖ can be robust ↔ collapse

# complex systems

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## ▶ dealing with complexity

- ▶ traditional decision theory rational choice models of limited use in CS
- ▶ change of attributes
  - ❖ modification of network structures
  - ❖ diversity (distribution; tail events) & innovation
  - ❖ adaptation rate, learning, etc.
  - ❖ selection & fitness criteria
- ▶ control ↔ efficiency
- ▶ example: institutions that have existed for more than 500 years
  - ❖ ca. 40 universities
  - ❖ ca. 125 businesses
    - ▶ approx. 2/3: recreational / leisure / etc. (restaurants, breweries, etc.)
    - ▶ rest: pharmacies, jewellery makers, cheese makers, knife makers
  - ❖ NOT: banks, construction businesses etc.

# literature

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## ▶ background reading, additional material

- ▶ Thomas C Schelling, *Micromotives and Macrobehaviour*, Norton & Company, New York 1978.
- ▶ Scott E Page, *The Difference: How the Power of Diversity Creates Better Groups, Firms, Schools, & Societies*, Princeton University Press 2007
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- ▶ John H. Holland, *Hidden Order. How Adaptation Builds Complexity*, Basic Books, New York 1995.
- ▶ Nigel Gilbert and Klaus G Troitzsch, *Simulation for the Social Scientist*, Open University Press 2005